Gross Worker Flows over the Business Cycle*

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Abstract

We build a hybrid model of the aggregate labor market that features both standard labor supply forces and frictions in order to study the cyclical properties of gross worker flows across the three labor market states: employment, unemployment, and non-participation. Our goal is to assess the relative importance of frictions and labor supply in accounting for fluctuations in labor market outcomes. Our parsimonious model is able to capture the key features of the cyclical movements in gross worker flows and indicates an important role for both frictions and labor supply.

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1 Introduction

Benchmark business cycle models offer vastly different views concerning the role of labor supply in accounting for business cycles. At one extreme, following the work of Lucas and Rapping (1969), benchmark real business cycle models view fluctuations in hours as the optimal response of labor supply to fluctuations in prices (i.e., wages and interest rates). At the other extreme, following the work of Mortensen and Pissarides (1994), workers are viewed as passive, always wanting to work but subject to frictions that sometimes prevent them from working. A striking feature of the literature is the extent to which it is dominated by models that correspond to one of these two extreme views. To us it seems reasonable to think that both extremes capture some part of reality. This raises the question of how to assess the importance of each. The objective of this paper is to take a first step in addressing this issue.

To approach this question, we adopt the view that participation decisions reflect desired labor supply and unemployment reflects frictions that create a gap between actual and desired labor supply. This view leads us to focus on the behavior of gross worker flows over the business cycle as a way to assess the importance of labor supply and frictions in accounting for business cycle fluctuations in the labor market. Specifically, we build a parsimonious hybrid model of individual labor supply that features both standard labor supply forces as well as frictions. We aggregate across heterogeneous households to yield a model of aggregate labor supply in the presence of frictions, and assess the ability of different aggregate shocks to generate the cyclical patterns for gross worker flows that are found in the data.

Our model assumes that households differ in three ways at any point in time: they have different payoffs of market work relative to not working, some have (access to) jobs and others do not, and some have more assets than others. Job opportunities arrive randomly to households—a key idiosyncratic factor. Workers are risk-averse but cannot insure directly; however, they can accumulate an asset in order to provide self-insurance. Asset wealth is
important in that there is a wealth effect on labor supply, capturing the natural notion a
“the need of income” is a cause for increasing one’s labor supply. While stylized, we think
this simple model captures the essence of the situation that most workers face throughout
their life.

Most workers are quite far from the boundary of indifference between working and not
working: for example, those with high returns to market work typically have a strong prefer-
ence to work and those with low returns to market work typically prefer not to work.
However, a non-negligible group of workers is close enough to indifferent that idiosyncratic
or aggregate shocks can make them switch participation status over the near term. This
group turns out to be key for understanding both gross flows and the movement of stocks
over the cycle. It is thus important how our model places restrictions on the size and com-
position of this group. Our calibration—the selection of key parameters for utility, work
payoff, and job availability—is designed to match the average gross flows. We then ask how
these flows move over time when there are aggregate shocks to the market conditions that
individuals face.

We consider two types of aggregate shocks: shocks to job availability, or equivalently,
frictions, and shocks to prices. We consider two components to friction shocks—one to the
employment-finding rate and another to the employment-loss rate—and two components
to price shocks: one that raises everybody’s return to market activity and another to the
interest rate. The aggregate shocks are calibrated to be empirically reasonable in magnitude.
In the context of this model we ask three main questions. First, do the outcomes—flows and
stocks—move like they move the data? Second, how important are each of the shocks to the
different components of market conditions? And third, what role does labor supply play?

We have three main findings. First, our relatively parsimonious model does a good job of
accounting for the key features of fluctuations in \( E, U, \) and \( N \) and in the gross worker flows
between these three states. We offer intuition to argue that the simulation results reflect
some basic economic forces present in the model, suggesting that our results capture some robust economic mechanisms at work in the model.

Second, we find that both kinds of shocks—those to prices and those to frictions—play key roles in allowing the model to match the data. To most, it is not surprising that the latter are important for understanding the movements in unemployment. What is less obvious is that a model without aggregate price shocks fails to match the data. In particular, in this case the participation rate becomes much too volatile and countercyclical.

The reason for this result is our third, and arguably most important finding: labor supply responses play a key role. Specifically, if we were to fix participation exogenously, fluctuations in job availability alone would do a decent job of accounting for fluctuations in $E$, $U$ and $N$. In particular, movements between $E$ and $U$ could be pinned down by appropriate choices of the job-finding and job-loss rates; moreover, by definition $N$ would not fluctuate, but since its volatility in the data is not so high, this would not be a major flaw. However, in the data, gross flows between $N$ and each of $E$ and $U$ are substantial, volatile, and cyclical.\(^1\) Thus, it appears quite important to allow for an endogenous participation decision. And when labor supply responses to friction shocks are allowed, the model predicts a strong dampening of their effect on employment. Intuitively, when it is hard to find a job, workers with a job stay on longer and workers without a job become less choosy. Thus, without any price movements, in particular wage movements, aggregate employment does not fall much at all as jobs become harder to find, participation rises (becomes countercyclical), and the cyclical fluctuations in participation become large—three features that are all at odds with the data. This also explains the intuition why the model with a constant wage cannot match the data, as was mentioned above.

The presence of an empirically plausible labor supply response along the extensive margin—plausible in the sense of being consistent with average gross flows—has important implications

\(^1\)Looking across countries, $N$ exhibits substantial variation as well. See, for example, Rogerson and Shimer (2010).
for evaluating theories in which labor supply is not necessarily assigned a large role. Put somewhat differently, exogenously shutting down the participation margin hides the fact that such a model contains quantitatively important forces with counterfactual predictions.

Our paper is related to several others in the literature. Many papers have studied properties of gross flows, including, for example, Abowd and Zellner (1985), Poterba and Summers (1986), Blanchard and Diamond (1990), Davis and Haltiwanger (1992), Fujita and Ramey (2009), Elsby, Hobijn, and Şahin (2012), and Shimer (2012).

Ham (1982) was an early attempt to rigorously study unemployment in a labor supply setting, showing that unemployment spells could not be interpreted as optimal labor supply responses. Consistent with his findings, our model features both an operative labor supply margin and unemployment, but unemployment is a departure from desired labor supply. More recently, Low, Meghir, and Pistaferri (2010) study life cycle labor supply in the presence of frictions. Our study is very much in the spirit of theirs, though because our focus is on aggregate effects over the business cycle, our individuals are described in a more stylized manner (without regard to age, etc.).

Our analysis is also related to several recent papers that seek to extend general equilibrium business cycle models of employment and unemployment to allow for a participation decision. The key feature that distinguishes our paper from these is our focus on gross worker flows—these papers only consider labor market stocks. Alternatively, our model can be viewed as adding frictions to the labor supply model of Chang and Kim (2006), which features idiosyncratic shocks, indivisible labor, and incomplete markets. We discuss how the specific findings in our paper relate to some of these papers in greater detail in Section 6.

An outline of the paper follows. In the next section we document the key business cycle facts for gross worker flows among the three labor market states for the US over the period 1968–2009. Section 3 describes our theoretical framework. Section 4 describes how we...
investigate business cycle fluctuations and Section 5 presents our results. Section 6 discusses our paper relative to the related literature and Section 7 concludes.

2 Gross Worker Flows Over the Business Cycle

This section documents the business cycle facts for gross worker flows that serve as the focus of our analysis. We estimate gross worker flows using the matched Current Population Survey (CPS) data for the period 1968–2009 following an algorithm similar to that used elsewhere.\(^3\)

While some of the patterns that we highlight have been documented in previous work (see, e.g., Blanchard and Diamond (1990) and Shimer (2012)), some details vary across studies and it is important that we have a consistent set of statistics for the exercises we carry out later.\(^4\)

A model that successfully accounts for the behavior of gross worker flows will necessarily account for behavior of the net flows and hence the three labor market stocks—employment (\(E\)), unemployment (\(U\)) and out of the labor force (\(N\)). Conversely, a model that cannot account for the behavior of the three labor market stocks (i.e., the net flows) must necessarily miss on some aspects of the gross flows. Since it is somewhat simpler to describe the behavior of the stocks, we will find it useful later on to examine the properties of both the stocks and the flows in the models that we consider. For this reason, Table 1 presents summary statistics from the data for the business cycle properties for the stocks and the flows. We use \(u\) to denote the unemployment rate, \(U/(E+U)\), \(lfpr\) to denote the labor force participation rate, \((E+U)/(E+U+N)\), and \(f_{ij}\) to denote the fraction of workers that move from state \(i\) in

\(^{3}\)In particular, see Blanchard and Diamond (1990), Fujita and Ramey (2009), Elsby, Hobijn, and Şahin (2012), and Shimer (2012).

\(^{4}\)Differences include the method used to identify cyclical components, the time period, as well as whether to report statistics for flows of workers as opposed to transition rates. For example, Blanchard and Diamond (1990) focus on the component of the time series that is accounted for by what they call “aggregate demand shocks”, whereas we focus on the cyclical component as identified using the HP filter. They consider the time period 1968–1986, whereas we consider 1968–2009. And we characterize transition rates whereas they characterize the level of flows. This last feature can make some properties appear different. For example, whereas the transition rate from \(U\) to \(E\) (which we denote as \(f_{UE}\)) is strongly procyclical, the fact that the size of the unemployment pool is also countercyclical implies that the level of the \(U\) to \(E\) flow is actually countercyclical.
the previous period to state \( j \) in the current period.\(^5\) The series are quarterly, produced by taking the quarterly average of monthly series, and all series are then logged and HP filtered. Further details regarding data sources and construction for labor market flows are provided in Appendix A.1.

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The patterns for the stocks are relatively well known. Employment is strongly procyclical, and the unemployment rate is strongly countercyclical. Although the labor force participation rate is procyclical, it is not as strongly cyclical as the other two series. The unemployment rate is the most volatile of the three series, and the labor force participation rate is the least volatile. All three series are highly autocorrelated.

Next we turn to the cyclical behavior of the gross flows, beginning with the flows between employment and unemployment. The flow rate \( f_{EU} \) is strongly countercyclical whereas the flow rate \( f_{UE} \) is strongly procyclical. Both are very persistent, and they exhibit roughly equal volatility.

More interesting for our purposes are the flows that involve non-participation. Although the stock of non-participants does not vary that much over the business cycle relative to the other two stocks, Table 1 shows that the flows between non-participation and the other states exhibit pronounced movements at business cycle frequencies. Specifically, whereas the fluctuations in the participation rate are an order of magnitude smaller than the fluctuations

\(^5\)We do not make any correction for time aggregation when reporting statistics for the flows. Our model will explicitly allow for some time aggregation, so the statistics in Table 1 will be the appropriate statistics to compare with the values generated by our model. We note, however, that applying time aggregation corrections do not change any of the qualitative patterns that we comment on below. Shimer (2011) examines these flows using data that are corrected for time aggregation but finds the same cyclical properties as we do. The analogous statistics for the series that are corrected for time aggregation are shown in Appendix A.2.
in the unemployment rate, the fluctuations in the transition rates into and out of non-participation are of roughly the same order of magnitude as those in the much-studied flows between \( E \) and \( U \). Looking only at the two flow rates into employment, \( f_{UE} \) and \( f_{NE} \), one would not be led to conclude that the participation rate plays only a minor role in accounting for employment fluctuations. The reason that the labor force participation rate does not move more over the cycle is because of the offsetting effect of an increased \( U \) to \( N \) transition rate during good times.

Consistent with the earlier work of Blanchard and Diamond (1990), the flows involving \( U \) and \( N \) are very different. In particular, whereas the flow rate from \( E \) into \( U \) is strongly countercyclical, the flow rate from \( E \) into \( N \) is weakly procyclical. And whereas the flow rate from \( N \) into \( E \) is procyclical, the flow rate from \( N \) into \( U \) is countercyclical. It is interesting to note at this stage that some of the cyclical properties revealed in Table 1 might reasonably be viewed as counterintuitive. For example, although the participation rate increases during good times, one of the flow rates out of participation, \( f_{EN} \), actually increases during good times. Similarly, although the participation rate decreases during bad times, one of the flow rates into participation, \( f_{NU} \), actually increases during bad times.

Lastly, Table 1 indicates that the flow rate from \( U \) into \( N \) is procyclical, implying that this flow rate decreases during recessions. This is contrary to an apparent piece of conventional wisdom that holds that unemployed workers are more likely to become discouraged during bad times. Note that this is not inconsistent with the fact that the stock of discouraged workers is higher during recessions: even with a constant flow rate between unemployment and discouragement, the fact that the stock of unemployment is higher in recessions will also imply that the stock of discouraged workers is also higher.

For future reference we note two results in the recent work by Elsby, Hobijn, and Şahin (2012). They go one step further than we do here by looking at, among other things, classification error and the role of worker attachment. First, they find that although classification
error is particularly relevant for the average level of the $U$ to $N$ flow, it is not of first order importance for its cyclical properties. Second, they find that the composition of the unemployment pool shifts towards “more attached” workers during recessions. This factor accounts for roughly one-half of the decline in the $U$ to $N$ transition rate during recessions. The most important dimension of attachment turns out to be prior employment status. This feature will be present in the quantitative model that we study. In fact, our relatively parsimonious model will deliver natural explanations for all of the patterns just documented.

3 Labor Supply and Gross Worker Flows

In this section we present a model of individual labor supply that generates individual transitions among the three labor market states, and then explain how it can be used to study aggregate gross worker flows.

3.1 A Model of Individual Labor Supply

Consider an individual with preferences given by:

$$E_t \sum_{t=0}^{\infty} \beta^t \left[ \log(c_t) - \alpha e_t \right]$$

where $c_t \geq 0$ is consumption in period $t$, $e_t \in \{0, 1\}$ is time devoted to work in period $t$, $0 < \beta < 1$ is the discount factor and $\alpha > 0$ is the disutility of work. A fundamental building block of our model is that an individual’s (net) return from work in the market is stochastic. In reality the relevant shocks could influence both the reward to market work and the opportunity cost of market work, but since it is ultimately the relative value of market work that matters, we consider only a single shock, which we model as an idiosyncratic shock to market productivity, $z_t$. We assume it follows an AR(1) process in logs:

$$\log z_{t+1} = \rho \log z_t + \varepsilon_{t+1}$$
where the innovation $\varepsilon_t$ is a mean zero normally distributed random variable with standard deviation $\sigma_{\varepsilon}$.$^6$

Much previous work on labor supply has assumed that the relevant market conditions that an individual faces are summarized by prices, most notably the wage rate ($w$) and the interest rate ($r$). A key innovation of our labor supply model is to expand the set of market conditions to also include two parameters, $\lambda$ and $\sigma$, that describe labor market frictions. We will refer to $\lambda$ as the employment opportunity arrival rate and to $\sigma$ as the employment separation rate. At this point we assume that market conditions are constant over time; when we consider business cycle fluctuations we will allow market conditions to fluctuate.

Events within a period unfold in the following way. If employed in period $t-1$, the individual loses the employment opportunity at the beginning of period $t$ with probability $\sigma$. Next, if the individual does not have an employment opportunity, he or she receives one with probability $\lambda$. At this point the individual makes decisions regarding labor supply and consumption, but can only choose $e_t$ equal to 1 if they have an employment opportunity. Given our timing assumption, if the individual suffers the $\sigma$ shock at the beginning of period $t$, he or she can still be employed in period $t$ if a new opportunity is received and they choose to work.

The market structure is standard in the incomplete markets literature. The individual cannot borrow and there are no markets for insuring idiosyncratic risk, but can accumulate an asset, whose level we denote by $a$. To capture the presence of various transfer programs that implicitly provide some insurance, we assume that there is a proportional tax $\tau$ on labor earnings and a lump sum transfer $T$. Combining these features, the individual’s period budget equation is given by:

$$c_t + a_{t+1} = (1 + r)a_t + (1 - \tau)wz_t e_t + T.$$  

$^6$Because $z$ is mean-reverting, some movements in the return to market work will be predictable whereas some will not. A richer model would include more detail, perhaps with part of the predictable component reflecting age effects, and with multiple random components that differ in persistence. Our approach here should be viewed as a parsimonious first step.
Note that $w$ is the wage per efficiency unit of labor services, and $wz$ is the observed wage rate for this individual.

We formulate the individual’s optimal decision problem recursively. The individual’s state consists of employment opportunity status at the time that the labor supply decision is made, asset holdings, and productivity. Let $W(a, z)$ be the maximum value conditional on working and $N(a, z)$ denote the maximum value conditional on not working. Define $V(a, s)$ by:

$$V(a, z) = \max\{W(a, z), N(a, z)\}.$$ 

The Bellman equations for $W$ and $N$ are given by:

$$W(a, z) = \max_{c \geq 0, a' \geq 0} \{\log(c) - \alpha + \beta E_{z'}[(1 - \sigma + \sigma \lambda w)V(a', z') + \sigma(1 - \lambda w)N(a', z')]\}$$  
$$s.t. \ c + a' = (1 + r)a + (1 - \tau)wz + T$$

and

$$N(k, z) = \max_{c \geq 0, a' \geq 0} \{\log(c) + \beta E_{z'}[\lambda wV(a', z') + (1 - \lambda w)N(a', z')]\}$$  
$$s.t. \ c + a' = (1 + r)a + T.$$ 

### 3.2 The Participation Margin in the Model

An important feature of our labor supply model is that frictions can prevent the individual from working in situations where he or she would like to, i.e., the individual can be “off” his or her labor supply curve in the sense that actual labor supply need not be the same as desired labor supply given market prices. This provides us with a method for distinguishing between the individual being unemployed versus not participating. We call the individual **unemployed** if he or she is not working but would have worked if presented with the opportunity (i.e., $e = 0$ and $W(a, z) > N(a, z)$). We call the individual **out of the labor force** if he or she is not working and would not have worked even if presented with the opportunity (i.e., $e = 0$ and $N(a, z) > W(a, z)$).
Official statistics divide non-employed workers into the categories of unemployed and out of the labor force based primarily on how they answer a question regarding active search in the previous four weeks. Although our model does not feature an active search decision, it can be mapped into this definition. Specifically, if active search is a discrete decision and the cost of search is very small, the decision to search effectively amounts to asking an individual if he or she would prefer working to not working.\(^7\)

Given this method for defining labor market states in the model, the individual will stochastically transit among the three states—employment, unemployment and non-participation. Idiosyncratic productivity and assets determine whether an individual would like to work given the opportunity, and frictions influence whether an individual who prefers to work will be employed or unemployed. As will become clearer later in the analysis, it is important to note that frictions directly impact optimal labor supply behavior in this model. That is, the extent of frictions influences whether an individual with a given level of assets and a given idiosyncratic productivity will desire to work, so that the labor supply decision is not separable with respect to the level of frictions.

Figure 1 shows a stylized version of the optimal decision rule for participation.

The participation decision is captured by an upward-sloping curve in \((a, z)\) space with the individual wanting to work, i.e., participating, for \((a, z)\) combinations that are below the line. Specifically, Figure 1 says that higher productivity and lower assets both make it more likely that an individual will participate, holding all else constant. The former effect represents a standard intertemporal substitution effect: holding all else constant the individual prefers to participate when the return to market work (relative to the opportunity cost of working) \(^7\)Given evidence from time use data on the amount of time devoted to search, we think it is reasonable to assume that the cost of active search is very small. In our earlier work we argued that a more natural way to connect the model to the data was to adopt a more inclusive definition of unemployment in the data, based on the desire to work rather than active search. Nonetheless, we found that the broader definition was not substantively important either in terms of the features in the data or the ability of the model to account for the data. We revert to the standard definition of unemployment in this paper because of the difficulty in getting a longer time series for flows between the states with the broader measure.
is high. The latter effect represents an income effect: holding all else constant, the greater the wealth that an individual has, the less likely it is that he or she will work. The earlier comment about frictions influencing optimal labor supply decisions amounts to saying that the position of the curve in Figure 1 is influenced by the two labor market frictions.

3.3 Using the Model to Address Aggregate Gross Worker Flows

To this point we have considered the situation of an individual worker and described how this individual will transition between the three labor market states. A natural way to use this model to examine its implications for aggregate gross worker flows is to assume that there are a large number of workers, each of whom is just like the individual we described above, with all of the shocks being idiosyncratic. Given a set of market conditions (i.e., prices and frictions), we could then look for a stationary distribution of individuals. In this stationary distribution there would be an invariant distribution of individuals over the individual states: assets, idiosyncratic productivity and whether employed last period, and hence an invariant distribution of individuals over the three labor market states of employment, unemployment and out of the labor force.

In this economy, all individuals have the same decision rules, so the participation boundary in Figure 1 would be the same for all individuals. Given a participation boundary
and the invariant distribution over pairs \((a, z)\), we can determine the participation rate by integrating the distribution above the boundary. Gross flows between participation and non-participation occur when individuals transit across the boundary. Loosely speaking, holding market conditions and the stochastic process for idiosyncratic shocks fixed, these flows will depend on how much mass is near the boundary. Additionally, for those individuals who are above the boundary and hence are participating, their distribution between employment and unemployment will influence the magnitude of the flows between these two states and non-participation.

A key exercise that we carry out in this paper is to examine how fluctuations in market conditions influence fluctuations in gross worker flows, specifically those that involve flows between participation and non-participation. Figure 1 offers a useful framework for organizing one’s thinking about this issue. For simplicity, consider a permanent one time change in market conditions. The figure suggests that there will be two distinct effects on flows between participation and non-participation. First, and as noted previously, a one-time change in market conditions will lead to a one-time movement in the participation boundary. This will necessarily lead some individuals to change their participation status, even holding their individual state constant. But note that this effect is only present in the period of the change in market conditions. The second effect has to do with the changes in the mass of individuals who are near the boundary, and in particular, how those individuals who are located just above the boundary are distributed between \(E\) and \(U\). Unlike the first effect, which was a one-time change in flows, this effect will be persistent. Additionally, this effect will have a dynamic component, since the how individuals just above the boundary are distributed between \(E\) and \(U\) will also have some dynamics. For example, suppose that the participation region expands. At the time of the change, all of those individuals who were just below the original participation boundary will necessarily become participants, and a fraction of them will enter unemployment since they will not find a job immediately. But as time passes, the
dynamics of job finding, job loss and idiosyncratic shocks will lead to a stationary distribution for these individuals in which a smaller fraction of them are unemployed. Intuitively, in the immediate aftermath of this change in market conditions, the majority of individuals who are participating but close to the boundary will be unemployed. We will refer to this feature later on in the paper.

4 Fluctuations in Gross Worker Flows

Our main goal is to examine the extent to which our labor supply model of gross worker flows can match the properties of fluctuations in gross worker flows exhibited in Table 1 when subjected to empirically reasonable shocks to “aggregate market conditions”, by which we mean prices and frictions. We emphasize that our goal here is not to find a full general-equilibrium model of what explains the variation in market conditions—what makes wages higher some times than other times and jobs easier to find some times than other times. This would necessitate taking a stand on the relative importance of different mechanisms in the aggregate economy and those mechanisms are not our priority here. Rather, we seek parsimonious representations of market conditions that influence households systematically in their labor supply decisions. In this section we describe the method that we use to achieve this goal.

4.1 Modeling Shocks to Market Conditions

There are a few different ways that we could proceed. One strategy would be to estimate the model using some type of simulated moments estimator on time series data. We instead adopt a much simpler and more transparent approach that we think offers some important insights into the role that different driving forces play in shaping the cyclical properties of gross worker flows. Specifically, given that our focus is on business cycle fluctuations and that a key feature of business cycles is comovement among series, we effectively focus on perfectly correlated movements in market conditions that reflect business cycle movements. We ask
whether such movements can account for business cycle fluctuations in gross worker flows if the relative variances of the movements in each variable are set to empirically reasonable values. Intuitively, we want to consider shocks to labor demand that manifest themselves in fluctuations in prices and frictions.

The simplest implementation of this method would posit a latent aggregate state $s$ that follows a Markov process, with prices and frictions all being functions of this latent aggregate state $s$. Relative to this specification we introduce one additional element, described below, that serves to discipline the joint movements in $w$ and $r$.

We impose this discipline by introducing a particular form of general equilibrium conditions. Specifically, we posit an aggregate production function

$$Y_t = Z_t K_t^{\theta} L_t^{1-\theta},$$

where $\theta \in (0, 1)$, $K_t = \int k_{it}di$ is aggregate input of capital services (which is the sum of the workers’ assets), and $L_t = \int e_{it}z_{it}di$ is aggregate input of labor services (which is the sum of the employed workers’ efficiency unit of labor). Here, we model the latent aggregate state as a TFP shock ($Z$) to the aggregate production function, and impose that changes in $w$ and $r$ are mutually consistent with changes in factor inputs under the assumption that factor prices are equal to marginal products. Consistent with the approach described above, we assume that the two frictional parameters are functions of the underlying latent aggregate state $Z$.

We emphasize that we do not interpret the TFP shock in a literal sense; rather it is simply a vehicle to generate fluctuations in prices and impose some discipline on joint movements in $w$ and $r$. As we will see later, we will calibrate the model so as to match fluctuations in wages rather than fluctuations in TFP. In this sense we are not imposing that wage movements in the data reflect market clearing wages given observed movements in TFP.

We describe the

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8 More generally, one might consider a specification in which the innovations are perfectly correlated but in which the individual components display different degrees of persistence.

9 As we will see later, we will calibrate the model so as to match fluctuations in wages rather than fluctuations in TFP. In this sense we are not imposing that wage movements in the data reflect market clearing wages given observed movements in TFP.

10 Our procedure introduces some feedback from frictions to prices to the extent that frictions affect quantities. It turns out that these effects are minimal, so that our more sophisticated analysis is likely very close.
implementation of this procedure in more detail in the Appendix A.4.

4.2 Calibrating the Stationary Distribution

In this section we calibrate the parameters of our model so that the stationary distribution that results with constant market conditions generates flows of workers across labor market states that match the average levels of gross worker flows in the data. Since this procedure draws heavily on the one outlined in Krusell et al. (2011), we just sketch it here.

The model has ten parameters that need to be assigned: preference parameters $\beta$ and $\alpha$, idiosyncratic shock parameters $\rho_z$ and $\sigma_\varepsilon$, frictional parameters $\sigma$ and $\lambda$, the tax rate $\tau$, the transfer $T$, and prices $r$ and $w$. Because data on labor market transitions are available monthly, we set the length of a period to be one month.

Three parameters-- $\tau$, $\rho_z$, and $\sigma_\varepsilon$--can be set without solving the model. Consistent with various studies, we set $\tau = .30$.\textsuperscript{11} Recall that our idiosyncratic shock process should be viewed as a composite of all idiosyncratic shocks that affect the static return to working versus not working. Shocks to wages are of course only one such component. However, since these are the shocks for which we have the best measures, our benchmark specification calibrates the shock process to estimates of idiosyncratic wage shocks. Specifically, we choose values for $\rho_z$ and $\sigma_\varepsilon$ based on Floden and Linde (2001), who estimated $\rho_z = .92$ and $\sigma_\varepsilon = .21$ expressed on an annual basis.\textsuperscript{12}

The remaining parameters are chosen so that the steady state equilibrium matches specific targets. Given values for the two frictional parameters, $\lambda$ and $\sigma$, the other parameters are chosen in a standard fashion. Given other parameter values (including $r$), the value

\footnotesize
\textsuperscript{11} Following the work of Mendoza, Razin, and Tesar (1994) there are several papers which produce estimates of the average effective tax rate on labor income across countries. Minor variations in methods across these studies produce small differences in the estimates, but .30 is representative of these estimates.

\textsuperscript{12} Krusell et al. (2011) showed that the ability of the model to account for the flows between states remains relatively unchanged over a wide range of values of $\rho$ and $\sigma_\varepsilon$. What mattered most was that $\rho$ was reasonably persistent (at least .5), but not too close to being a unit root (say less than .97), and that $\sigma_\varepsilon$ was not too small.

of the discount factor $\beta$ will influence the level of average asset holdings in the stationary distribution. We first set $r$ so that the annual rate of return on assets is 4%. Then we choose $\beta$ so that the amount of capital accumulated in steady state would be consistent with an annual return of 4% assuming the production function (1).\textsuperscript{13} The production function also pins down the value of $w$ from the marginal product of labor. We set $T$ to be consistent with a balanced budget in the stationary distribution, that is, $T_t = \int \tau w_t e_{it} z_{it} di$.\textsuperscript{14} The preference parameter $\alpha$, which captures the disutility of working, is set so that the employment to population ratio in the stationary distribution is equal to .61. This is the value of the employment to population ratio for the population aged 16 and older for the period 1968–2009.\textsuperscript{15}

It remains to choose values for $\lambda$ and $\sigma$. There is an intimate connection between $\lambda$ and the unemployment rate in the model. If $\lambda = 1$ then unemployment will be zero, since everyone always has the opportunity to work. We therefore choose $\lambda$ so that the steady state unemployment rate matches the average value for the unemployment rate in the U.S. data for the period 1968–2009, which is .061. We choose $\sigma$ to target the average flow rate out of employment over our sample period, which is 3.6%. We target this rate based on our belief that the employment state is the one subject to the least amount of measurement error.

Table 2 summarizes the calibrated values and the various targets used in the calibration.

<table>
<thead>
<tr>
<th>Table 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Calibration Targets</td>
</tr>
<tr>
<td>$\frac{E}{P} = .610$, $\frac{U}{E+U} = .061$, $1 + r = 1.04^{1/12}$, $E \rightarrow E = .964$</td>
</tr>
<tr>
<td>Parameter Values</td>
</tr>
<tr>
<td>$\beta$, $\alpha$, $\rho_\epsilon$, $\sigma_\epsilon$, $\lambda$, $\sigma$, $\tau$</td>
</tr>
<tr>
<td>.9967, .61, .9931, .1017, .44, .013, .30</td>
</tr>
</tbody>
</table>

The labor market flows in our calibrated model and the data are displayed in Table 3.

\textsuperscript{13}Specifically, we calculate this from (1) with capital share $\theta$ equal to .3 and a monthly depreciation rate of .0067.

\textsuperscript{14}Following the work of Mendoza, Razin, and Tesar (1994) there are several papers which produce estimates of the average effective tax rate on labor income across countries. Minor variations in methods across these studies produce small differences in the estimates, but .30 is representative of these estimates.

\textsuperscript{15}We calibrate to values for the period 1968–2009 because this is the period for which we have consistent measures of labor market flows.
Overall the model does a reasonable job of capturing the salient features of the data. Specifically, it does a good job of capturing the degree of persistence in each of the three states. The one major discrepancy is that the model does not generate enough flows from $U$ to $N$. Given our strategy of targeting the stock of workers in $U$, this necessarily implies that the other flow out of $U$ (i.e., the flow from $U$ to $E$) must also be off. It has long been known that classification errors lead to spurious flows, especially between unemployment and not in the labor force (see, e.g., Abowd and Zellner (1985) and Poterba and Summers (1986)). The survey that Abowd and Zellner and Poterba and Summers used to estimate the extent of classification error on transition rates was discontinued shortly thereafter, so one cannot use their procedure to produce an adjusted time series. More recently, Elsby, Hobijn, and Şahin (2012) devise another procedure for purging the data of spurious flows that one can carry out over a longer time period. They estimate that the average “true” transition rate from $U$ to $N$ is $0.14$ for the 1968-2009 period. In Appendix A.2 we show that with an empirically plausible amount of measurement error the model does a much better job of matching the flows between $U$ and $N$. While classification error is important in matching the average behavior of flows in the data, we also show in Appendix A.2 that it is not important for our key findings about business cycle fluctuations. And as noted previously, the work by Elsby, Hobijn, and Şahin (2012) shows that classification error does not have an important impact on cyclical properties.

<table>
<thead>
<tr>
<th>FROM</th>
<th>TO</th>
<th>FROM</th>
<th>TO</th>
</tr>
</thead>
<tbody>
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<td>E</td>
<td>E</td>
<td>0.954</td>
<td>0.954</td>
</tr>
<tr>
<td>E</td>
<td>U</td>
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<tr>
<td>E</td>
<td>N</td>
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<td>U</td>
<td>E</td>
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<tr>
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<td>U</td>
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<td>0.505</td>
</tr>
<tr>
<td>U</td>
<td>N</td>
<td>0.222</td>
<td>0.099</td>
</tr>
<tr>
<td>N</td>
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<td>N</td>
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<tr>
<td>N</td>
<td>N</td>
<td>0.925</td>
<td>0.921</td>
</tr>
</tbody>
</table>
4.3 Calibrating Shocks to Market Conditions

In this subsection we describe how we calibrate the stochastic process for fluctuations in market conditions. As is standard in the business cycle literature with heterogeneous agents, we assume that the shocks to market conditions follow a two state Markov process. We will refer to one state as the “good” state and the other state as the “bad” state. The good state will have a high value of $Z$ (and hence also for $w$ and $r$), a high value for the employment arrival rate $\lambda$, and a low value for the employment separation rate $\sigma$. We denote the two possible realizations for the market conditions shock as $(Z^G, \lambda^G, \sigma^G)$ and $(Z^B, \lambda^B, \sigma^B)$. We parameterize the TFP shock as $Z^G = 1 + \varepsilon^Z$, and $Z^B = 1 - \varepsilon^Z$, and the other two shocks as $\lambda^G = \lambda^* + \varepsilon^\lambda$, $\lambda^B = \lambda^* - \varepsilon^\lambda$, $\sigma^G = \sigma^* - \varepsilon^\sigma$, $\sigma^B = \sigma^* + \varepsilon^\sigma$, where $\lambda^*$ and $\sigma^*$ are the values for the model calibrated to match average transition rates. We assume that the transition matrix for the Markov process is symmetric, with diagonal element denoted by $\rho$.

In our model, both the level and fluctuations in $f_{UE}$ closely mimic the level and fluctuations in $\lambda$. For this reason we choose the value of $\varepsilon^\lambda$ so that the fluctuations in $f_{UE}$ in the simulated model match the standard deviation of the fluctuations in $f_{UE}$ found in US data. This leads to $\varepsilon^\lambda = .069$. Controlling for $\lambda$, which influences the impact of time aggregation on measured $f_{EU}$, the level and fluctuations in $f_{EU}$ closely follow the level and fluctuations in $\sigma$, so we choose $\varepsilon^\sigma = .00051$ so as to match the fluctuations in $f_{EU}$.

We choose the value of $\varepsilon^Z$ so as to target the volatility of wages. While market conditions are defined by the value of $w$, the wage per efficiency unit of labor services, this is not directly observable in the data. Instead, what we observe in the data is the average value of the wage payment per unit of time, which we will refer to as $\bar{w}$. In our model this is given by the ratio of total wage payments to the level of employment and is the concept of wages that we target in our calibration.

There are two commonly used alternative measures of wages in macro studies. The first measure is the average hourly earnings of production and nonsupervisory employees in
the private sector and is based on the establishment survey. The second measure is real compensation per hour in the nonfarm business sector, based on the productivity and costs releases.\footnote{For example, Gertler and Trigari (2009) use the first measure while Galí (2011) use the second one. Galí (2011) shows that these two measures have different implications for wage inflation.} To obtain a reasonable range of values for the volatility of wages, we calculate the volatility of wages for the 1964-2009 period using each of these two measures. When we use the first measure we deflate the average hourly earnings using both the consumer price index (CPI) and the GDP deflator, which also matters. We find that the standard deviation of average hourly wages is 0.0115 when deflated with the CPI and 0.0074 when deflated with the GDP deflator. When we use the real compensation measure, the volatility of wages turns out to be 0.0097. These calculations give us a range of 0.0074-0.0115 and we choose 0.0096, which is in the middle of this range and is consistent with the compensation based measure. It turns out that this value will lead to fluctuations in employment in the model of the same magnitude as those found in the data. This requires $\varepsilon^Z = .0287$.

In our model we can clearly distinguish between fluctuations in $w$ and $\bar{w}$. A sizable literature (see, e.g., Bils (1985), Keane, Moffitt, and Runkle (1988) and Solon, Barsky, and Parker (1994)) has argued that cyclical fluctuations in $\bar{w}$ are significantly less than fluctuations in $w$ due to cyclical changes in the composition of the employment pool. We report the details later, but note here that in our benchmark model the size of the negative composition bias is substantial.

## 5 Results in the Benchmark Model

In this section we report the results of our study. We begin by examining the ability of the model to account for cyclical movements in stocks, and then move on to examine cyclical movements in gross worker flows.
5.1 Cyclical Properties of Stocks

We begin by assessing the ability of the model to match the cyclical movements in the three labor market stock variables—employment, the unemployment rate and the participation rate. Table 4 shows the results for the benchmark model and the data. For the model, the output $Y$ is calculated from (1).

<table>
<thead>
<tr>
<th>Volatilities</th>
<th>Correlations</th>
<th>Autocorrelations</th>
</tr>
</thead>
<tbody>
<tr>
<td>$std(x)$</td>
<td>$corr(x, Y)$</td>
<td>$corr(x, x_{-1})$</td>
</tr>
<tr>
<td>$u$</td>
<td>$lfpr$</td>
<td>$E$</td>
</tr>
<tr>
<td>Data</td>
<td>.12</td>
<td>.003</td>
</tr>
<tr>
<td>Model</td>
<td>.13</td>
<td>.004</td>
</tr>
<tr>
<td></td>
<td>$.92</td>
<td>.72</td>
</tr>
<tr>
<td></td>
<td>.84</td>
<td>.68</td>
</tr>
</tbody>
</table>

As noted earlier, the value of wage fluctuations that we targeted in our benchmark specification turns out to generate exactly the same fluctuations in employment as found in the data. However, it is noteworthy that the model also does a good job of accounting for the size of fluctuations in both unemployment and participation. Moreover, it also correctly accounts for the fact that employment is strongly procyclical, the unemployment rate is strongly countercyclical, and the labor force participation rate is weakly procyclical. While the model slightly understates the persistence in unemployment and employment, it does accurately predict that the participation rate is less persistent than than the other two stocks.

To understand the economic forces underlying these movements in labor market stocks, it is instructive to separately consider the role of shocks to prices versus frictions. To consider the case of shocks to only prices we set $\varepsilon^\lambda = \varepsilon^\sigma = 0$, and to consider the case of shocks to frictions only we set $\varepsilon^Z = 0$. Table 5 presents results.

---

17 As noted earlier, even in the job availability shocks only case, our method will allow for changes in prices induced by changes in factor inputs. It turns out that these effects are very small, so that this case effectively corresponds to a case in which prices are constant.
The striking finding in Table 5 is that neither price nor friction shocks alone are capable of reproducing the key cyclical features found in the data. Specifically, with friction shocks only we see that participation not only fluctuates too much but is also strongly countercyclical instead of weakly procyclical. Although this specification does a good job of matching fluctuations in the unemployment rate, employment fluctuations are very small relative to their value in the data. In contrast, with price shocks only, participation is procyclical but fluctuates too much relative to the other series. And although employment fluctuates the same as in the data, unemployment hardly fluctuates at all.

We conclude that in the context of our model of labor supply, both price and friction shocks are essential in accounting for the patterns found in the data. This finding has important implications for the mechanisms that can drive labor market fluctuations over the business cycle in a general equilibrium setting. For example, the fact that models in the spirit of Mortensen and Pissarides featuring TFP or some other supply shocks but with perfectly rigid wages will not capture the behavior of the three labor market stocks when extended to allow for labor supply with wealth effects. Previous researchers such as Hall (2005) and Shimer (2005) had argued that this class of models offered a good account of labor market dynamics in the context of a model in which participation is fixed exogenously. Although participation does not fluctuate too much over the cycle in the data, our analysis shows that exogenously shutting down this margin is far from innocuous.

As a first step in exploring the underlying economic mechanism behind this result, consider how the participation region adjusts as friction parameters change from their level in
the bad aggregate state to their level in the good aggregate state. Figure 2 illustrates this for the friction shocks only case by plotting the participation boundary for the two different realizations of the friction shocks evaluated at the mean level of the other individual states.

Figure 2: Cut-off wealth and productivity levels for the model with friction shocks only

![Figure 2](image)

The important message from Figure 2 is that when frictions worsen, thereby making it more difficult to have an employment opportunity, individuals respond by expanding the set of individual states in which they desire to work.\(^{18}\) This manifests itself in two ways: individuals who are employed will be less likely to move out of employment in response to idiosyncratic shocks (or asset accumulation), and some individuals who are not employed will decide to accept employment opportunities under conditions that they previously would not.

This effect is intuitive. A key desire for individuals in this economy is to arrange the timing of work to coincide with periods of high individual productivity. Frictions interfere with an individual’s ability to achieve the desired timing. \(^{18}\) When frictions become more severe, individuals respond by expanding the set of conditions under which they will work if...

\(^{18}\)In Krusell et al. (2010) we demonstrated that this effect was quantitatively important in terms of steady state outcomes. Here we see that the effect is quantitatively significant in a business cycle context as well.
given the opportunity, i.e., by becoming less choosy about when they work. The implication is that participation will be countercyclical in the presence of only shocks to frictions. While the magnitude of this effect will depend on the density of individuals around the boundary of the two regions, Figure 2 illustrates the main economic mechanism at work. It is important to emphasize that this effect depends critically on the size of income and substitution effects in labor supply. In particular, assuming linear utility and hence no income effects will underestimate the desire of individuals to work more in response to changes that lower income.

The second class of business cycle models that the results in Table 5 cast doubt on are those implicit in standard real business cycle models. Standard real business cycle models such as Hansen (1985) contain no frictions and do not allow one to separate the non-employed into the unemployed and non-participants. Our model does permit this, but the price shocks only row in Table 5 shows that if job availability is constant over the business cycle, then the model does not deliver sufficient movement in unemployment. One recurring critique of real business cycle models has been that they do not account for unemployment, and our analysis supports this critique. To understand the underlying economics, it is again instructive to examine how decision rules and flows are affected by price shocks when frictions are held constant. Figure 3 plots the behavior of the decision rule for participation that is equivalent to Figure 2.

This figure illustrates the standard intertemporal substitution effects present in standard real business cycle models: when wages are high individuals choose to work more, which corresponds to expanding the set of individual states in which they desire to work. This is the effect that leads to procyclical employment and participation. To the extent that the employment responses reflect standard intertemporal substitution, it may seem curious that this specification is able to generate countercyclical fluctuations in unemployment. We return to this issue later when we discuss our results in relation to those in Veracierto (2008).
5.2 Cyclical Properties of Gross Flows

It is reassuring that our parsimonious labor supply model of gross worker flows can account for the cyclical properties of labor market stocks given empirically reasonable shocks to market conditions. This outcome is not at all a foregone conclusion and relies on the subtle yet intuitive economic mechanisms that we outlined in the last subsection. However, our model was constructed to study gross flows, and the success in generating empirically reasonable movements in the stocks will not be particularly relevant if the underlying gross flows behave counterfactually. We therefore now ask whether the model can also account for the cyclical behavior of gross worker flows. In interpreting our results we will again stress the underlying mechanisms in detail in order to understand the economics behind the model’s predictions.

Table 6 shows the results for the cyclical properties of flow rates in our benchmark model. For ease of comparison, we also repeat the properties of the data that were previously reported in Table 1.
Table 6

Gross Worker Flows in the Benchmark Model

A. Data

<table>
<thead>
<tr>
<th></th>
<th>$f_{EU}$</th>
<th>$f_{EN}$</th>
<th>$f_{UE}$</th>
<th>$f_{UN}$</th>
<th>$f_{NE}$</th>
<th>$f_{NU}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\text{std}(x)$</td>
<td>.085</td>
<td>.032</td>
<td>.077</td>
<td>.060</td>
<td>.043</td>
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<td>$\text{corr}(x, Y)$</td>
<td>-.82</td>
<td>.33</td>
<td>.78</td>
<td>.78</td>
<td>.64</td>
<td>-.70</td>
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<tr>
<td>$\text{corr}(x, x_{-1})$</td>
<td>.73</td>
<td>.20</td>
<td>.84</td>
<td>.73</td>
<td>.41</td>
<td>.75</td>
</tr>
</tbody>
</table>

B. Model

<table>
<thead>
<tr>
<th></th>
<th>$f_{EU}$</th>
<th>$f_{EN}$</th>
<th>$f_{UE}$</th>
<th>$f_{UN}$</th>
<th>$f_{NE}$</th>
<th>$f_{NU}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\text{std}(x)$</td>
<td>.085</td>
<td>.031</td>
<td>.077</td>
<td>.051</td>
<td>.080</td>
<td>.066</td>
</tr>
<tr>
<td>$\text{corr}(x, Y)$</td>
<td>-.90</td>
<td>.35</td>
<td>.92</td>
<td>.56</td>
<td>.89</td>
<td>-.92</td>
</tr>
<tr>
<td>$\text{corr}(x, x_{-1})$</td>
<td>.68</td>
<td>.09</td>
<td>.72</td>
<td>.30</td>
<td>.70</td>
<td>.68</td>
</tr>
</tbody>
</table>

This table shows that the model does quite a good job of accounting for the key patterns. It captures the countercyclicality of unemployment inflows ($EU$ and $NU$ flow rates), the procyclicality of unemployment outflows ($UE$ and $NU$ flow rates) and the mild procyclicality of the $EN$ flow rate. The model delivers a volatility and correlation (with output) for $f_{NE}$ that are somewhat too high. We discuss this shortcoming in more detail below.

To examine the economics behind the cyclicality of the gross flows it is instructive to focus on the transition dynamics in the various flows when the economy has been in one aggregate state for many periods and then receives a realization of the other aggregate shock that persists for many periods. Figure 4 shows the responses of the transition rates as the economy moves from bad times to good times in this fashion.

5.2.1 Understanding the Flows between $E$ and $U$

We begin with the flows between $E$ and $U$, which are the simplest to understand. To move from $U$ to $E$ across adjacent periods requires that two things happen: the individual must receive a work opportunity (which happens with probability $\lambda$) and not suffer an idiosyncratic shock that changes their desire to work. The change in the probability of the second event as we move from bad to good market conditions is of second order importance. So the dominant effect is the increase in $\lambda$, implying an increase in the transition rate from $U$ to $E$. Note that this change persists as long as the good aggregate state persists.
To move from $E$ to $U$ across adjacent periods, three things must happen: a worker must suffer a separation, not receive a new employment opportunity, and not suffer an idiosyncratic shock that changes their desire to work. Again, the change in the probability of the third event is of second order importance. The probability of the first two events is $\sigma(1-\lambda)$, which is clearly lower in the good state, implying a decrease in the $E$ to $U$ flow rate. Again, this change persists as long as the economy stays in the good state.

In this context, and as a side issue, it is interesting to assess the relative importance of the changes in $\sigma$ and $\lambda$ on the observed change in the flows between $E$ and $U$. To do this we simulate the model with shocks to only one friction at a time and compute summary statistics for the gross flows. The results are in Table 7.

<table>
<thead>
<tr>
<th>Table 7</th>
<th>Contribution of the Shocks: Flows</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
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<td>$f_{EU}$</td>
<td>$f_{UE}$</td>
</tr>
<tr>
<td>Data</td>
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<tr>
<td>All Shocks</td>
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</tr>
<tr>
<td>$\lambda$ shock</td>
<td>.069</td>
</tr>
<tr>
<td>$\sigma$ shock</td>
<td>.033</td>
</tr>
</tbody>
</table>
The interesting result here is that even when there are only shocks to $\lambda$, so that $\sigma$ is constant, the model accounts for roughly 80% of the volatility in $f_{EU}$. This reflects the time aggregation that is implicit in our model: when $\lambda$ is low it is more likely that a worker who experiences an employment separation will remain in the unemployment state. Note that in the specification with only shocks to $\sigma$ there is also an effect on the transition rate from $U$ to $E$. This may at first seem somewhat surprising. However, this effect is due to a one-time effect associated with changes in the value of $\sigma$. The nature of the effect is that during good times (i.e., when $\sigma$ decreases), some people move from participation to non-participation due to the fact that as it becomes easier to work when one desires, one becomes more particular about timing periods of work with high values of the idiosyncratic shocks. As a result, during the period in which $\sigma$ changes from high to low, some of the previously unemployed move to non-participation and hence even though they receive employment opportunities they choose not to work. This causes a one-time reduction in $f_{UE}$. The fact that it is a one-time reduction is evident in the very low correlation between $f_{UE}$ and output in the case of shocks only to $\sigma$.

5.2.2 Understanding the Flows between $E$ and $N$

Returning to the transition dynamics in Figure 4, we next consider the change in the transition rate from $N$ to $E$. Note that there is a persistent increase in this flow, but that the increase in the initial period of the shock is even larger than the persistent effect. The persistent increase is due to the change in frictions. To move from $N$ to $E$ two things must happen: the individual must experience a change in their idiosyncratic shock that makes them want to work, and they must also receive an employment opportunity. Once again, the change in the probability of receiving an offer is the dominant effect, so that when $\lambda$ increases, so does the probability of transiting from $N$ to $E$. To understand why the initial

\footnote{As explained in the theoretical section above, there are also predictable movements over time across the boundary due to asset accumulation (in $E$) or decumulation (in $N$), as well as a drift in $z$ toward its mean. These are both small quantitatively and so we do not focus on them in this discussion.}
effect is significantly larger, note that when market conditions change to the good state, the participation region for individual workers expands. Hence, in the initial period the pool of potential workers who transition from $N$ to $E$ includes not only those who transit across the boundary between the participation and non-participation region, but also those who enter the participation region because of the change in the position of the boundary. Because the effect of the change in the boundary only occurs in the initial period of the change, this causes an initial spike in the $N$ to $E$ flow.

Next we consider the movement from $E$ to $N$. Note that the persistent effect is positive whereas the immediate effect is negative. To understand why the immediate and persistent effects are of different sign it is important to isolate the two separate effects that we noted earlier: the effect due to the one-time change in the participation boundary versus the persistent and dynamic effect associated with the changing mass of employed individuals who are close to the participation boundary. In the stationary distribution, with a fixed decision rule defining the boundary between the participation region and the non-participation region, the flow from $E$ to $N$ occurs when an employed individual crosses the boundary. The flow is therefore determined by the mass of employed individuals that are close to the boundary. When the economy is hit with a positive shock to market conditions, the participation region expands, thereby making it less likely that an employed individual who is initially near the older boundary will actually exit the participation region.

The second effect has to do with changes in the mass of employed individuals who are near the boundary. As noted earlier, this effect will have a dynamic component since the distribution of employed individuals “fills in” the area between the two boundaries over time. The long run effect is purely determined by the movement of employed individuals across the boundary in the new stationary distribution. In good times, it turns out that there are relatively more marginal workers in the employment pool, and these workers are more likely to experience a transition to out of the labor force. In order to illustrate this point, we draw
Figures 5 to 7 that describe the distribution of workers, in terms of the distance from the participation boundary, in both the good and the bad aggregate state.

Figure 5: The distribution of “distance to indifference”: $E$ workers

In the model, a worker’s situation is described as a point in $(a, z)$ space. In order to describe the distribution of workers’ distance from the participation boundary in a one-dimensional metric, we measure the distance in terms of “$z$-equivalence”. In particular, we ask each worker (worker $i$ at time $t$) a question: “by how much would your value of $\ln(z_{it})$ have to decrease to make you indifferent between participating and not participating?” That is, we calculate $\ln(z_{it}) - \ln(z^*_t(a_{it}))$, where $z^*_t(a)$ is the level of $z$ that makes a worker with assets $a$ indifferent at time $t$ between participating and not participating. Then we count the fraction of workers whose $\ln(z_{it}) - \ln(z^*_t(a_{it}))$ falls into each bin.

Each of Figures 5 through 7 has two histograms: one for the good aggregate state and one for the bad aggregate state.\textsuperscript{20} Looking at the $E$ pool (Figure 5), we see that there are

\textsuperscript{20}In order to focus on the “long-run” effect, both histograms for the good state correspond to the situation after being in the good state for 80 periods. Minor adjustments are made in the figure in order to correct for
Figure 6: The distribution of “distance to indifference”: $U$ workers

Figure 7: The distribution of “distance to indifference”: $N$ workers

numerical approximation errors.
more marginal workers—workers with a short distance to the boundary—in good times than in bad times. The reason why there are more marginal workers in good times is the change in job frictions. If the employment opportunity arrival rate is relatively high, then new hires will be a greater fraction of all employment.\textsuperscript{21} New hires in our model are disproportionately composed of individuals who are close to the boundary, that is, individuals who previously did not want to work but received an idiosyncratic shock that pushed them over the boundary. Because individuals who are close to the boundary are more likely to receive a new realization that causes them to cross the boundary, the result is that we now have greater flows from $E$ to $N$.

5.2.3 Understanding the Flows between $N$ and $U$

Lastly, we consider the flows between $N$ and $U$. First, note that the change in the flow from $N$ to $U$ is basically the mirror image of the change in the $N$ to $E$ flow, since this reflects the case in which an individual changes their desire to work but does not receive a work opportunity. As the change in the first effect is of second order importance, the second effect dominates, and persists as long as the good state persists.

As for the flow from $U$ to $N$, the reasoning is similar to that for the $E$ to $N$ flow. In particular, the immediate effect is a decrease due to the expansion in the size of the participation region. The persistent effect is again positive for reasons involving the composition of the unemployment pool. Referring back to Figure 6, we see that there are more marginal workers in good times. Specifically, since in the good state unemployed workers exit to employment more quickly, the pool of unemployed individuals is relatively more dominated by individuals who have just entered unemployment. Since employed workers are less likely to enter unemployment in good times, new entrants to unemployment are dominated by individuals that transition from $N$ to $U$. But these individuals are more likely to be close to the boundary,

\textsuperscript{21}The decrease in the value of $\sigma$ creates the opposite effect, but consistent with results presented earlier, the effects of changes in $\lambda$ are quantitatively more important.
making them more susceptible to a transition that puts them back in the $N$ state. The reason that the persistent effect is relatively larger in this case than in the case of the $E$ to $N$ flow has to do with the fact that the persistence in the unemployment state is much lower than the persistence in the employment state, so that the composition effects are relatively more important. This model feature is consistent with Elsby, Hobijn, and Şahin (2012), who show that the composition of the unemployed pool shifts towards more “attached” workers during recessions, where the most important dimension of attachment is prior employment status. They show that this mechanism accounts for one-half to two-thirds of the decline in the $U$ to $N$ flow rate during recessions.

We noted earlier that the volatility of $f_{NE}$ in the model is significantly larger than it is in the data, and that its correlation with output is also somewhat high relative to the data. Looking at Figure 4, it is apparent that one of the sources of the large volatility is the large jump in $f_{NE}$ that occurs immediately upon impact of the new realization of market conditions. While we do not pursue this idea here, it is perhaps reasonable to think that this movement of individuals from out of the labor force into employment may be spread over a slightly longer period. If this were the case, then the standard deviation would presumably drop considerably. This would also diminish somewhat the correlation between $f_{NE}$ and output.

5.2.4 Summary

The above discussion has focused on describing the intuition for the qualitative patterns found in Figure 4. These qualitative patterns can in turn be easily connected with the correlations that we see in Table 6. We conclude that the economics implicit in the model that is responsible for these patterns is quite straightforward, and for this reason we think the results are a robust feature of our relatively parsimonious labor supply model of worker flows. Of course, the extent to which the model can reproduce the quantitative features of fluctuations in gross flows depends not only on the qualitative patterns but also the
quantitative magnitudes of the various effects. It is reasonable to think that a key factor for the quantitative results is the mass of individuals that are near the participation boundary. In this regard, the discipline in our quantitative work derives from the fact that our steady state model is consistent with the average level of gross flows. In this sense, our model captures the amount of workers that are close to the boundary. Also, it is important to emphasize that the quantitative movements in the participation boundary are very much influenced by the presence of wealth effects on labor supply.

5.3 Fluctuations in Wages and Composition

When we discussed calibrating shocks to wages we noted that there were several different notions of wages that were of interest and that had received attention in the literature. Here we report the properties of different wage measures. Results are reported in Table 8.

<table>
<thead>
<tr>
<th>Behavior of Wages</th>
<th>Volatility: std(x)/std(Y)</th>
<th>Correlation: corrcosf(x, Y)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>w</td>
<td>w̄</td>
</tr>
<tr>
<td>Benchmark</td>
<td>.63</td>
<td>.49</td>
</tr>
</tbody>
</table>

As noted earlier, in our benchmark model, the standard deviation of the average wage relative to output is .49. Table 8 shows that this is roughly 20% lower than the volatility of the wage per efficiency unit of labor services, which has a standard deviation relative to output of .63. Both of these measures are highly correlated with output. The reason for this difference is that during good times, the participation region expands to include individuals with lower values of idiosyncratic productivity. Interestingly, fluctuations of the average wage for all new hires is significantly more volatile—by roughly 50% or so—than the average wage. Note that this is due entirely to composition effects and is not because wage setting differs for new hires relative to existing workers. Haefke, Sonntag, and van Rens (2008) documented that wages of new hires are more volatile than wages for existing workers and argued that this had important implications for wage setting and the equilibrium fluctuations.
in standard matching models. Gertler and Trigari (2009) cautioned that this conclusion might be premature if composition effects were significant. In our benchmark model these composition effects are large. Note, however, that the wage series for new hires in our model is not very highly correlated with output.

The above discussion of wage fluctuations is ultimately about composition changes in the employment pool. There is also a literature on the cyclical composition of the unemployment pool. Consistent with earlier arguments in Solon, Barsky, and Parker (1994), recent work by Mueller (2010) argues that the average quality of an unemployed worker rises significantly (on the order of two to three percent) in recessions. His measure of the productivity of an unemployed worker is based on the worker’s most recent wage when employed (typically 8 months earlier). Our model reproduces these findings. Figure 8 shows the change in the average worker productivity for all unemployed workers as the economy experiences the same transition as in Figure 4.

Figure 8: Response of average productivity of unemployed workers to a positive shock

There is an initial rise but a long-term fall in the quality of the unemployed during a boom. In the long run, this group is composed more of workers transiting from $N$ during
booms than during recessions, when the impact of recently separated workers (with higher $z$) on this pool is larger. The histogram for $U$ in Figure 6 also speaks to this composition effect: we see a larger mass of workers further from their indifference point, i.e., at high $z$ values, in recessions than in booms.

6 Relationship to the Literature

Having presented our results we are now in a better position to compare our findings with those of other recent papers. In particular, the key papers that we note are Galí, Smets, and Wouters (2011), Veracierto (2008), Christiano, Trabandt, and Walentin (2010), Shimer (2011), and Haefke and Reiter (2011). One key difference between our analysis and these other papers is that none of them focuses on gross worker flows, either in steady state or over the cycle. We believe this difference is critical. As we noted previously, any model of participation is going to implicitly have a boundary that determines the participation and non-participation regions. In response to an aggregate shock, the size of the movements in participation and nonparticipation must surely be heavily influenced by the mass of individuals that are near the boundary. To us it seems unclear how one could be confident in having an empirically reasonable mass of people near the boundary without modeling gross flows, since this is surely the single most relevant piece of information.

Having pointed this out, we next turn to some common findings regarding the behavior of the three labor market stocks in different contexts. We compare results both at a qualitative as well as quantitative level, since we think there are some robust qualitative findings across papers, despite many differences in model details. We begin with Veracierto (2008).\textsuperscript{22} Although Veracierto’s model has predictions for the stocks of workers in the three labor market states, the gross flows are not uniquely determined due to the fact that in equilibrium many workers are necessarily indifferent between two transitions. However, we can compare predic-

\textsuperscript{22}Veracierto extends the earlier work by Tripier (2004).
tions about the number of workers in each of the three states. There are some differences in details regarding model specification. For example, Veracierto’s analysis is explicitly general equilibrium with fluctuations driven by aggregate TFP shocks. Nonetheless, from the perspective of labor supply, our price shocks are very similar. Similar to us, Veracierto finds that although the model can generate substantial fluctuations in employment, it fares very poorly in accounting for the behavior of unemployment and participation. In particular, he finds that unemployment becomes procyclical. Veracierto ascribes the procyclical unemployment rate to the fact that when a high TFP shock occurs, individuals move from not-participating to participating, thereby increasing unemployment because it takes time to find a job. Figure 9 shows the dynamics in our model following a positive shock to prices only, and assuming that good state persists.

Figure 9: Response of labor market stocks to a positive shock to prices only

The figure shows that our model has the same initial response to an increase in TFP as in Veracierto’s model; that is, there is an immediate jump in the size of the labor force and an increase in unemployment. However, over time these individuals will become employed, and in our model the unemployment rate approaches a lower level than attained prior to
the shock. This asymptotic response turns out to dominate the immediate effect in terms of its effect on the correlation between the unemployment rate and output. Hence, while our model with price shocks only does not match the volatility of the unemployment rate, it does produce a countercyclical unemployment rate. Despite this one difference with the results in Veracierto, our model displays quantitative responses that are quite similar to his for the other variables.

Next we consider Shimer (2011). Shimer uses a fully specified search and matching model and assumes rigid wages to obtain significant and persistent fluctuations in the vacancy (i.e., recruiter) to unemployment ratio. In his model, all workers are alike in productivity and he finds that it is necessary to make search very costly in order to generate movements in the participation rate that are similar to those in the data. In contrast, our results show that allowing for a empirically reasonable amount of worker heterogeneity and an empirically reasonable extent of fluctuations in wages is sufficient, without having to assume high search costs. In our view, the search cost Shimer needs to match the data seems implausibly high: the magnitude of his cost implies that holding consumption constant, workers would rather work 35 or 40 hours per week than search for a little more than three hours per week. Shimer assumes identical agents and so does not have predictions for gross flows, since all nonparticipants are indifferent between participating and not participating. As we emphasized previously, it seems reasonable that the mass of individuals near the boundary will be critical for quantitative properties of the model.

A more closely related paper to ours is Haefke and Reiter (2011). Like us, they allow for idiosyncratic shocks and so in principle generate predictions for gross flows, though they examine both male and female labor supply and stress the interpretation of fluctuations in the value of home productivity. However, their focus is on other aggregates—the aggregate labor-supply elasticity—and they do not report gross flows. An important modeling difference

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23 The same is true for Christiano, Trabandt, and Walentin (2010), who also do not model gross flows.

24 See also Ebell (2011) for a related approach.
between our paper and theirs is that they have linear preferences and do not allow for income effects on labor supply. As we noted earlier, these effects are quantitatively important in our analysis.

Galí, Smets, and Wouters (2011) consider a model in which wages and a key driving force for business cycles is the extent of markups in the labor market. They find that they cannot match the behavior of participation with standard preferences. This result is similar in spirit to our finding for price shocks only. They go on to show that the model can generate participation responses similar to the data if they allow for externalities in preferences. Again, their model does not generate predictions for gross worker flows.

In summary, a common finding in the recent literature is that it is challenging to match the behavior of all three labor market stocks over the business cycle. Different papers have proposed different remedies. In our view these various remedies should be viewed as complementary. A distinguishing feature of our approach is to insist on a model that can connect to both the micro data on individual worker flows and to studies of labor supply.

7 Conclusion

We have developed a model of individual labor supply in the presence of frictions and used it to simulate the effects of aggregate shocks to prices and frictions on the labor market outcomes for of a large set of households. Our key findings are (i) that a model calibrated to match steady state flows does well in accounting for the cyclical movements of the flows; (ii) fluctuations in job finding and job loss rates alone cannot match the data; and (iii) the labor supply channel is important, despite the relatively modest, though procyclical, fluctuations in the labor force participation rate. It is interesting to note, in particular, that as a corollary our model with worker heterogeneity can match the fluctuations in the participation rate with a rather standard formulation of household preferences, something which has proved challenging with other setups.
Our model offers a rich yet parsimonious description of individual labor supply in a setting with heterogeneity, search frictions and an empirically reasonable market structure. It is the first paper to consider the effects of aggregate shocks on individual labor market transitions in this setting. However, it is also simplistic in some dimensions relevant for the microeconomic data. One of these dimensions regards our model of the household as an infinitely-lived unit. Clearly, an extension that distinguishes different members of the households would be relevant, as would an age dimension, along the lines of Low, Meghir, and Pistaferri (2010). Also, we have left out details of job experiences, including any specifics of what influences individual productivity (such as learning on the job and on-the-job search). Similarly, we abstract from an explicit consideration of search costs. We do believe that our framework is a very useful starting point for extensions in all these directions. Related, we also believe that it is useful for assessing a variety of further issues, such as the heterogeneous effects of business cycles on various subgroups of the population. While we have focused on aggregate shocks to frictions and the return to market activity, we can also study other aggregate shocks, including various candidates for demand shocks.

Finally, as pointed out above, in contrast with much of the literature—in particular the recent studies of Hall (2005) and Shimer (2005)—we focus on the worker side and leave open deeper, general equilibrium explanations behind the fluctuations in labor market frictions, as we leave open what drives the returns to market activity and, indeed, any connections between these shocks. The good performance of the model of course makes it all the more important to further isolate and study these drivers. One view in the literature is that a search/matching model with rigid wage formation and frictions that are entirely driven by productivity fluctuations can explain the data well. From the present perspective, such a model will likely be hard to square with labor market flows, since we have found the movements in the return to market activity necessary for understanding them.
References


Gross Job Creation, Gross Job Destruction, and Employment Reallocation


Appendix (Not For Publication)

A.1 Data

The Current Population Survey (CPS) reports the labor market status of the respondents each month that allows the BLS to compute important labor market statistics like the unemployment rate. In particular, in any given month a civilian can be in one of three labor force states: employed ($E$), unemployed ($U$), and not in the labor force ($N$). The BLS definitions for the three labor market states are as follows:

- An individual is counted as employed if he or she did any work at all for pay or profit during the survey month. This includes part-time or temporary work as well as full-time year-round employment.

- An individual is considered unemployed if he or she does not have a job, has actively looked for employment in the past 4 weeks and is currently available to work.

- An individual is classified as not in the labor force if he or she is included in the labor force population universe (older than 16 years old, non-military, noninstitutionalized) but are neither employed nor unemployed.

Households are interviewed for four consecutive months, rotate out for eight months and then rotate in for another four months. The panel feature of the CPS makes it possible to calculate transitions by individual workers between these three labor market states. However, not all the respondents stay in the sample for consecutive months; the rotating feature of the panel implies that only 75 percent are reinterviewed according to the CPS sampling design. Moreover, many other respondents cannot be found in the consecutive month due to various reasons and are reported as missing. The failure to match individuals in consecutive months is known as margin error and it causes biased estimates of the flow rates as discussed by Abowd and Zellner (1985), Fujita and Ramey (2009), and Poterba and Summers (1986). The simplest correction for margin error is to simply drop the missing observations and reweight
the transitions that are measured, a procedure that is known as the missing-at-random (MAR) method. However, this procedure could lead to biases if missing observations are not missing at random. To deal with this problem, Abowd and Zellner (1985) and Poterba and Summers (1986) proposed alternative corrections for margin error which use information on labor market stocks. Their correction reweights the unadjusted flows in order to minimizes the distance between the reported labor market stocks and the stocks that are imputed from the labor market transitions. We follow the algorithm proposed by Elsby, Hobijn, and Şahin (2012), which is similar in spirit to Poterba and Summers’ method, but differs in implementation. We use the basic monthly CPS files from January 1976 to December 2009 and data from January 1968 to December 1975 based on tabulations by Joe Ritter using data that was made available by Hoyt Bleakley. All transition probabilities are calculated for the population older than 16 years old and are seasonally adjusted.

A.2 Calibration of the Steady State

A key aspect of the steady state calibration procedure is to choose parameters so that the distribution of workers across the three labor market states and the flows of workers between states in the steady state equilibrium are similar to their average values over time in the US economy, that is, to ensure that the calibrated model has the requisite microfoundations. Official statistics divide non-employed workers into the two categories of unemployed and out of the labor force based primarily on how they answer a question regarding active search in the previous four weeks. Although our model does not feature a search decision, it can be mapped into this definition. Specifically, if active search is a discrete decision and the cost of search is very small, the decision to search amounts to asking an individual if he or she would prefer working to not working.\footnote{Given evidence from time use data on the amount of time devoted to search, we think it is reasonable to assume that the cost of active search is very small. An extension of this model to incorporate search costs is feasible, though it would require significantly more computer time. As discussed later in the paper, we conjecture that if search costs of the size estimated in the literature are allowed, the model would deliver very similar results to those obtained here.} Among those individuals in our model who are not
employed in period $t$, we will label anyone who would prefer to be employed “unemployed” and anyone who would prefer to not work “out of the labor force”.\footnote{In our earlier work we argued that a more natural way to connect the model to the data was to adopt a more inclusive definition of unemployment in the data, based on the desire to work rather than active search. Nonetheless, we found that the broader definition was not substantively important either in terms of the features in the data or the ability of the model to account for the data. We revert to the standard definition of unemployment in this paper because of the difficulty in getting a longer time series for flows between the states with the broader measure.}

The steady state model has nine parameters that need to be assigned: preference parameters $\beta$ and $\alpha$, production parameters $\theta$ and $\delta$, idiosyncratic shock parameters $\rho_z$ and $\sigma_\varepsilon$, frictional parameters $\sigma$ and $\lambda$, and the tax rate $\tau$. Because data on labor market transitions are available monthly, we set the length of a period to be one month. We set $\tau = .30$.\footnote{Following the work of Mendoza, Razin, and Tesar (1994) there are several papers which produce estimates of the average effective tax rate on labor income across countries. Minor variations in methods across these studies produce small differences in the estimates, but .30 is representative of these estimates.}

Because our model is a variation of the standard growth model, we can assign some parameter values following standard procedures used to calibrate versions of the growth model. Because of incomplete markets and idiosyncratic uncertainty, we cannot derive analytic expressions for the steady state, and so cannot isolate the connection between certain parameters and target values. Nonetheless, it is still useful and intuitive to associate particular targets and parameter values. Specifically, given values for $\lambda$, $\sigma$, $\rho_z$, and $\sigma_\varepsilon$, we choose $\theta = .3$ to target a capital share of .3, $\delta$ to achieve an investment to output ratio equal to .2, and the discount factor $\beta$ to target an annual real rate of return on capital equal to 4%. The other preference parameter $\alpha$, which captures the disutility of working, is set so that the steady state value of the employment to population ratio is equal to .61. This is the value of the employment to population ratio for the population aged 16 and older for the period 1968 – 2009.\footnote{We calibrate to values for the period 1968-2009 because this is the period for which we have consistent measures of labor market flows.}

It remains to choose values for $\lambda$, $\sigma$, $\rho_z$ and $\sigma_\varepsilon$. Recall that our idiosyncratic shock process should be viewed as a composite of all idiosyncratic shocks that affect the static return to working versus not working. Shocks to wages are of course only one such component. However, since these are the shocks that we have the best measures of, our benchmark
specification calibrates the shock process based on estimates of idiosyncratic wage shocks. Specifically, we choose values for $\rho_z$ and $\sigma_\varepsilon$ based on Floden and Linde (2001), who estimated $\rho_z = .92$ and $\sigma_\varepsilon = .21$ expressed on an annual basis. There is an intimate connection between $\lambda$ and the unemployment rate in the model. If $\lambda = 1$ then unemployment will be zero, since everyone always has the opportunity to work. We therefore choose $\lambda$ so that the steady state unemployment rate matches the average value for the unemployment rate in the US data for the period 1968-2009, which is .061. We choose $\sigma$ to target the average flow rate out of employment over our sample period, which is 3.6%. We target this rate based on our belief that the employment state is the one subject to the least amount of measurement error.

Table A1 summarizes the calibrated values and the various targets used in the calibration.

<table>
<thead>
<tr>
<th>Table A1</th>
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</thead>
<tbody>
<tr>
<td>Benchmark Calibration</td>
</tr>
<tr>
<td>Targets</td>
</tr>
<tr>
<td>$I = .20, r_K = .3, E^U = .610, \frac{U}{E + U} = .061, 1 + r - \delta = 1.04^{1/12}, E \rightarrow E = .954$</td>
</tr>
<tr>
<td>Parameter Values</td>
</tr>
<tr>
<td>$\theta$</td>
</tr>
<tr>
<td>.30</td>
</tr>
</tbody>
</table>

The labor market flows in our calibrated model and the data are displayed in Table A2.

<table>
<thead>
<tr>
<th>Table A2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Flows in the Data and the Model</td>
</tr>
<tr>
<td>US 1968-2009</td>
</tr>
<tr>
<td>FROM</td>
</tr>
<tr>
<td>$E$</td>
</tr>
<tr>
<td>$E$</td>
</tr>
<tr>
<td>$U$</td>
</tr>
<tr>
<td>$N$</td>
</tr>
</tbody>
</table>

Krusell et al. (2011) showed that the ability of the model to account for the flows between states remains relatively unchanged over a wide range of values of $\rho$ and $\sigma_\varepsilon$. What mattered most was that $\rho$ was reasonably persistent (at least .5), but not too close to being a unit root (say less than .97), and that $\sigma_\varepsilon$ was not too small. An issue for our quantitative exercises is the extent to which different specifications of the shock process influence our results, despite having little impact on worker flows. We carry out sensitivity analysis to assess this.
Overall the model does a reasonable job of capturing the salient features of the data. Specifically, it does a good job of capturing the degree of persistence in each of the three states. One major discrepancy is that the model does not generate enough flows from $U$ to $N$. Given our strategy of targeting the stock of workers in $U$, this necessarily implies that the other flow out of $U$ (i.e., the flow from $U$ to $E$) must also be off.

One issue that was not explicitly considered in our earlier work that we want to discuss here concerns classification error. There is strong evidence in the literature (see, e.g., Poterba and Summers (1986)) that classification errors lead to spurious flows, especially between unemployment and not in the labor force. One strategy for addressing this would be to try to purge the official data of measurement error. Unfortunately, this is not feasible. The survey that Poterba and Summers used to estimate the extent of classification error on transition rates was discontinued shortly thereafter. Instead, we deal with this issue by adding some measurement error to the data generated by our model. We provide details on this procedure in Appendix A.3 and show that with an empirically plausible amount of measurement error the model does a much better job of matching the flows between $U$ and $N$. While classification error is important in matching the average behavior of flows in the data, we show in Appendix A.3 that it is not important for our key findings about business cycle fluctuations.

**A.3 Classification Error**

As discussed in Appendix A.2, there is strong evidence that classification errors lead to spurious flows. In this section, we allow classification errors to induce spurious transitions between $U$ and $N$ and examine how our results are affected. In particular, following the estimates of Poterba and Summers (1986), we assume that a consumer with true state $U$ state misreports it as $N$ with probability 0.1146 and that a consumer with true state $N$ state misreports it as $U$ state with probability 0.0064.\(^{30}\) We recalibrate the model, setting $\alpha$, $\lambda$,
and $\sigma$ in order to match the observed employment population ratio of .61, the average value of unemployment rate of .061, and the average flow rate out of employment of 3.6%. The new parameter values are $\alpha = 0.606, \lambda = 0.423, \sigma = 0.0135$.

Table A3

<table>
<thead>
<tr>
<th>Flows in the Data and the Model with Classification Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>US 1968-2009</td>
</tr>
<tr>
<td>FROM</td>
</tr>
<tr>
<td>-------</td>
</tr>
<tr>
<td>E</td>
</tr>
<tr>
<td>0.954</td>
</tr>
<tr>
<td>0.030</td>
</tr>
<tr>
<td>U</td>
</tr>
<tr>
<td>0.270</td>
</tr>
<tr>
<td>0.222</td>
</tr>
<tr>
<td>N</td>
</tr>
<tr>
<td>0.048</td>
</tr>
<tr>
<td>0.925</td>
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</tbody>
</table>

Steady state flows are presented in Table A3. Comparing with Table A2, the $UE$ transition rate goes down slightly, resulting in a slightly better match with data. The $UN$ transition rate increases substantially and is almost as high as in the data. The match of the $UU$ transition rate somewhat worsens.

With this new set of parameter values, we repeat the exercise for our benchmark model, recalibrating the parameters of the driving forces to match the same targets as in the main text (the standard deviation of employment, the standard deviation of the $EU$ flow rate, the standard deviation of the $UE$ flow rate). The new parameter values are: $\varepsilon_Z = 0.02895$, $(\lambda_G, \lambda_B) = (0.4937, 0.3523)$, and $(\sigma_G, \sigma_B) = (0.01289, 0.01411)$. Table A4 presents the results.

Table A4

<table>
<thead>
<tr>
<th>Behavior of Stocks with TFP and Job Availability Shocks</th>
</tr>
</thead>
<tbody>
<tr>
<td>Volatilities: $std(x)$</td>
</tr>
<tr>
<td>------------------------</td>
</tr>
<tr>
<td>$u$</td>
</tr>
<tr>
<td>Data</td>
</tr>
<tr>
<td>Model (Benchmark)</td>
</tr>
<tr>
<td>Model (CE)</td>
</tr>
</tbody>
</table>

The row labeled Model (Benchmark) simply repeats Table 5 from the paper. The row labeled Model (CE) is the model that incorporates classification error. The results from the new exercise are almost identical to the benchmark result, except that the cyclicality of the labor force participation rate is slightly weaker.
Table A5 describes the cyclical properties of the flows.

<table>
<thead>
<tr>
<th>Table A5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Flows in the Benchmark and CE Models</td>
</tr>
<tr>
<td><strong>A. Data</strong></td>
</tr>
<tr>
<td>( f_{EU} )</td>
</tr>
<tr>
<td>std(( x ))</td>
</tr>
<tr>
<td>corr(( x, Y ))</td>
</tr>
<tr>
<td>corr(( x, x_{-1} ))</td>
</tr>
<tr>
<td><strong>B. Model (Benchmark)</strong></td>
</tr>
<tr>
<td>( f_{EU} )</td>
</tr>
<tr>
<td>std(( x ))</td>
</tr>
<tr>
<td>corr(( x, Y ))</td>
</tr>
<tr>
<td>corr(( x, x_{-1} ))</td>
</tr>
<tr>
<td><strong>B. Model (Classification Error)</strong></td>
</tr>
<tr>
<td>( f_{EU} )</td>
</tr>
<tr>
<td>std(( x ))</td>
</tr>
<tr>
<td>corr(( x, Y ))</td>
</tr>
<tr>
<td>corr(( x, x_{-1} ))</td>
</tr>
</tbody>
</table>

The two sets of model results are almost identical, except that the \( EN \) and \( NE \) transition rates are slightly more cyclical and persistent. Note that in this exercise we have assumed that classification errors do not have a cyclical component. This is consistent with recent work of Elsby, Hobijn, and Şahin (2012).

**A.4 Model and Computation**

We discipline the links among relevant variables (and the workers’ expectations) by building a general equilibrium model in the background.

The general equilibrium structure is very simple. The economy is populated by continuum of (population one) workers whose decision problem is described in Section 3.1. On the firm side, there is a representative firm who operates competitively\(^{31}\) with production function

\[
Y_t = Z_t K_t^\theta L_t^{1-\theta},
\]

where \( \theta \) is set at .3. \( K_t = \int k_{it} di \) is aggregate input of capital services (which is the sum of the workers’ assets) and \( L_t = \int e_{it} z_{it} di \) is aggregate input of labor services (which is the aggregate supply of labor.

\(^{31}\)One can think of a “island” structure as in Krusell et al. (2011) in order to maintain consistency between the labor market frictions and the competitive behavior by firms and workers.
sum of the employed workers’ efficiency unit of labor). Output $Y_t$ can be used either for consumption and investment, and capital depreciates at the rate $\delta = .0067$.

The government balances budget every period, that is, it sets the lump-sum transfer $T_t$ by

$$T_t = \int \tau w_t e_i z_t d_i$$

where $\tau = .30$.

One can define a Recursive Competitive Equilibrium of this economy in a standard manner, that is, (i) workers optimize given the price functions and the perceived laws of motion for aggregate state variables, (ii) the representative firm optimizes, (iii) the markets clear, (iv) the government budget clears, and (v) the actual laws of motion and the perceived laws of motions for the aggregate state variables are consistent with each other. The prices $w_t$ and $r_t$ in the main text are from this Recursive Competitive Equilibrium for given processes of aggregate shocks ($Z_t$, $\lambda_t$, and $\sigma_t$).

The computation follows the algorithm which is briefly summarized below and described in more detail later subsequently.

1. Replace $\Omega$ by more limited information that can easily be kept track of. Here, we choose the current aggregate capital stock $K$ and the aggregate capital-labor ratio in the previous period, $M_{-1} \equiv K_{-1}/L_{-1}$, as the information that the consumers use when they make decisions.

2. The consumers have to forecast tomorrow’s aggregate capital $K'$ and also need to calculate today’s aggregate capital-labor ratio $M = K/L$ (to know the prices today).

We use the following simple forecasting rules:

$$\log(K') = a_0 + a_1 \log(K) + a_2 \log(z) + a_3 \log(M_{-1})$$

and

$$\log(M) = b_0 + b_1 \log(K) + b_2 \log(z) + b_3 \log(M_{-1}).$$
At the first iteration, make a guess for the values of $a_0$, $a_1$, $a_2$, $b_0$, $b_1$, and $b_2$.

3. Obtain the prices $r$ and $w$ from $z$ and the forecasted $M$. Obtain $T$ from $w$, $K$, and the forecasted $M$. Solve the optimization problem of the consumers.

4. Simulate the economy using the decision rules of the consumers obtained above. In particular, we can obtain the time series of $K$ and $M$. Check whether the law of motion for $K'$ and the forecasting rule for $M$ guessed above are consistent with the simulated values. That is, run a regression using the simulated data to see if the coefficients conjectured above are identical to the ones obtained from the regression (also check the fit of the regression). If they are different, modify the coefficients and go back to the previous step. Repeat until the coefficients have converged.

We find that this procedure works well in our model, and the resulting forecasting rules are remarkably accurate. This means that even if we add more information to each consumer’s information set, the consumer cannot forecast much better.

In detail, the steps are as follows.

1. The aggregate information set $\Omega$ is restricted to a limited set of information. In particular, we limit the information to the current aggregate state $Z$, the current aggregate capital stock $K$, and the aggregate capital-labor ratio in the previous period $M_{-1} \equiv K_{-1}/L_{-1}$. Then, the value functions can be rewritten as $V(k, z, Z, K, M_{-1})$, $W(k, z, Z, K, M_{-1})$, and $N(k, z, Z, K, M_{-1})$, where

\[
V(k, z, Z, K, M_{-1}) = \max\{W(k, z, Z, K, M_{-1}), N(k, z, Z, K, M_{-1})\},
\]

and the Bellman equations for $W$ and $N$ are given by:

\[
W(k, z, Z, K, M_{-1}) = \max_{c, k'} \{\log(c) - \alpha + \beta E_{z', Z''}[(1 - \sigma(1 - \lambda))V(k', z', Z', K', z', Z', K', M)]\}
\]

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s.t. $c + k' = r(Z, K, M_{-1})k + (1 - \tau)w(Z, K, M_{-1})z + (1 - \delta)k + T(Z, K, M_{-1})$

$$c \geq 0, \ k' \geq 0$$

and

$$N(k, z, Z, K, M_{-1}) = \max_{c, k'} \{ \log(c) + \beta E_{z', Z', K'} [\lambda V(k', z', Z', K', z', Z', K')] \}$$

s.t. $c + k' = r(Z, K, M_{-1})k + (1 - \delta)k + T(Z, K, M_{-1})$

$$c \geq 0, \ k' \geq 0.$$

2. In order to calculate the right hand sides of the Bellman equations (3) and (4), the consumer has to be able to see the prices today and form an expectations on the future aggregate state variables. We adopt a log-linear forecasting rules:

$$\log(K') = a_0 + a_1 \log(K) + a_2 \log(Z) + a_3 \log(M_{-1})$$

and

$$\log(M) = b_0 + b_1 \log(K) + b_2 \log(Z) + b_3 \log(M_{-1}).$$

At the first iteration, we make a guess for the values of $a_0, a_1, a_2, b_0, b_1,$ and $b_2.$

3. We discretize the state space. For the aggregate shocks, the vector $(Z, \lambda, \sigma)$ can take two possible sets of values—these values vary with experiments, and are detailed in the main text. $z$ is discretized into 20 points. The grids are equally spaced in terms of $\log(z),$ from the minimum of two standard deviations below the mean and the maximum of two standard deviations above the mean. The individual asset has 48 grids for the
purpose of the individual optimization, ranging from 0 to 1440 (the average capital holding is 183.7). The grids are (smoothly but) unequally spaced so that there are more grids on the smaller side of $k$ (this is because there is more curvature in the value functions around the smaller values of $k$). We set 5 equally spaced grids on $K$ (ranging from 160 to 200 for the benchmark) and 5 equally spaced grids on $M_{-1}$ (ranging from 145 to 185 for the benchmark).

For each aggregate state (and using (6), the prices and the transfer can be calculated as

\[
\begin{align*}
\tau &= \theta ZM^{\theta-1}, \\
w &= (1 - \theta)ZM^\theta,
\end{align*}
\]

and

\[
T = \tau w \frac{K}{M}.
\]

Then we perform the optimization at each grid point and iterate over the value functions in order to solve the Bellman equations (3) and (4). Along $K'$ and $M$ directions, the value functions are interpolated using a polynomial interpolation where necessary. A linear interpolation is used in $k'$ direction. We start from the guesses on $V$ and $N$ functions, then obtain the new $W$ function and the new $N$ function from the right hand sides of (3) and (4), and then obtain the new $V$ function from (2). We search for optimal asset decision globally using golden section search. We use global method without differentiation (with linear interpolation) because of potential nonconcavity and nondifferentiability due to the discrete labor-leisure choice.

4. Once the Bellman equations are solved (and we have the value functions and the policy functions for the asset choice), we simulate the economy. In particular, we draw 5000 periods of the aggregate shocks, start from the stationary distribution of (asset, productivity, employment) in the steady state model, and iterate over the density functions.
For this simulation, we increase the number of grids in $k$ direction to 12001. (The policy functions are linearly interpolated in $k$ direction. For $K$ and $M_{-1}$ directions, polynomial interpolations are used where necessary.)

The detail of the simulation is as follows. We have a mass of consumers on a particular grid of (asset, productivity, employment). Given the current aggregate state, we know how this mass is divided and moved into the next period (asset, productivity, employment) grids, given the policy functions and the transition probabilities.

Two details to note here—for the asset direction, since the decision rules are continuous, most likely $k'$ won’t fall on the exact grid point. We divide the mass linearly in that case—if the decision rule says that $k'$ for a particular (asset, productivity, employment) combination would be $0.3k_n + 0.7k_{n+1}$ (where $n$ is the index of the grid point), then we allocate 30% of people on $k_n$ and 70% of people on $k_{n+1}$ in the next period. For the employment direction, we have to decide whether the people who moved to a particular (asset, productivity, employment) would work or not in the next period in the cases where they have a choice. This can simply be done by comparing $W$ and $N$ next period at each grid points, given the next period aggregate state. One drawback of this simple method is that the employment distribution will be the same between the case where $(W_n > N_n, W_{n+1} \ll N_{n+1})$ and $(W_n \gg N_n, W_{n+1} < N_{n+1})$ (where the subscript is the grid index of $k'$ where the value function is evaluated), and the labor supply can potentially jump with a small change in environment if the threshold value crosses a grid point. In order to “smooth out” this effect, we linearly interpolate the employment decision based on the distances of the value functions at each grid points. In effect, we are supposing that consumers are distributed uniformly between $k_{n+1}$ and $k_n$ instead of having a mass at $k_n$ (except at the maximum grid point) and approximating the value function by linear interpolation in between these grids.\(^{32}\)

\(^{32}\)This smoothing method introduces a small downward bias in the level of labor supply, but this effect

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Once the simulation is done, we have a time series of \((Z, K, M_{-1})\). Using this time series (discarding the first 1000 periods), we run OLS regressions (5) and (6). We repeat the same steps until the coefficients converge.

The converged forecasting equations are

\[
\log(K') = 0.050234 + 1.004265 \log(K) + 0.000514 \log(Z) - 0.014181 \log(M_{-1}), \quad R^2 = 0.999998
\]

and

\[
\log(M) = -0.147328 + 0.280710 \log(K) - 0.070561 \log(Z) + 0.742800 \log(M_{-1}), \quad R^2 = 0.990492
\]

for the experiment with only frictions \((Z_G = 1.016 \text{ and } Z_B = 0.984 \text{ are used for the purpose of these forecasting rules})\),

\[
\log(K') = 0.064087 + 0.991358 \log(K) + 0.027667 \log(Z) - 0.003739 \log(M_{-1}), \quad R^2 = 1.000000
\]

and

\[
\log(M) = -0.658345 + 0.828787 \log(K) - 0.276471 \log(Z) + 0.284357 \log(M_{-1}), \quad R^2 = 0.998948
\]

for the case of \(Z\) only, and

\[
\log(K') = 0.061413 + 0.993660 \log(K) + 0.028053 \log(Z) - 0.005560 \log(M_{-1}), \quad R^2 = 1.000000
\]

and

\[
\log(M) = -0.558708 + 0.745101 \log(K) - 0.326600 \log(Z) + 0.350141 \log(M_{-1}), \quad R^2 = 0.999771
\]

for the benchmark case.

Once all above is done, we simulate many consumers to obtain the statistics of interest. (In this simulation, we do not need any interpolation for the next period employment—we simply compare the value function.) We simulate 100,000 people to obtain the statistics of the tables. For the “impulse response” diagrams, we simulate 10,000,000 people.

is negligible given the large number of grids. We cross-checked with the simulation with a large number of individuals and the behavior of aggregate variables is almost identical. Clearly one can use a more elaborated method of adjustment, but we choose this method due to its simplicity.