The Overnight Drift

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Abstract
This paper documents that U.S. equity returns are large and positive during the opening hours of European markets. These returns are pervasive, economically large, and highly statistically significant. Consistent with models of inventory risk, we demonstrate a strong relationship with order imbalances at the close of the preceding U.S. trading day. Rationalizing unconditionally positive “overnight drift” returns, we uncover an asymmetric reaction to demand shocks: market selloffs generate robust positive overnight reversals, while reversals following market rallies are much more modest. We argue that demand shock asymmetry can arise in inventory management models with time-varying dealer risk bearing capacity.

Key words: overnight returns, immediacy, volatility risk, inventory risk
Since the advent of electronic trading in the late 1990’s, U.S. S&P 500 index futures have traded close to 24 hours a day. In this paper, we document that, despite the 24 hour nature of the market, returns do not accrue linearly around the clock. In fact, the largest positive returns are between 2:00 and 3:00 - the opening of European markets in U.S. Eastern Time terms (ET) - averaging 3.7% on an annualized basis (1.48 basis points per day). We dub these positive average returns the ‘overnight drift’ and argue that the pattern is most likely driven by the overnight resolution of order imbalances arising from the end of the preceding U.S. trading day.

We begin by dissecting trading during the U.S. overnight session and introduce a number of tests which demonstrate that returns during the 2:00 – 3:00 window are special in both economic and statistical terms. First, inspired by the data mining literature, we conduct a bootstrap exercise to estimate the distribution of test statistics of average hourly returns. Considering the distribution of point and \( t \)-statistic estimates for all hours we find a clear bi-modal distribution, with the 2:00 – 3:00 return corresponding to the higher mode. Strikingly, when comparing the distribution for all hours with the overnight drift hour, we see that the lower 2.5% interval for overnight drift return point estimates lies above the pooled 97.5% interval. Likewise, the lower 2.5% interval for the distribution of \( t \)-statistics lies above the pooled 97.5% interval. Second, accounting for multiple testing concerns, we consider Bonferroni and Benjamini-Yekutieli adjusted critical values and show that the only hour which remains consistently significant in full sample and subsamples is 2:00 – 3:00.

Next, following the fund alpha literature, we study the persistence of overnight drift returns: they are positive in 20 out of 23 years since 1998 and statistically significant in 17 of these. In contrast, for example, opening hour returns between 9:00 – 10:00 are on average large and negative but only during recessionary periods (2000-2003, 2007-2008 & 2009) and flat otherwise. Furthermore, we show that the 2:00 – 3:00 return is statistically significant on every day of the week, and in 9 out of 12 months of the year, while returns during other periods of the day enter sporadically.

The theoretical market microstructure literature offers two broad types of potential explanations for the overnight drift pattern: the presence of differentially informed traders in the market, generating asymmetric information, and inventory (risk) management by market makers. For asymmetric information alone to explain the overnight drift, (1) news revelation to informed traders would need to systematically occur between the U.S. market close and the European market open and (2) the information revealed overnight would need to be positive on average. We show that stan-
standard information releases, such as macroeconomic, monetary policy and earnings announcements, do not explain the overnight drift, suggesting that asymmetric information alone is an implausible explanation for the overnight drift.

Studying potential explanations, we argue that unconditionally positive returns around the opening of European markets are consistent with predictions from models of inventory management and demand for immediacy, such as Grossman and Miller (1988) (GM). The framework of GM shows that risk-averse market makers profit by providing liquidity to investors with asynchronous trading demands, generating mean reversion in prices as market makers absorb shocks to their inventories. To understand how inventory management concerns can lead to the overnight drift, suppose there is selling pressure during the day, translating into an overall negative order imbalance by the end of regular trading hours. Market makers become net buyers, bearing inventory risk until they are able to sell to new market participants arriving overnight; however, they demand compensation for this in terms of positive expected returns.

A natural question that arises is why do price reversals not occur earlier upon the opening of overnight markets? The answer is that, even though overnight volumes have grown steadily over our sample period, the close of regular trading at 16:15 marks the only time of the day when volumes jump discontinuously down. Even in recent years volumes during Asian open hours remain substantially below volumes at the U.S. close: between 2009 – 2020 trading volumes in regular Asian hours (18:00 – 2:00) were 50 to 100 times lower than volumes during U.S. trading hours. Indeed, recasting the trading day in volume time, where each period has a fixed number of contracts traded, returns increase linearly in signed volume until around 60,000 contracts, corresponding to the average number of contracts traded by 3:00. In other words, it takes market makers roughly 60,000 contracts to offset end-of-day order imbalances as of the previous day, with this re-balancing occurring earlier during the night as trading increases during Asian market hours. Conditioning on end-of-day order imbalances, we show the relationship between signed volume and returns in volume-time is approximately linear but asymmetric; thus, re-cast in volume time, demand shock asymmetry is a more general feature of the data observable throughout Asian and European hours.

We study in greater detail predictions from GM-type models which state that returns for pro-

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1 The CME does not designate ‘specialist’ market makers in e-mini futures. Instead, effective market makers are any participants willing to post limit orders on both sides of the order book and hence supplying liquidity (immediacy) to other traders in the market.

2 As pointed out by Easley, de Prado, and O’Hara (2012), in the high-frequency world, trade time, as captured by volume, is a more relevant metric than clock time and models of immediacy and inventory risk, such as Grossman and Miller (1988), are implicitly set in volume time as it is assumed that a fixed number of trades occur in each period.
viding immediacy should be higher when order imbalances are larger or uncertainty is higher. In order to exploit as much data as possible and to account for a time-trend in volumes, our main proxy for order imbalance is defined as relative signed volume, computed as signed volume over gross volume, and denoted $RSV_t$. On average, close-to-close $RSV_t$ is negative consistent with the idea that the futures market is traded as a hedging instrument for the underlying.

Sorting our full sample based on closing $RSV_t^{close}$, sampled between 15:15 – 16:15, we show that order imbalances at U.S. close are followed by overnight price reversals as predicted by inventory models and that price reversals following market sell-offs are much stronger than following market rallies. Moreover, price reversals are accompanied by contemporaneous trading flows in the expected direction. We also study the additional intuitive prediction that market makers should not require a liquidity premium for holding zero inventory, and therefore order imbalances close to zero should have little price impact. Consistent with this idea, when closing imbalances are approximately zero, we find reversal returns which are economically small and statistically indistinguishable from zero.

Next, we study the relationship between overnight returns and uncertainty. In double sorts on $RSV_t^{close}$ and the end-of-day level of VIX, we show that, conditional on the level of the VIX, average overnight returns are higher following days with greater negative end-of-day order imbalance. Conversely, conditional on the size of negative end-of-day order imbalance, average overnight returns are higher following days with greater end-of-day levels of the VIX. That is, consistent with the predictions of models of immediacy, price reversals are larger following days with larger end-of-day order imbalances and even more so if the large order imbalances coincide with periods of elevated uncertainty.

Double sorts on order imbalances and uncertainty also reveal that the distribution of the VIX is similar across positive and negative order imbalance days, suggesting that the asymmetry in price reversals is unlikely driven by a correlation between order imbalances and the level of asset return variance. Instead, we speculate that this asymmetry is related to market maker time-varying risk-bearing capacity. The literature on financial intermediation has proposed a number of mechanisms that can generate variation in effective risk aversion, including regulatory constraints, risk-management constraints, and funding constraints. Studying a simple extension to the benchmark

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3 Our findings are robust to tests based on signed volume over the sample period 2007 – 2020 for which total gross volumes were relatively stable.

4 While hourly $RSV_t$’s are negative during regular trading hours they are economically small at market close. However, overnight imbalances are positive and strongly statistically significant between 2:00 and 3:00, mirroring unconditionally positive returns during this hour.
GM model, we show that demand shock asymmetry arises when dealers face value-at-risk (VaR) constraints as in Danielsson, Shin, and Zigrand (2004) and Adrian and Shin (2010, 2014a). In the data, negative end-of-day imbalances are associated with positive changes in return variance.\(^5\) Positive shocks to volatility increase the likelihood that dealer constraints bind, magnifying their effective risk aversion during sell-offs and increasing required compensation for providing immediacy. During market rallies the opposite intuition holds.\(^6\)

We confirm our inventory risk conjecture more formally by estimating high frequency predictability regressions of returns on end-of-day order imbalance, and find statistically and economically significant loadings on the hours when London and Frankfurt financial markets open. Thus, high frequency returns become predictable as market makers transact with new participants arriving overnight, trading away order imbalances remaining from the previous U.S. trading day. Exploiting high frequency predictability regressions further, we conduct a natural experiment to test the relationship between the overnight price reversals and the arrival of overnight traders. In particular, we exploit the fact that while the U.S. observes daylight savings time (DST), Japan does not, so that, as seen from the perspective of a U.S. trader, the timing of Japanese market opening changes exogenously from 19:00 in winter to 20:00 in summer.\(^7\) Indeed, accounting for DST, return predictability around Tokyo open shifts forward by one hour when moving from winter to summer time, so that exogenous variation in the time of arrival of liquidity traders leads to predictable variation in the returns earned overnight. Expanding the natural experiment to also include the 3 weeks of the year when the DST is asynchronous between the U.S. and Europe, we again find that the overnight return predictability shifts to the 4:00 – 5:00 hour (the first hour of regular trading in London and Frankfurt when the U.S. – Europe time difference is 4 hours).

We conclude by studying a set of trading strategies that exploit overnight price reversals. Pre-transaction costs, a trading strategy that goes long the S&P 500 futures between 2:00 and 3:00 earns a Sharpe ratio of 1.1 and accounting for bid-ask spreads this reduces to −0.5. Extending the trading interval to the sub-period between 1:30 – 3:30 increases the pre-transaction cost Sharpe ratio to 1.3 but with an associated post-transaction Sharpe ratio equal to 0.3. This is exactly what is predicted by models of inventory risk: market makers position their limit order books to incentivize trades

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\(^5\)This is the so called ‘leverage effect’ which is the well studied empirical fact that equity volatility tends to rise when returns are negative, and fall when returns are positive (see, for example, Black, 1976).

\(^6\)Alternatively, if the permitted VaR is given as a fraction of equity, rather than as a dollar amount, the VaR constraint becomes tighter when market maker equity declines. Brunnermeier and Pedersen (2009) show that similar dynamics can also arise when market makers have to post (cash) margins to fund levered positions.

\(^7\)The Tokyo Stock Exchange trades from 9:00 to 15:00 in Japanese Standard Time.
that bring their inventory closer to their targets, and do so by making the trade, which pays the bid-ask spread, non-profitable.

Finally, we note that although the documented high frequency return patterns of this paper are not easily profitable, the persistent presence of the overnight drift suggests that the intraday timing of portfolio adjustments should be an important consideration for asset managers and institutional investors. Indeed, market developments suggest that arbitrageurs are trying to capitalize on the patterns identified in this paper, with NightShares launching two exchange-traded funds (ETFs) in June 2022, targeted specifically at earning the overnight drift, citing financing costs and end-of-day order imbalances as driving forces behind the pattern.8

**Related Literature:** In the time-series, existing studies have documented that equities earn a substantial proportion of their returns during the overnight period compared to the regular U.S. trading-hours (for example, Cliff, Cooper, and Gulen, 2008 or Kelly and Clark, 2011). In work subsequent to ours, Bondarenko and Muravyev (2020) replicate our finding that the lion’s share of CTC equity futures returns are earned around the opening hours of European markets.

In the cross-section, Heston, Korajczyk, and Sadka (2010) study high frequency periodicity in firm level returns documenting persistent intraday return reversals, which the authors argue arise because investors have predictable demand for immediacy at certain points within the day. Lou, Polk, and Skouras (2017) document firm level reversal patterns between intraday and overnight returns: overnight (intraday) returns predict subsequent overnight (intraday) returns positively, while overnight (intraday) returns predict subsequent intraday (overnight) returns negatively. The authors link this pattern to a ‘tug of war’ between retail investors trading at the beginning of the day and institutional investors who trade at the end of the day. Bogousslavsky (2018), on the other hand, studies institutional constraints and a cross-section of intraday pricing anomalies.

Finally, we motivate our empirical design from a literature that studies demand for immediacy and inventory risk (Grossman and Miller, 1988; Vayanos, 2001; Brunnermeier and Pedersen, 2009; Rostek and Weretka, 2015). A common prediction of these models links price reversals to temporary order imbalances absorbed by liquidity providers.9 Indeed, the Duffie (2010) presidential address reviews price dynamics with ‘slow-moving’ capital and highlights that ‘Even in markets that are extremely active, price dynamics reflect slow capital when viewed from a high-frequency perspective.’

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8See, for example, [www.ft.com/content/e64bd276-c58f-441e-8cea-dccf58bfb46f](www.ft.com/content/e64bd276-c58f-441e-8cea-dccf58bfb46f)

9For a textbook treatment we refer the reader to Foucault, Pagano, and Röell (2013).
I. Data

Our primary focus is data on intraday trades and quotes for S&P 500 futures contracts traded on the Chicago Mercantile Exchange (CME). The initial S&P 500 futures contract was introduced by the CME in 1982, trading both by open outcry and electronically during U.S. regular trading hours concurrently with the cash market.\textsuperscript{10} This ‘big’ futures contract (henceforth $SP$) was originally quoted with a multiplier of $500 per unit of underlying, so that if the index trades, for example, at $500, the value of the $SP$ contract is $250,000. As the index level rose over time, the $SP$ contract became expensive to trade at this multiplier and the contract multiplier was cut to $250 times the index on November 3, 1997.\textsuperscript{11} In September 1993, the $SP$ contract began trading electronically outside regular hours via the CME GLOBEX electronic trading platform. The S&P 500 e-mini futures contract (henceforth $ES$) was introduced on September 9, 1997 and is quoted at fifty times the index, i.e. one-fifth of the big $SP$ contract. The ‘e’ in e-mini is for electronic as trading takes place only on the CME GLOBEX platform which facilitates global trade for (almost) 24-hours a day, 5-days a week. The two futures contracts have quarterly expiries on the third Thursday in March, June, September and December. The most traded contract is almost always the front contract (the contract closest to expiry). Only when the front contract is close to expiry is the back contract (the contract second closest to expiry) more traded. This is because market participants roll their positions in advance of the expiry. We always use the most traded contract.

Exact trading times on CME platforms have changed over time but today trades are executed continuously from Sunday (18:00) – Friday (17:00), with a daily maintenance as of 2020 between 17:00 and 18:00.\textsuperscript{12}

Our primary data source exploits tick-by-tick data on trades and quotes for the $ES$ contract from Refinitiv Datascope Select, which we complement with data obtained directly from the CME.\textsuperscript{13} The trades dataset includes the trade price, trade size and trade time. The quotes dataset includes quote price, quote size and quote time, with the first five levels of the order book available at all

\textsuperscript{10}Regular trading hours are defined by the open outcry or pit session which trades between 9:30-16:15

\textsuperscript{11}The minimum tick size was also cut to 0.25. See Karagozoglu, Martell, and Wang (2003) for a discussion on how this change affected market liquidity and volatility.

\textsuperscript{12}Between November 1994 and December 2012 the trading week began on Sunday at 18:30 and closed on Friday at 16:15. The trading day (other than Sundays) ran from 18:00 one day to 17:30 the following day with maintenance break between 16:15 – 16:30. From December 2012 to December 2015 trading began half an hour earlier on Sundays (18:00) and closed one hour later Fridays (17:15 ET). There was also a maintenance break from 23:00 to 00:00 on Tuesday through Friday from October 1998 to September 2003.

\textsuperscript{13}Refinitiv Datascope Select was formerly known as Thomson Reuters Tick History.
times. All trades and quotes are time-stamped to the millisecond, using Universal Time (UT). We convert the UT timestamps to U.S. Eastern Time (ET), and define the intraday (ID) and overnight (ON) trading sessions relative to the opening hours of the U.S. cash equity market. We identify the direction of trades by comparing the trade price to the most recent quoted prices of the top level in the limit order book: buy (sell) orders trade at the best available ask (bid) price. Our sample period with 24 hour trading starts in January 1998 and ends in December 2020. Market depth for the first 5 levels of the order book is available since 2009.

Panel (a) of figure 1 displays within-the-month average daily trading volume for the SP and ES contracts where the ES is further split by volumes within ON and ID trading sessions. We measure volume as the total number of contracts traded in the most liquid contract, multiplying the volume for the SP contract by 5 (10 prior to 1998) to make its volume comparable to the ES. The figure shows that, since the advent of electronic trading, volume in the SP has trended down over time. Instead, the trading volume in the ES (plotted in red for ON and blue for ID) was growing in the run up to the 2008 financial crisis, and thereafter stabilized at around 1-2 million contracts traded per day. Turning to panel (b), we see that, while the annual volume traded ON as a percentage of overall volume was small and constant at around 2% until the years 2002, it increased somewhat linearly to around 15% in 2010 and remained flat until 2018. In 2018, with the level of the index above 2000, using the index multiplier of 50, this implies $15 billion traded daily during the overnight session. We also note that in the final years of our sample (2019 & 2020) the share of overnight trading in the ES has again increased and stands at around 20% of total volumes.

II. Returns around the clock

This section studies intraday returns computed from the most liquid e-mini contract, which is almost always the front month contract, except in expiration months when contracts are rolled. Returns are computed from mid quotes of best bid-offers. Our sample period spans January 5, 1998 – December 31, 2020 (23 years).

14Throughout the paper we use military time so that 2:00 corresponds to 2:00 a.m., and 16:30 corresponds to 4:30 p.m.
A. Main result

The $n$-th log return on day $t$ is defined as

$$r_{t,n}^N = p_{t,\frac{n}{N}} - p_{t,\frac{n-1}{N}}$$

for $n = 1, \ldots, N$, where $p_{t,\frac{n}{N}}$ denotes the log price at time $n/N$ on day $t$ and $N$ is the number of return observations throughout the day. $n = 0$ and $n = N$ corresponds to 18:00 when a new trading day begins as defined by the CME. We work interchangeably with hourly returns ($N = 24$), 15-minute returns ($N = 96$), 5-minute returns ($N = 288$), and 1-minute returns ($N = 1440$).

The grey bars in figure 2 display hour-by-hour log returns and the black line depicts cumulative 5-minute log returns, averaged across all days in our sample. Estimates are annualized in percentage points and show that ON returns are positive, on average, between the hours of 00:00 and 4:00. Thirty minutes prior to the opening of the cash market at 9:30 equity returns are initially large and negative and become smaller in magnitude but remain persistently negative until 12:00. We dub negative return realizations between 9:00 – 10:00 ‘opening hour’ returns. The ID period is then characterized by a flat return profile until 15:00, which is followed by a sequence of positive returns that turn strongly negative after the maintenance break.

This overnight return pattern is surprising. The red line in figure 2 plots the cumulative average return profile one would expect if information arrived continuously and returns accrued linearly, which contrasts starkly to the realised return profile displayed in back. On average, the CTC log return is 5.9%, which is close to the average yearly log return on the S&P 500 index cash (excluding dividends). More than half of this return is generated during the ON session: from 16:15 to 9:30 equity returns averaged 3.6% p.a. More striking than this, the return earned during the 2:00 to 3:00 hour averaged 3.7% p.a. We dub this return sequence the ‘overnight drift’ (OD). Figure 3 displays a more granular view of returns around the OD. Here, we see a persistent sequence of positive returns, which are clearly visible in almost every interval between 1:00 and 4:00, showing that the positive average return between 2:00 and 3:00 is not driven by within-the-hour outliers but instead represents a continuous drift over this interval of the overnight trading session.

What is special about this hour? Table II collects opening and closing times for 14 global

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15Our last observation on Fridays is at 18:00. Our first observation on Sunday is at 18:01. Thus the weekend return is incorporated into the first overnight return on Mondays.

16Standard equity futures contract do not give the owner the right to dividend claims.
equity markets, in the local time zone and in corresponding Eastern Time (ET). As U.S. regular trading hours on GLOBEX close, New Zealand, Australia, Japan, Singapore and then China open between 18:00 and 21:30. Day trading in these venues closes between 2:00 and 3:00, at which point Dubai, Russia, London and Europe open. Thus, the OD coincides with the opening of regular trading on Euronext, Eurex, and the Frankfurt Deutsche Börse, as well as pre-market trading on the London Stock Exchange, all occurring at 2:00. This observation highlights the geographical nature of 24-hour trading and provides a first clue towards a potential explanation.

B. Summary statistics

Stacking hourly returns in the vector \( \mathbf{r} \) and denoting by \( D \) a dummy matrix containing appropriately located 0 and 1’s, we estimate the \( 1 \times 24 \) vector of mean log returns \( \mu \) via the projection \( \mathbf{r} = D\mu^\top + \mathbf{\varepsilon} \). Table I reports estimates for \( \mu \) and \( t \)-statistics computed from HAC robust standard errors. We also report \( p \)-values adjusted for multiple testing, medians, standard deviations, skewness and kurtosis estimates.

Consider first panel (a) of table I which collects ON return statistics. Average returns for the hours \{24-01, 01-02, 02-03\} are equal to \{0.46, 0.43, 1.5\} basis points per hour per day (bps) with corresponding \( t \)-statistics equal to \{2.8, 2.8, 7.1\}, respectively. Due to the minimum tick size, median returns computed from quotes are often zero during the night. However, even the median quote return for the OD hour is large and positive equal to 0.64 bps.\(^{17}\) Consider now panel (b) of table I which collects ID return statistics. The opening hour return is strongly negative, equal to -1.2 bps with a \( t \)-statistic of 2.6, and the 17:00 – 18:00 return is equal to -0.43 bps with a \( t \)-statistic of -3.6. The remaining ID returns are flat and statistically indistinguishable from zero.

Within the 24 sub-periods of the day, there is reasonably large variation in average returns across hourly windows. Indeed, while the hours \{24-01, 01-02, 02-03\} are striking in both economic and statistical terms, there are other windows which are statistically significant at the 10% level over the full sample. This is to be expected since we are simultaneously testing more than one null hypothesis, and it is well known that an appropriate significance level such as \( \alpha = 0.05 \) is not valid due to an inflated probability of committing a type I error. We account for the multiple testing

\(^{17}\) The OA reports findings for returns computed from volume weighted average prices (VWAPs) which are very close to returns computed from quotes.
nature of our analysis in two ways.

First, we conduct a bootstrap exercise partitioning the day into 24 hourly sub-periods as in table I. Distributions of test statistics are calculated using a block bootstrap (BS) sampling 10,000 times, with the optimal block length chosen following Patton, Politis, and White (2009). Panel (a) of figure 4 plots the distribution of all hourly returns pooled together while panel (b) plots the distribution of returns during 2:00 – 3:00. Dotted blue lines mark 95% confidence intervals. Black dotted lines represent median estimates for specific hours. Each histogram is normalized such that it represents a probability density function estimate, i.e., the sum of the bar areas is equal to 1. In terms of economic magnitudes the $OD$ return lies well above the upper 97.5% interval. More striking, comparing panel (a) to panel (b), the lower 2.5% BS interval for the distribution of $OD$ estimates lies above the pooled 97.5% interval. Panel (c) repeats this exercise but plotting the distribution of all hourly pooled t-statistics while panel (c) plots the distribution of t-statistics for the $OD$ hour. The conclusion here is the same: the statistical significance of the $OD$ returns is extreme compared to all other hours. Moreover, panels (a) and (c) are clearly bi-model, which is due to unusually large returns realised between 2:00 – 3:00. Making this point clear, panels (e) and (f) compute the equivalent test statistics to panels (a) and (c) after removing 2:00 – 3:00. In these plots the second mode disappears further highlighting the unusual nature of the $OD$ hour.

Second, we account for multiple testing by using the Bonferroni (BF) correction to control the family-wise error (FWER) and the Benjamini-Yekutieli (BY) procedure to control for the false discovery rate (FDR). Accounting for the multiple testing problem, we find that only the $OD$ hour and the 17:00 – 18:00 hour are significant, and this holds for both BF and BY methods. More specifically, using the BF correction the significance level is adjusted to $\alpha/m$ where $m = 24$ hours is the number of tests. At the 5% level, the BF adjusted significance level is $0.05/24 = 0.0021$ and it is $0.01/24 = 0.00042$ at the 1% level. With a $p$-value of $1.1 \cdot 10^{-12}$, the $OD$ hour is extremely statistically significant. The BY method is a ‘step up’ procedure that computes null specific thresholds starting from the least significant hypothesis and working up until significant

\[\text{Insert table I and figure 4 here}\]

\[18\] The FWER is the probability of making one or more type I errors. The FDR is the expected ratio of the number of type I errors to the total number of rejections of the null. Harvey, Liu, and Saretto (2020) provides a recent survey of multiple testing procedures in the context of financial economic applications.

\[19\] We note that between 1998 and 2012 trade was closed between 17:30 – 18:00 and in 2020 the maintenance break was moved to 17:00 – 18:00. In the following we do not further investigate the 17:00 – 18:00 hour as it is of little economic importance. Moreover, this hour is not significant when computing returns from trading prices instead of quotes (see table I in the OA).
alternative hypotheses are detected. The BY thresholds are reported in table A.4 (OA) at the 10%, 5% and 1% levels and shows that the OD hour is the only significant return hour at the 1% level.

In summary, the evidence presented so far demonstrates that 2:00 – 3:00 is a special hour of the day, in both economic and statistical terms, and very far from what one should expect to see just by luck.

C. Subsample Analysis and Persistence

In addition to concerns related to multiple testing one could also be suspicious that the “outperformance” of OD returns compared to other hours were sample specific or a result of data-mining.

A first simple test to address this concern splits the sample in two and recomputes figure 2 which is displayed in figure 5. Panel (a) considers the sample period January 1998 – December 2010 and in panel (b) the sample period is January 2011 – December 2020. One observes that the overall pattern of 24 hour returns across subsamples is quite different. On the one hand, in the first sample opening hour returns are large, negative and significant after accounting for multiple testing using a BF adjustment (blue highlighted bars) but are slightly positive and insignificant in the second sample period. On the other hand, returns between 17:00 – 18:00 are insignificant in the first sample period but become significant in the second sample period. However, both samples share the common characteristic that OD returns are large, positive, and significant at the 5%.\(^{20}\)

\[\text{Insert figure 5 here}\]

Second, a common approach used in the fund management literature to distinguish skill (outperformance) from luck is to study persistence in funds \(\alpha\) (see, e.g., Fama and French, 2021). Analogously, figure 6 displays the cumulative log returns to a $1 initial investment that trades various sub-periods of the day. Panel (a) considers long positions in the hours \(\{24-01, 01-02, 02-03\}\) and panel (b) considers the cumulative returns that go short the opening and 17:00 – 18:00 hours of the day.

A passive CTC investment in e-mini futures (not shown) bears well known business cycle risk, as evidenced by large negative returns in the aftermath of the dot-com bubble, the 2008 financial crisis, and more recently during the early stages of the COVID pandemic.\(^{21}\) By contrast, a $1 investment that holds e-mini futures for only one hour during the OD period would have returned

\(^{20}\)Subsample statistics are reported in the OA.

\(^{21}\)A $1 investment in e-mini futures CTC would have returned $3.8 by December 2020.
2.4 by December 2020 and displays little variation (it is highly persistent). A $1 investment trading either 24:00 – 1:00 or 1:00 – 2:00 would have yielded around half this value implying that the OD accounts for 50% of the total return earned for holding e-mini futures over the extended window 24:00 – 3:00.\textsuperscript{22} Panel (b) reveals that opening hour returns are persistently negative during recessions or states of distress (2000-2003, 2007-2008, 2020) but are otherwise flat. Section B in the OA also shows that opening hour return are only significantly negative on Thursdays and Fridays suggesting they are due to a day of the week effect in bad states of the world. Returns between 17:00 – 18:00, on the other hand, are persistent but are smaller economically; comparable in size to the returns earned between 24:00 – 1:00 and 1:00 – 2:00.

Examine the overnight session further, figure 7 examines average returns year-by-year for the hours \{24-01, 01-02, 02-03\}.\textsuperscript{23} Panel (c) shows that OD returns were positive in 20 out of 23 years. Interestingly, the largest yearly average OD return (10.7% p.a.) occurred in 2020, during the initial year of the COVID pandemic. The OD is slightly negative in the recessionary years of 2002 and 2008, and again in 2019. The bottom panels report (1 − \(p\)) values from t-tests against the null of zero. Panel (e) shows that, at the 10% level, the OD is significant in 17 out of 23 years. Splitting the sample year-by-year highlights the statistical and economic consistency of 2:00 – 3:00 returns compared to 12:00 – 1:00 or 1:00 – 2:00 returns. Indeed, while the two hours that precede the regular opening hours in London are mostly positive, they are much smaller economically and are rarely significant at conventional levels. Moreover, section B in the OA studies these findings along a number of different dimensions and demonstrates that positive statistically significant average returns during 2:00 – 3:00 are a systematic feature of the data, present on all days of the week and 9 out 12 months of the year.

While observing significant positive or negative return hours is certainly interesting, developing a unified explanation for all hours of the day is beyond the scope of this paper. Instead, we will focus on the overnight return patterns straddling the opening of European markets, paying special attention attention to 2:00 – 3:00, which in economic and statistical terms is the salient hour of the day; thus allowing us to test theory driven hypotheses consistently over the entire sample.

\textsuperscript{22}A detailed analysis of investment returns with and without transaction costs is delayed until section V.
\textsuperscript{23}Figure A.5 in the OA reports year-by-year results for the hours 9:00 – 10:00 & 17:00–18:00.
III. Inventory management and price reversals

In the section, we study a potential explanation for the overnight return patterns documented above. To help frame the discussion of the confluence of factors that can explain an asymmetric overnight drift, it is helpful to start from the frictionless benchmark in, for example, Glosten and Milgrom (1985). Glosten and Milgrom (1985) consider the bid and ask price setting problem of a risk-neutral, zero-profit (competitive) market specialist (market maker) and show that, in the absence of any frictions, such as inventory costs and asymmetric information, the bid price equals the ask price and the expected return earned by the market maker is indeed 0. Phenomena like the overnight drift – that is, high frequency price reversals with a non-zero unconditional mean – must thus arise when one or more of the assumptions in the frictionless Glosten and Milgrom (1985) benchmark case are violated.

The first strand of the market microstructure literature relaxes the assumption of no asymmetric information (see e.g. Menkveld, 2016, for an overview). Glosten and Milgrom (1985) show that, when risk-neutral, competitive market makers face informed traders, the optimal bid-ask spread is not zero, and increases in the amount of information present in the market. Thus, for the overnight drift to arise as a result of asymmetric information, news revelation to informed traders has to systematically occur between the U.S. market close and the European market open – so that market makers set a lower bid at U.S. market close and a higher ask at European market opens – and the information revealed overnight has to be positive on average. In the Appendix, we show that the overnight drift cannot be explained by standard information releases, including macroeconomic, monetary policy and earnings announcements, suggesting that overnight information revelation is an unlikely source of the overnight drift.

The second strand of literature focuses on the impact of market maker inventories (see e.g. Stoll, 1978; Amihud and Mendelson, 1980; Ho and Stoll, 1981, 1983; Mildenstein and Schleef, 1983; O’Hara and Oldfield, 1986; Grossman and Miller, 1988; Shen and Starr, 2002) and the costs of maintaining those inventories. This literature finds that, even in the absence of financing constraints on the part of the market makers, market makers that either face non-linear costs (Amihud and Mendelson, 1980; Shen and Starr, 2002) or that are risk-averse (O’Hara and Oldfield, 1986) set bid-ask spreads in a way that reflects their inventory positions. In such models, the setting of the bid and the ask prices depend on both contemporaneous demand and supply and on the future expected value of the
security. Price reversals can thus arise in models of inventory (risk) management due to variation in either order imbalances over time or in expectations of future value of the security (information revelation).

Finally, most recently, the market microstructure literature has studied the link between funding liquidity – that is, how constrained market makers are in funding their inventories – and market liquidity provision. Gromb and Vayanos (2002); Weill (2007); Brunnermeier and Pedersen (2005); Attari, Mello, and Ruckes (2005); Brunnermeier and Pedersen (2009) feature models in which capital-constrained market makers (or market makers with costly capital) undersupply market liquidity, leading to time-variation in market returns due to order imbalances, fundamental information revelation and market maker capital constraints. Given the implausibility of information revelation alone as the source of the overnight drift, in this Section, we focus on the implications of the inventory risk-management based models for market microstructure.

More concretely, consider the following stylized example. News is announced during the U.S. intraday trading session that results in selling pressure at market close. Orders transact at the best available bids and, consequently, execute at successively lower prices down the order book. As the sell-off unfolds, prices drop below fundamental values because risk-averse market makers bear inventory risk. Market makers are compensated for bearing that risk through high expected returns, earned when they offload their excess inventory to new customers arriving overnight.

Grossman and Miller (1988) (GM) provides a framework that models such ‘liquidity events’ through the supply and demand for immediacy. In GM, buyers and sellers arrive at different points in the trading day, which generates transient imbalances between buy and sell volumes. Market makers offer immediacy to incoming traders by absorbing order imbalances and subsequently trading them away. In our context, compensation for bearing inventory risk (a liquidity premium) is earned through expected returns for offloading positions to new customers arriving overnight, i.e., prices drop from $S_0$ to $S_1$ as the market sells off intraday and rebounds from $S_1$ to $S_2$ as trading begins in overseas timezones. Defining the overnight return as $R_{ON} = (S_2 - S_1)/S_1$, conditional expected returns based on date $t = 1$ information are given by

$$E [R_{ON}|\mathcal{F}_1] = \text{Dollar Order Imbalance} \times \frac{\text{Return Variance}}{\text{Risk Bearing Capacity}^{-1}}$$

Models of the GM type provide an intuitive link between liquidity provision, demand for immediacy and price formation. The basic prediction of GM-type models is that the expected returns to
providing immediacy are higher when (1) order imbalances are larger; (2) when payoffs are more uncertain; (3) when the total risk bearing capacity of market makers is lower. In the following, we study our proposed explanation by testing these predictions.

A. End-of-day Volumes

To motivate an inventory management explanation, consider figure 8 which displays intraday and overnight trading volume patterns. To account for an increasing trend in trade over time, for each day we compute the volume in every 5 minute interval weighted by the average volume that occurred in a 5 minute interval on that day. A number above ‘1’ means there is more volume during a given 5 minute interval compared to the daily average and vice-versa for a number below ‘1’.

Panel (a) shows that most trade occurs around the opening and close of the U.S. cash market. Panel (b) zooms in on the overnight session revealing three U-shaped patterns: between 18:00 and 2:00 (Asia), between 2:00 and 3:00 (European opening), and between 3:00 and 8:30 which coincides with scheduled U.S. macro announcements.

Quantifying intraday magnitudes in the recent sample, panels (c) plots average volumes for all hours of the day during 2020. With the index level at 3000 (late May & early June) closing volume in the 5 minute interval 16:10 - 16:15 averaged \(85000 \times 50 \times 3000 \sim 13\) billion USD. By comparison, panel (d) zooms in on the overnight hours showing that volumes are an order of magnitude smaller. Cumulative volumes in the 8 hour period between 18:00 and 3:00 total \(13500 \times 50 \times 3000 \sim 2\) billion USD so that, even in 2020, overnight trading represents a small fraction of the volume in the 5-minute interval preceding the maintenance break.

The key take-away from figure 8 is that there is an economically large downward jump in intraday volume at U.S. close and that overnight trading activity is between 50 to 100 times lower compared to the U.S. trading hours. From an inventory management perspective this makes order imbalances at close particularly risky since the extreme trading volumes leading up to U.S. close at 16.15 can generate large inventory imbalances. Such imbalances cannot be immediately traded away when the overnight session starts at 18:00 because the overnight trading activity is much lower. Moreover, even in recent years, order imbalances can last most of the overnight period and cannot be resolved until European trading begins.

[ Insert figure 8 here ]
B. Volume Time

In the previous section, we showed that returns earned during the OD hour account for the bulk of total overnight returns and argued that this pattern is inconsistent with returns accruing linearly over time. Instead, the high returns earned during the OD hour is in line with the basic idea of GM-style models, which imply that, conditional on an order imbalance, prices revert as new participants arrive and market makers offload their inventories. In clock-time, the speed of mean reversion depends on the volume of new participants because market makers cannot manage inventory imbalances when trading activity is low. Conversely, when trading activity is high, markets markers can offload quickly.

In this context, a natural alternative to clock time is to measure time elapsed in terms of the trading volume as first proposed by Mandelbrot and Taylor (1967). Specifically, we consider volume time, which advances one increment for every contract traded and thus equals cumulative trading volume. Volume time is a type of activity time, like tick time, advancing slowly when few contracts are traded (Asian hours) and quickly when many contracts are traded (U.S. hours). By definition, trade activity is constant in volume time and we therefore expect order imbalances to revert linearly to zero in volume time. Thus, we also expect price reversals induced by inventory management to be linear when measured in volume time.

From the perspective of inventory risk models, the empirical measure of order imbalance would be net inventory held by market makers. As these are not observable, we proxy for them from signed volume defined as

\[ SV_{i}^{t} = \#\text{buy orders} - \#\text{sell orders}, \]

where \# of orders is defined as the number of contracts, \( t \) is the day, and \( i \) is the period during the day. Note that \( SV_{i}^{t} \) is measured in dollar units consistent with equation 2, and the sample period is 2007–2020 since total volume was relatively stationary during this period (see figure 1). Table A.7 of the OA shows the intraday properties of \( SV_{i}^{t} \) while panels (a) and (b) of figure A.6 show the distribution and time series of \( SV_{i}^{t} \) at U.S. close.

Figure 9 displays cumulative log returns (computed from VWAPS) and cumulative signed volume in both clock time and volume time, sorted by \( SV_{i}^{\text{close}} \), which is the signed volume measured in the

\(^{24}\)Mandelbrot and Taylor (1967) argue that price changes follow a Pareto distribution in clock time but are normally distributed in volume time. This result was later generalized by Ané and Geman (2000). More recently, Kyle and Obizhaeva (2016) propose and test “market microstructure invariance”, which states that the distributions of risk transfers and transaction costs are constant across assets when measured in business-time (activity time).
last hour before the maintenance break between 15:15–16:15. Panel (a) and (c) are in clock time and we clearly see that price reversals are strongest at the opening of Asian (19:00 and 20:00) and European markets (2:00 and 3:00 ET) when volume jumps up, and that returns quickly flatten off after the initial hours of European trade. Panel (b) and (d) are in volume time. Following negative (positive) closing order imbalances, both signed volume and returns increase (decrease) essentially monotonically. Following market sell-offs, most of the overnight return is earned by the point 60,000 contracts are traded, or in other words, around the time when European markets open.

Corresponding positive closing order imbalances generate a smaller price impact than negative closing order imbalances, even if order flow is quite symmetric following positive versus negative end-of-day imbalances. Thus, viewed from the perspective of volume time, we observe an almost linear but asymmetric demand shock response throughout Asian and European hours.

[ Insert figure 9 here ]

C. Economic Magnitudes

Next, we evaluate the quantitative plausibility of an inventory risk hypothesis. From the data, we can observe three of the four terms that enter equation 2: the expected overnight returns $E[R_{ON}|\mathcal{F}_1]$, the end-of-day dollar order imbalance, and the (conditional) return variance. The final component – the risk-bearing capacity of the market is harder to observe directly. Instead, we note that the risk bearing capacity can be expressed as $\text{Risk Bearing Capacity} = \frac{N+1}{ARA}$ where $N$ is the number of market makers providing immediacy and $ARA$ is absolute risk aversion common across market makers. Recall further that the coefficient of relative risk aversion (RRA) is approximately the $ARA$ multiplied by wealth, which allows us to re-cast equation 2 as a prediction for the RRA of the market makers in this market

$$\text{RRA} = \frac{E[R_{ON}|\mathcal{F}_1]}{\text{Dollar Order Imbalance} \times \text{Return Variance}} \times \text{Wealth} \quad (4)$$

where $\text{Wealth}$ denotes total capital of the market makers, $(N + 1) \times \text{Wealth}_i$, that is allocated to supporting equity market trades. While market participants’ capital allocations to particular trades are notoriously hard to measure, we can follow the literature on financial intermediation (see e.g. Adrian and Shin, 2014b) by proxying for $\text{Wealth}$ and proxy with the equity value-at-risk (VaR) of
large dealers. The total equity VaR of large dealers proxies for how much capital is at risk for these intermediaries when they provide liquidity in equity markets, and is thus closely related to the total risk bearing capacity of market makers in the market.

We obtain the quarterly time series of average broker-dealer equity VaR from Bloomberg in order to perform a proxy calculation of implied market maker $RRA$. Figure A.9 in the OA shows the time-series of equity VaR varies between 50 and 750 billion USD between 2000.Q1 and 2020.Q4, peaking in the financial crisis and rising again during the COVID-19 crisis. Average equity VaR during the sample period 2007Q1 – 2020Q4 was equal to 300 billion USD, which we take as our proxy for $\text{Wealth}$. Then, from panel (b) of figure 9, we take the realized overnight return, measured in volume time, equal to $\sim 17\%$ p.a. as a proxy for expected overnight returns conditional on a market sell-off. From panel (d) of figure 9 we obtain the corresponding resolved overnight market maker imbalance of $\sim 1500$ contracts that, with the index level at 2000, equates to a dollar imbalance of $1500 \times 50 \times 2000 = 150$ billion USD. We measure $\frac{\text{Return Variance}}{\text{VIX}^2}$ as the unconditional level of the $\text{VIX}^2$ in our sample, which was $20\%^2$. The implied market maker relative risk aversion is therefore

$$RRA = \frac{0.17}{150 \times 0.04} \times 300 = 8.5$$

(5)

To put this estimate in context, Greenwood and Vayanos (2014) perform a similar conversion of Treasury arbitrageurs’ ARA to RRA to estimate a range of $[7.6, 91.2]$ for the RRA. For mortgage backed security arbitrageurs Malkhozov, Mueller, Vedolin, and Venter (2016) perform a similar calculation coming up with an estimate of 88. Our ‘back-of-the-envelope’ calculation suggests that, not only is an inventory risk explanation plausible from a qualitative perspective, but also from a quantitative one.

25At the end of 2020, the five largest dealer banks were Bank of America, Citibank, JP Morgan, Goldman Sachs, and Morgan Stanley. As in Adrian and Shin (2014a), for firms which report VaRs at the 95% confidence level, we scale the VaR to the 99% using the Gaussian assumption.

26We discuss in the OA the assumptions behind using equity value-at-risk as a proxy for dealer capital committed to equity futures trades.

27Prior empirical literature has also studied the plausibility of inventory risk explanations though in more limited settings. Madhavan and Smidt (1993); Hansch, Naik, and Viswanathan (1998); Ready, Roussanov, and Ward (2013); Naik and Yadav (2003) find, in small samples of intraday data, that market makers control risk by mean-reverting their inventory positions toward target levels. Using 11 years of daily data on NYSE specialist inventory positions and trading revenue, Comerton-Forde, Hendershott, Jones, Moulton, and Seasholes (2010) test directly for the relationship between funding and market liquidity and find that both aggregate market-level and specialist firm-level spreads widen when specialists have large positions or lose money. They further document that, consistent with models of time-varying risk-bearing capacity, these effects are non-linear.
D. End-of-day Order Imbalance

We now study in more detail the prediction of GM-type models which states that returns for providing immediacy should be higher when order imbalances are larger. In order to exploit as much data as possible, and following much of the empirical literature, our main proxy for order imbalance in the remaining is relative signed volume, measured as signed volume over total volume

\[ RSV_t^i = \frac{SV_t^i}{TV_t^i} \in [-1, 1], \]  

(6) 

where \( TV_t^i = \# \text{buy orders} + \# \text{sell orders} \) accounts for the increasing trend in total trading volume over the sample 1998–2020.28

Table III reports summary statistics for hourly \( RSV_t \). On average, close-to-close \( RSV_t \) is equal to \(-2.4\%\) and is highly volatile. Negative CTC \( RSV_t \)'s are consistent with the idea that the futures market is traded as a hedging instrument for the underlying. However, while \( RSV_t \)'s are negative during the day, they are largely positive between 1:00 – 4:00. During the OD hour, average \( RSV_t \) is 2.4% with a t-statistic of 6.7, mirroring the unconditional positive returns during this hour. In the following, we use the last hour preceding the maintenance (15:15 – 16:15) to measure closing order imbalance, which we denote \( RSV_t^{\text{close}} \).29

[ Insert table III here ]

Figure 10 sorts all trading days into groups based on closing imbalances. For each group panel (a) reports returns during Asian hours (18:00 – 1:00), (b) reports returns during EU open (1:00 – 04:00), panels (c) & (d) report returns during the OD hour (2:00 – 3:00). The sorting is performed such that the groups are approximately equal in size and black bars indicate 95% confidence intervals.30

Summarising, figure 10 shows that (i) order imbalances at U.S. close are followed by overnight price reversals as predicted by inventory models; and (ii) price reversals are much stronger following market sell-offs giving rise to an unconditional positive overnight drift.

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28In the OA, we present counterparts to all of the results that follow using \( SV_t \) as alternative measure of imbalance (for the sample 2007–2020 as above). The results are quantitatively similar using either measure and thus robust to whether we standardize by volume or not.

29Panel (c) and (d) of figure A.6 show the distribution and time series of \( RSV_t \) at U.S. close. \( RSV_t^{\text{close}} \) is stationary around zero throughout the sample period and its variance is stable.

30Note that \( RSV_t^{\text{close}} \) is defined as buys minus sells so that a negative imbalance implies dealers are long and from equation 2 overnight expected returns should therefore be positive.
Using $RSV_t^{close}$ as a sorting variable the conditional return pattern resembles a step function centered around zero. Figure A.7 in the OA shows that, when sorting on $SV_t^{close}$, the conditional return pattern is monotonic, albeit with an asymmetric slope. More importantly, in both cases, negative closing imbalances generate statistically significant positive overnight returns.

[ Insert figure 10 here ]

Equation 2 contains an additional intuitive prediction that order imbalances close to zero should have little price impact. Indeed, market makers should not require liquidity premium for holding zero inventory. Panel (d) examines this prediction by zooming in on $OD$ returns based on $RSV_t^{close}$ straddling zero. Consistent with an inventory channel, when closing imbalances are approximately zero we find reversal returns which are economically small and statistically indistinguishable from zero.

E. Volatility risk

The second prediction of equation 2 is that expected overnight returns are increasing in the return variance of the risky asset. This is because risk-averse market makers demand a higher premium for holding larger price risk. To allow for differential effects on volatility due to demand shock asymmetry, we split the sample into positive and negative closing order imbalance days and then construct double sorts – based on terciles of $RSV_t^{close}$ and volatility – within each sub-sample. Panel a (panel b) of table IV reports double sorts conditional on negative (positive) $RSV_t^{close}$ days. Double sorted return averages are reported based on terciles of $RSV_t^{close}$ and the closing level of the VIX sampled at 16:15 each day.\footnote{Tick-by-tick quotes for the VIX index are sourced from Refinitiv and complemented with data from CBOE.} Within each set, we also report average $RSV_t^{close}$ and VIX levels ($A_1, A_2, B_1, B_2$). Double sorted $OD$ return averages are reported ($A_3, B_3$) along with high minus low differences and p-values testing the difference against zero.

We first note that the distribution of $EOD$ VIX appears quite symmetric conditional on positive versus negative $RSV_t^{close}$ days. Thus, it is unlikely that asymmetric price impact is due to a correlation between order imbalance and the level of asset return variance.\footnote{While changes in the VIX are highly negatively correlated with returns, the correlation between the level of the VIX and returns (order imbalance) is quite low.} Considering panel (a) (positive $RSV_t^{close}$) there is really no clear pattern is $3 \times 3$ sorted $OD$ return averages. Panel (b) (negative $RSV_t^{close}$) on the other hand is consistent with our priors from equation 2: (i) Conditional
on the level of the VIX, moving from low to high $RSV_{t}^{\text{close}}$ states, the $OD$ return averages are increasing. (ii) Conditional on the level of the $RSV_{t}^{\text{close}}$, moving from low to high $RSV_{t}^{\text{close}}$ states, the $OD$ return averages are also increasing. The only exception is in high VIX states where the impact of $RSV_{t}^{\text{close}}$ is large but flat. Moreover, the high-minus-low return spreads are in the anticipated direction and statistically significant in 5 out of 6 cases. Thus, as predicted by GM-style models, price reversals are larger following days with large end-of-day order imbalances and even more so if the large order imbalances coincide with periods of heightened uncertainty.

[ Insert table IV here ]

\(F. \quad \text{Demand Shock Asymmetry}\)

Consistent with the literature on downward sloping demand curves and imperfect liquidity provision, we have shown that demand shocks have a temporary price impact that reverts over time. However, we have also shown a strong asymmetry in price impact in response to positive versus negative demand shocks. This asymmetry generates a positive unconditional overnight return which in \textit{clock} time is concentrated in the hour from 2:00 – 3:00 (the \textit{OD}). In Section III.B we then showed that re-cast in \textit{volume} time, that demand shock asymmetry is a more general feature of the data observable throughout Asian and European hours.

To the best of our knowledge, such an asymmetry is novel to the literature. Now, recall from 2 that the conditional expected return to providing immediacy is the product of three terms: the end-of-day order imbalance, conditional variance of returns, and the inverse of the risk-bearing capacity of the market makers. Table IV shows that the first two terms are unlikely to contribute to the asymmetric response to positive and negative demand shocks: the distribution of demand shocks around ‘0’ is roughly symmetric and the distribution of the VIX conditional on the sign of the demand shock is roughly similar. Instead, the asymmetric response to positive and negative demand shocks may be driven by contemporaneous changes in the risk-bearing capacity of the market makers. This may arise through two different channels.

First, since there are no designated market makers for e-mini contracts, there is no obligation on the part of institutions that normally act as market makers to continue doing so in the face of large sell-offs. That is, during large sell-offs, institutions that act as market makers may choose to exit the market, reducing the total risk-bearing capacity of the market maker segment.
Second, those market makers that choose to remain during large sell-offs may reduce their individual risk limits in response to deteriorating market conditions. Section A.3 in the OA outlines how increases in volatility, which accompany market sell-offs, may translate into higher effective risk aversion when market makers face value-at-risk (VaR) constraints. Increases in volatility tighten the VaR constraint for market makers, translating into higher effective risk aversion. Conversely, decreases in volatility do not translate into lower effective risk aversion once the VaR constraint is no longer binding. Thus, an asymmetry in the pass through of positive versus negative volatility shocks can generate an asymmetry in return reversals following demand shocks.

Third, market makers may face an asymmetry in funding costs as in Brunnermeier and Pedersen (2009) who argue that decreases in risk-bearing capacity arise when market liquidity and funding liquidity interact in flight-to-quality episodes, with capital required for trading evaporating when market returns are negative. Indeed, during prolonged periods of market sell-offs, the CME increases the required initial margins for futures positions.

Each of these mechanisms may contribute to time-variation in effective risk aversion; we leave further investigation of return reversal asymmetry for future research.

IV. High frequency return predictability

Section II documented our central empirical finding and section III adopted a sorting based approach to test our explanation. In this section, we study further the link between overnight expected returns and EOD order imbalances within a high frequency predictability framework.

A. High Frequency Predictability and Order Imbalance

Panel (a) of table V reports point estimates from univariate regressions of hourly realised returns during the overnight session (18:00 – 6:00) on closing imbalances:

\[ r_{t,n}^H = \mu_n + \beta_{n}^{RSV} RSV_{t-1}^{close} + \epsilon_{t,n}, \text{ for } n = 1, \ldots, 12, \]  

(7)

together with \( t \)-statistics computed from robust standard errors clustered within each month. Returns are measured in basis points, and \( RSV_{t-1}^{close} \in [-1, 1] \). Thus, a point estimate of \( \beta_{n}^{RSV} = -10 \) implies a +1 basis point return response to a closing imbalance of \( RSV_{t-1}^{close} = -10\% \).

Consistent with an explanation based on inventory risk, we observe a strong negative relation
between the closing order imbalance and returns. The relation is strongest between 2:00 – 4:00. The estimates are both economically and statistically significant. A 1-standard deviation (6.55%) decrease in $R{SV}_{t-1}^{close}$ (a sell-off) induces a $6.55\% \cdot -17.49 = 1.15$ basis point increase in returns between 2:00 – 3:00. We also observe a statistically significant negative relationship between 20:00 – 21:00, corresponding to the opening of Japanese (TSE) and Australian (ASX) markets.

In panel (b) of Table V, we verify that order imbalance in the last hour of the U.S. trading day is the appropriate proxy for dealer inventory imbalances. We include order imbalances measured in the final three hours of the trading day (13:15–14:15, 14:15 – 15:15, and 15:15 – 16:15) as separate regressors in a multivariate extension to equation 7. Given the high levels of trading activity during U.S. open hours, we expect order imbalances from earlier in the day to have been traded away prior to the end of the trading day and thus have no impact on overnight returns. This is indeed what is suggested by the estimates in Table V. For example, focusing on the 2:00 – 3:00 interval, the point estimates monotonically decline the earlier in the day the order imbalance is measured and are insignificant beyond 14:15.

[ Insert table V here]

B. Falsification Test

Microstructure theory predicts a link between order imbalance and returns, both contemporaneously and at lagged intervals. In inventory management models, high-frequency predictability arises as market makers adjust their quotes to resolve imbalances. The more liquid a market is, the shorter the period of predictability will be because market makers can quickly trade imbalances away. In illiquid markets such as corporate bonds predictability can last several days. Microstructure theory also predicts negative autocorrelation in returns due to a host market frictions and, indeed we do observe negatively autocorrelated returns for the e-mini but the generally large liquidity of the market implies autocorrelation coefficients only are significant for, at most, 30 minutes.\textsuperscript{33} However, the closing of U.S. trading hours is a special point in the trading day because volume is extremely high relative to the subsequent trading hours.

Our proposed explanation relies on a special relationship between closing order imbalance and returns around European open. Table VI provides a ‘falsification’ test for this claim. For the

\textsuperscript{33}See figure A.8 in the OA.
overnight hours, panel (a) estimates univariate regressions of hourly returns on one hour lagged $RSV_t$. There is only one significant hour between 23:00 – 24:00 and the sign is positive not negative.

Panel (b) extends the regression to include the previous 12 lagged hours of $RSV_t$ for the night hours. Most of the point estimates in the table are insignificant. However, focusing on the highlighted purple diagonal estimates we find economically large and statistically significant return predictability arising from order imbalances at close of regular U.S. trading hours. More specifically, the point estimates are large at exactly the opening of Tokyo and European regular market opening times, even after controlling for all imbalances subsequent to U.S. close.

[ Insert table VI here ]

C. Demand Asymmetry and Volatility Risk

The sorting based approach of the previous section revealed a strong asymmetry in price impact in response to positive vs. negative demand shocks, which generates an unconditional positive overnight drift return (reversal). Panel (a) of table VII explores the asymmetry in a regression design that interacts $RSV_{t,close}$ with a dummy variable that takes on a value of ‘1’ if $RSV_{t-1,close} < 0$ and ‘0’ otherwise

$$r_{t,n}^H = \mu_n + \beta_n^{RSV} RSV_{t-1,close} + \beta_n^{NEG} \mathbb{1}_{NEG,t} + \beta_n^{RSV\times NEG} RSV_{t-1,close} \times \mathbb{1}_{NEG,t} + \varepsilon_{t,n} \quad n = 1, \ldots, 12.$$  

We find that the dummy variable is large and statistically significant during only the OD hour.

We also investigate the standard inventory risk prediction that price reversals should be amplified in states of high volatility. Testing this, we interact $RSV_{t,close}$ with the level of the VIX index sampled at 16:15 ET

$$r_{t,n}^H = \mu_n + \beta_n^{RSV} RSV_{t-1,close} + \beta_n^{VIX} VIX_{t-1,close} + \beta_n^{RSV\times VIX} RSV_{t-1,close} \times VIX_{t-1,close} + \varepsilon_{t,n} \quad (8)$$

for $n = 1, \ldots, 12$. Panel (b) of Table VII reports the estimates, showing that ex-ante volatility has a strong amplification effect on the relationship between order imbalance and overnight returns between 2:00 – 3:00. A 1-standard deviation decrease in $RSV_{t-1,close}$ when $VIX_{t-1,close} = 20\%$ (the average VIX level throughout the sample period is 19.8\%) generates a return response of $66.39 \times (-6.55\%) - 5.33 \times (-6.55\%) \times 20 = 2.6$ basis points. With the VIX at its 90th percentile (30\%)
the return response is 6.1 basis points and with the VIX at its 10th percentile (12 \%) there is close to zero effect.

[ Insert table VII here]  

D. Daylight savings tests  

The results so far highlight that large negative order imbalances at the end of the U.S. trading are subsequently resolved during the overnight trading session, as new customers arrive into the market. The 24-hour nature of the e-mini market allows us to provide additional evidence on this explanation by conducting a novel test that exploits exogenous variation, from the perspective of U.S.-based market makers, in the arrival time of Asia-based clients. Specifically, we exploit the fact that while both U.S. and Europe observe daylight savings time (DST), Japan does not. From the perspective of U.S.-based market makers, clients based in Japan arrive at 19:00 during U.S. winter months (DST off) and at 20:00 during U.S. summer months (DST on). Thus, DST changes represent exogenous variation in the arrival time of Japan-based clients.

Figure 11 shows that, during the second half of our sample (January 2007 – December 2020), when the trading volume during Asian opening hours is non-negligible, there is a spike in e-mini trading volume at 21:00 when DST is not active (red line) which is exactly at the opening of the Tokyo stock exchange (TSE). When DST is active, the increase in volume occurs instead at 20:00, which again corresponds to the opening of TSE in the U.S. summer. Notice, also, a secondary spike in trading volume at 22:30 when the TSE re-opens after its lunch break during U.S. winter months and at 23:30 when the TSE re-opens after the lunch break during the U.S. summer months.\(^{34}\)

[ Insert figure 11 here ]

We now test more formally whether changes in the arrival time of Asia-based clients translates into a change in the timing of overnight returns. Panel (a) of table VIII reports the estimated coefficients from a regression of hourly overnight returns between 18:00 – 23:00, measured in basis points, on order flow imbalance at the end of the preceding trading day, a dummy for U.S. DST, and an interaction between the two

\[
\hat{\tau}_{t,n} = \mu_n + \beta_{RSV}^{n} RSV_{t-1,close} + \beta_{DST}^{n} \text{1}_{DST,t} + \beta_{RSV \times DST}^{n} RSV_{t-1,close} \times \text{1}_{DST,t} + \varepsilon_{t,n} \tag{9}
\]

\(^{34}\)For an in-depth discussion of the TSE lunch break and its effects on trading on the NIKKEI, see Lucca and Shachar (2014).
for $n = 1, \ldots, 12$, where the dummy variable takes on a value of 1 in summer time (DST active) and 0 in winter time (DST not active), with daylight savings seen from a U.S. perspective. The sample period is 1998.1 – 2020.12.

Consistent with the hypothesis that DST creates exogenous variation in the arrival time of Asia-based clients, we see that the effect of $RSV$ moves forward by one hour when the U.S. goes from winter to summer time. To see this, consider first U.S. winter time where the DST dummy equals 0. Here, Australia opens at 18:00, TSE opens at 19:00, and Singapore opens at 20:00 (also, Shanghai opens at 20:15 and Hong Kong opens at 20:30). As expected, the effect of $RSV$ negative in hours with market openings where new agents arrive. specifically, $\beta_{RSV}^n = \{-9.34; -13.46; -6.70\}$ for the hours 18:00 – 19:00, 19 – 20:00 and 20:00 – 21:00.

Next, in U.S. summer time, where the DST dummy equals 1, there are no major market openings at 18:00, TSE opens at 20:00, Australia opens at 19:00 or 20:00, and Singapore opens at 21:00.35 Now, we find the effect of $RSV$ by summing $\beta_{RSV}^n + \beta_{RSV \times DST}^n = \{1.43; -1.43; -6.85\}$ and, indeed, we see that the effect of $RSV$ shifts in accordance with DST.

We can likewise exploit the fact that DST is observed both in Europe and the U.S. The standard time difference between New York and London is five hours but throughout our sample period the U.S. and Europe have switched to DST at different times, typically 1 week apart. Panel (b) of table VIII reports estimates of hourly overnight returns between 24:00 – 5:00 regressed on closing signed volume and a time difference dummy:

$$r_{t,n}^H = \mu_n + \beta_{RSV}^n RSV_{t-1}^{close} + \beta_{DIFF}^n \mathbb{1}_{DIFF,t} + \beta_{RSV \times DIFF}^n RSV_{t-1,close} \times \mathbb{1}_{DIFF,t} + \epsilon_{t,n} \quad n = 1, \ldots, 12,$$

where the dummy variable takes on a value of ‘0’ when the time difference between London and New York is 5 hours and a value of ‘1’ when the time difference is 4 hours. We find that the predictability of $RSV$ disappear in the hour 2:00 – 3:00 on days where the U.S. - EU time difference only is four hours. Predictability due to an overnight return reversal shifts by two hours to 4:00 – 5:00, which is the first hour of regular trading in London and Frankfurt when the U.S. - EU time difference is 4 hours. We note that there are less than 300 trading days here; thus, the point estimate is not well measured. However, the main takeaway of the European daylight savings test remains: when the U.S. and Europe are out of their usual 5 hour time-difference synchronization, consistent with idea

\footnote{Australia does not switch to winter (summer) time at exactly the same date where the U.S. switches to summer (winter) time. Therefore, seen from a U.S. perspective, Australia opens at 19:00 for short periods during the spring and fall.}
that liquidity traders are no longer entering the market at this time, predictability during the OD hour disappears.

[ Insert table VIII here ]

V. Trading overnight reversals

We conclude the paper by considering a set of trading strategies designed to exploit overnight price reversals, with and without transaction costs, and in doing so implicitly study how market makers set liquidity premiums in response to inventory shocks. The trading strategies we consider are stylized examples that expose an investor to holding the ES contract for a sub-period of each trading day compared to passively holding the ES contract. Returns on trading day \( j \) earned on a strategy that goes long the ES contract in the sub-period \([t_1, t_2]\) are computed as

\[
R^L_{j,[t_1,t_2]} = \frac{P_{j,t_2} - P_{j,t_1}}{P_{j,t_1}},
\]

(10)

where \( P \) denotes price of the ES contract. The analogous short position earns \( R^S = -R^L \). Mid quotes are used to compute returns excluding transaction costs. Transaction costs are incorporated from bid-ask quotes in Refinitiv data and returns are computed from quotes as

\[
R^L_{j,[t_1,t_2]} = \frac{P_{\text{bid},j,t_2} - P_{\text{ask},j,t_1}}{P_{\text{ask},j,t_1}} , \quad R^S_{j,[t_1,t_2]} = -1 \times \frac{P_{\text{ask},j,t_2} - P_{\text{bid},j,t_1}}{P_{\text{bid},j,t_1}} .
\]

(11)

We consider the following strategies:

- long CTC: \( t_1=16:15 \rightarrow t_2 = 16:15; \)
- long CTO: \( t_1 = 16:15 \rightarrow t_2 = 9:30; \)
- long OTC: \( t_1 = 9:30 \rightarrow t_2 = 16:15; \)
- long OD: \( t_1 = 2:00 \rightarrow t_2 = 3:00; \)
- long OD+: \( t_1 = 1:30 \rightarrow t_2 = 3:30 \)

We also consider a conditional trading strategy that ‘buys-the-dip’, denoted BtD, which holds the e-mini during the OD+ period but only on trading days following a negative order flow at market close \( RSV_{i-1}^{\text{close}} < 0 \). We report findings for the sample period 2004.1 — 2020.12, as after this point the bid-ask spread during the overnight period reached its minimum tick size (see figure A.13).
Table IX (a) reports summary statistics of the trading strategies when transaction costs are excluded. Holding the ES contract continuously (the CTC strategy) since 2004.1 has yielded an average yearly return of 8.9% with a Sharpe ratio of 0.42.\textsuperscript{36} The beta is equal to 1 by definition as we use the CTC return as a proxy for the market return. CTO and OTC returns contributed an approximately equal proportion to the total return earned by a passive investor holding the index: On an annualized basis, CTO returns averaged 4.6% and OTC returns averaged 4.2%. A dissection of this magnitude is not particularly surprising in itself. However, it is surprising that OD return component is comparable in size to the CTO and OTC returns, equal to 3.8% on average. The OD strategy has a Sharpe ratio of 1.1, which outperforms the market Sharpe ratio, and arises from a combination of high excess returns and low volatility during the overnight drift period. The best performing strategy is the conditional versions of OD+ which holds the e-mini on \( \sim 50\% \) of trading days. Returns from trading the BtD strategy are considerably larger than OD+ returns, which we interpret as additional evidence in support of the inventory risk prediction that past RSV should predict subsequently higher expected returns, as new agents arrive to market and liquidity suppliers offload their long positions. In addition to larger returns, the BtD strategy return variance is significantly lower and thereby the Sharpe ratio higher. Specifically, \( RSV_{t-1} < 0 \) has a Sharpe ratio of 1.8 compared to 1.3 of OD+.\textsuperscript{37}

Table IX (b) reports summary statistics post transaction costs. Returns on all simple strategies are significantly lower and only the OD+ strategy has a positive Sharpe ratio. However, the BtD strategy remains highly profitable (Sharpe ratio of 1.1) because it only pays the bid-ask spread on half the trading days when returns are higher. This is exactly what we would expect from an inventory management perspective. Market makers earn the bid-ask spread, buying at the bid on negative closing RSV days and selling at the ask during the overnight trading session. In general, market makers position their limit order books to incentivize trades that bring their inventory closer to their targets, making a contrarian trade – where a client would earn the bid-ask spread – less profitable.

It is important to highlight that small yet persistent intraday return seasonalities can have large low frequency effects. To illustrate this point, figure 12 depicts the cumulative returns of the CTC, OD, OD+ and BtD strategies for a one dollar investment in January 2004. The overnight

\textsuperscript{36}Sharpe ratios are computed from daily risk free rates implied by 4 week U.S. Treasury bills obtained from CRSP. Return volatilities (the denominator of the Sharpe ratio) are computed using daily data.

\textsuperscript{37}The large number of zero returns is also what causes the large kurtosis. The positive skewness of BtD occurs because the RSV < 0 signal filters a significant fraction of the negative returns.
strategies have performed exceptionally well in the sense that they never experience large negative returns. Remarkably, the BtD strategy has positive returns during the financial crises even though the strategy never shorts the market. Panel (a) displays returns for a hypothetical investor who trades without costs. Trading the $OD$ ($OD+$), a one dollar initial investment in 2004 generated a portfolio value of $1.9$ ($2.8$) in December 2020. Panel (b) of figure 12 displays cumulative returns including transaction costs. The $CTC$ return remains unchanged as it is a passive strategy (we only have to roll the contract at a quarterly basis and pay for the spread between the initial buy in 2004 and final sell in 2020). With transaction costs, the $OD$ is not profitable in practice. However, the BtD strategy earns large positive returns, generating a portfolio value of $1.9$ and while it does not beat a passive position in the market, it has a significantly higher Sharpe ratio and does not experience large losses related to the business cycle.

[Insert table IX and figure 12 here]

VI. Conclusion

In this paper, we study returns to holding U.S. equity futures around the clock and document a large positive drift in returns accruing during the opening hours of European market regular trading hours.

We argue that the large positive drift in returns is consistent with standard theories of demand for immediacy and the associated liquidity provision by risk-averse market makers. Consistent with such theories, we show that overnight returns have a strong relationship with (U.S.) end-of-day order imbalances, and that the relationship is asymmetric: while large negative order imbalances at the end of the U.S. trading day are followed by large return reversals overnight, the response to large positive end-of-day order imbalances is muted. This asymmetry in return reversals following negative and positive order imbalance days is what generates the unconditionally positive returns around European opening times. We conjecture that the asymmetry in return reversals arise due to time-varying risk bearing capacity of market makers in this market, which decreases during periods of large market sell-offs. Finally, we show that the demand for immediacy hypothesis is not only qualitatively consistent with the return and order flow patterns in the data but also provides a quantitatively-plausible explanation for the overnight drift.
References


Bondarenko, Oleg, and Dmitriy Muravyev, 2020, Market Return Around the Clock: A Puzzle, SSRN Abstract 3596245.


Cliff, Michael, Michael Cooper, and Huseyin Gulen, 2008, Return differences between trading and non-trading hours: Like night and day, *Working paper*.


VII. Tables

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(a) Overnight
(b) Intraday

Table I. Summary statistics: hourly returns around the clock

Summary statistics for S&P 500 e-mini futures hourly log returns. Returns are computed from mid quotes at the top of the order book and reported in basis points. Panel (a) displays overnight hours and panel (b) displays intraday hours. Mean, medians and standard deviations are displayed in basis point terms. t-statistics testing again the null of zero returns are computed from HAC robust standard errors. p-values indicate significance levels under a student-t distribution. Sample period is January 1998 — December 2020.
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Table II. Open and closing times of global equity cash indices
The table displays opening and closing times for 14 global equity markets, in the local
time zone and in corresponding Eastern Time Zone (ET) for June, 2018. The abbrevia-
tions are NYSE=New York Stock Exchange, TSE=Tokyo Stock Exchange, LSE=London Stock Exchange, HKE=Hong Kong Stock Exchange, NSE=National Stock Exchange of India, BMF=Bovespa Bolsa de Valores Mercadorias & Futuros de Sao Paulo, ASX=Australian Securities Exchange, FWB=Frankfurt Stock Exchange Deutsche Börse, RTS=Russian Trading System, JSE=Johannesburg Stock Exchange, DIFX=NASDAQ Dubai, SSE=Shanghai Stock Exchange, SGX=Singapore Exchange, NZSX=New Zealand Stock Exchange, TSX=Toronto Stock Exchange. Opening and closing times are collected from the public website of each exchange. * Denotes locations that do not observe Daylight Savings Time (DST). Relative to the table, the time difference is plus 1 hour outside the U.S. DST period. ** Denotes locations south of equator that do observe DST. Relative to the table, the time difference is plus 2 hours when outside the U.S. DST period and in the DST period of the given region.
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<td>−0.39</td>
<td>−0.21</td>
<td>−0.48</td>
<td>−0.36</td>
<td>0.03</td>
<td>0.81</td>
<td>−1.00</td>
<td>−2.36</td>
</tr>
<tr>
<td>t-stat</td>
<td>−5.74</td>
<td>−5.75</td>
<td>−4.21</td>
<td>−1.92</td>
<td>−4.32</td>
<td>−3.36</td>
<td>0.33</td>
<td>6.12</td>
<td>−2.80</td>
<td>−1.14</td>
</tr>
<tr>
<td>Median</td>
<td>−0.50</td>
<td>−0.39</td>
<td>−0.28</td>
<td>−0.21</td>
<td>−0.38</td>
<td>−0.42</td>
<td>−0.03</td>
<td>0.78</td>
<td>−1.68</td>
<td>−0.91</td>
</tr>
<tr>
<td>Sdev</td>
<td>6.04</td>
<td>5.80</td>
<td>7.00</td>
<td>8.22</td>
<td>8.48</td>
<td>8.28</td>
<td>7.20</td>
<td>9.97</td>
<td>46.71</td>
<td>136.19</td>
</tr>
<tr>
<td>Skew</td>
<td>−0.54</td>
<td>−0.33</td>
<td>0.35</td>
<td>0.31</td>
<td>0.22</td>
<td>1.53</td>
<td>0.50</td>
<td>0.23</td>
<td>0.04</td>
<td>−0.12</td>
</tr>
<tr>
<td>Kurt</td>
<td>16.83</td>
<td>8.31</td>
<td>7.85</td>
<td>7.69</td>
<td>7.00</td>
<td>21.40</td>
<td>9.97</td>
<td>12.03</td>
<td>3.52</td>
<td>4.00</td>
</tr>
</tbody>
</table>

### (c) EOD

#### Table III. Summary statistics: relative signed volume around the clock

Summary statistics for S&P 500 e-mini futures hourly relative signed volume defined as

\[
RSV_t = \frac{\# buy\ orders - \# sell\ orders}{\# buy\ orders + \# sell\ orders} \in [-100\%, 100\%],
\]

which states order imbalance relative to total volume in percentages. Panel (a) displays overnight hours and panel (b) displays intraday hours. Panel (c) displays \( RSV_t \) in quarterly intervals between 15:00 – 16:15 and in the final column reports summary statistics for \( RSV_t^{\text{close}} \) which is relative signed volume measured between 15:15 – 16:15. Mean, medians and standard deviations are displayed in percentages. Sample period is January 1998 — December 2020.
<table>
<thead>
<tr>
<th></th>
<th>VIX Low</th>
<th>VIX Med</th>
<th>VIX High</th>
<th>VIX Low</th>
<th>VIX Med</th>
<th>VIX High</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Panel A1: Positive RSV</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>RSV Low</td>
<td>1.23</td>
<td>1.29</td>
<td>1.20</td>
<td>12.71</td>
<td>19.16</td>
<td>31.56</td>
</tr>
<tr>
<td>RSV Med</td>
<td>4.04</td>
<td>4.10</td>
<td>4.06</td>
<td>12.60</td>
<td>18.32</td>
<td>30.41</td>
</tr>
<tr>
<td>RSV High</td>
<td>9.55</td>
<td>9.43</td>
<td>9.37</td>
<td>12.49</td>
<td>18.04</td>
<td>28.11</td>
</tr>
<tr>
<td><strong>Panel A2: Average VIX</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>14.88</td>
<td>15.84</td>
<td>21.30</td>
<td>22.71</td>
<td>20.97</td>
<td>22.32</td>
</tr>
<tr>
<td><strong>Panel A3: OD Average Returns</strong></td>
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<td></td>
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<tr>
<td>RSV Low</td>
<td>0.59</td>
<td>0.80</td>
<td>2.33</td>
<td>1.74</td>
<td>0.54</td>
<td></td>
</tr>
<tr>
<td>RSV Med</td>
<td>-2.41</td>
<td>1.96</td>
<td>6.02</td>
<td>8.43</td>
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<tr>
<td>RSV High</td>
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<td>-0.11</td>
<td>-1.96</td>
<td>-1.84</td>
<td>0.44</td>
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<tr>
<td>High-Low</td>
<td>0.71</td>
<td>0.91</td>
<td>4.30</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>p-value</td>
<td>0.59</td>
<td>0.67</td>
<td>0.22</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>VIX Low</th>
<th>VIX Med</th>
<th>VIX High</th>
<th>High - Low</th>
<th>p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>RSV Low</td>
<td>0.88</td>
<td>4.93</td>
<td>12.66</td>
<td>11.78</td>
<td>0.00</td>
</tr>
<tr>
<td>RSV Med</td>
<td>3.23</td>
<td>6.33</td>
<td>13.03</td>
<td>9.80</td>
<td>0.00</td>
</tr>
<tr>
<td>RSV High</td>
<td>4.42</td>
<td>8.93</td>
<td>7.01</td>
<td>2.60</td>
<td>0.31</td>
</tr>
<tr>
<td>High-Low</td>
<td>3.54</td>
<td>3.99</td>
<td>-5.64</td>
<td></td>
<td></td>
</tr>
<tr>
<td>p-value</td>
<td>0.02</td>
<td>0.09</td>
<td>0.12</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Table IV. Double sorts on relative signed volume and closing VIX**

We split the sample into positive (panel a) and negative (panel b) closing relative signed volume. Within each set we double-sort trading days into terciles of relative signed volume RSV and the closing level of the VIX. Within each set we report average RSVs and VIX levels (A1, A2, B1, B2). Double sorted overnight drift OD return averages are reported (A3, B3) along with high minus low differences and p-values testing the difference against zero. Sample period is January 1998 – December 2020.
Table V. Regression: overnight returns on closing relative signed volume

Panel (a) displays regression estimates of hourly overnight returns regressed on closing relative signed volume:

\[ r_{t,n}^H = \mu_n + \beta_n^{SV} RSV_{t-1}^{close} + \varepsilon_{t,n} \quad n = 1, \ldots, 12. \]

Panel (b) estimates a multivariate extension to this regression that includes relative signed volume recorded in the final three hours of the trading day before the maintenance break. Days where the time difference between London and New York is different from 5 hours are excluded. Estimates are in basis points. \( t \)-statistics reported in parenthesis are computed from robust standard errors clustered within each month. Sample period is January 1998 – December 2020.
Table VI. Falsification test

Panel (a) displays regression estimates of hourly overnight returns regressed on a one hour lag of relative signed volume. Panel (b) displays regression estimates of hourly overnight returns regressed on twelve lags of hourly relative signed volume. Days where the time difference between London and New York is different from 5 hours are excluded. Estimates are in basis points. \( t \)-statistics reported in parenthesis are computed from robust standard errors clustered within each month. Sample period is January 1998 – December 2020.
Table VII. Regression: overnight returns on closing relative signed volume and interactions

Panel (a) displays regression estimates of hourly overnight returns regressed on closing relative signed volume and an interaction term that takes on a value of '1' if $RSV_{t−1}^{\text{close}} < 0$ and '0' otherwise

$$r_{t,n}^H = \mu_n + \beta_n^{RSV} RSV_{t-1}^{\text{close}} + \beta_n^{NEG} N_{t,n} \cdot \beta_n^{RSV \times NEG} RSV_{t-1}^{\text{close}} \times N_{t,n} + \epsilon_{t,n}, \quad n = 1, \ldots, 12.$$

Panel (b) displays regression estimates of hourly overnight returns regressed on closing relative signed volume and an closing signed volume interacted with the level of the VIX from the close of the preceding day

$$r_{t,n}^H = \mu_n + \beta_n^{RSV} RSV_{t-1}^{\text{close}} + \beta_n^{VIX} VIX_{t-1}^{\text{close}} + \beta_n^{RSV \times VIX} RSV_{t-1}^{\text{close}} \times VIX_{t-1}^{\text{close}} + \epsilon_{t,n}, \quad \text{for } n = 1, \ldots, 12,$$

Days where the time difference between London and New York is different from 5 hours are excluded. Estimates are in basis points. $t$-statistics reported in parenthesis are computed from robust standard errors clustered within each month. Sample period is January 1998 – December 2020.
Table VIII. Daylight saving tests

In panel (a) hourly overnight returns are regressed on closing relative signed volume and a dummy variable for daylight savings time:

\[ r_{t,n}^H = \mu_n + \beta_{n}^{RSV} RSV_{t-1} + \beta_{n}^{DST} I_{DST,t} + \beta_{n}^{RSV \times DST} RSV_{t-1,close} \times I_{DST,t} + \epsilon_{t,n} \quad n = 1, \ldots, 12, \]

where the dummy variable takes on a value of ‘0’ in winter time (DST not active) and ‘1’ in summer time (DST active) and daylight savings is seen from a U.S. perspective. The Tokyo Stock Exchange (TSE) opens at 19:00 when DST is not active and at 20:00 when DST is active. Estimates are in basis points. In panel (b) hourly overnight returns are regressed on closing relative signed volume and time-zone difference dummy:

\[ r_{t,n}^H = \mu_n + \beta_{n}^{RSV} RSV_{t-1,close} + \beta_{n}^{DIFF} I_{DIFF,t} + \beta_{n}^{RSV \times DIFF} RSV_{t-1,close} \times I_{DIFF,t} + \epsilon_{t,n} \quad n = 1, \ldots, 12, \]

where the dummy variable takes on a value of ‘0’ when the time-zone difference between London and New York is 5 hours (3282 observations) and a value of ‘1’ when the time-zone difference is 4 hours (240 observations). t-statistics reported in parenthesis are computed from robust standard errors clustered within months. Sample period is January 1998 – December 2020.
### Table IX. Trading strategies

Summary statistics for returns of intraday trading strategies excluding (panel (a)) and including (panel (b)) transaction costs. **CTC** is continuously holding the E-mini contract. **CTO** is holding the contract from 16:15 to 8:30; **OTC** is from 9:30 to 16:15; **−OR** is shortening the opening returns from 8:30 to 10:00; **OD** is the overnight drift from 2:00 to 3:00; **OD+** is from 1:30 to 3:30. **RSV_{close}\_t-1 < 0** is a buy the dip strategy that goes long from 1:30 to 3:30 only on days following a negative closing order flow. Means and standard deviations are in annualized percentages. The Sharpe ratios uses the 4 week U.S. Treasury bill as the risk-free rate. Betas are computed using the **CTC** return as the market return. Returns excluding transaction cost are computed from mid quotes and returns including transaction costs are computed from the best bid and ask prices quotes. The sample period is 2004.1 — 2020.12. The trading strategies start in 2004 as this is where the overnight bid/ask spread reached its effective minimum of 1 tick.

<table>
<thead>
<tr>
<th></th>
<th><strong>CTC</strong></th>
<th><strong>CTO</strong></th>
<th><strong>OTC</strong></th>
<th><strong>OD</strong></th>
<th><strong>OD+</strong></th>
<th><strong>RSV_{close}_t-1 &lt; 0</strong></th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Mean</strong></td>
<td>8.95</td>
<td>4.62</td>
<td>4.20</td>
<td>3.75</td>
<td>6.21</td>
<td>6.07</td>
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<td><strong>Sdev</strong></td>
<td>19.35</td>
<td>11.23</td>
<td>14.90</td>
<td>2.65</td>
<td>4.13</td>
<td>2.95</td>
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<tr>
<td><strong>Sharpe ratio</strong></td>
<td>0.42</td>
<td>0.34</td>
<td>0.23</td>
<td>1.10</td>
<td>1.30</td>
<td>1.78</td>
</tr>
<tr>
<td><strong>beta</strong></td>
<td>1.00</td>
<td>0.37</td>
<td>0.63</td>
<td>0.02</td>
<td>0.04</td>
<td>0.02</td>
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<tr>
<td><strong>Skew</strong></td>
<td>0.01</td>
<td>−0.67</td>
<td>−0.33</td>
<td>1.18</td>
<td>2.16</td>
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<td><strong>Kurt</strong></td>
<td>20.06</td>
<td>20.86</td>
<td>13.65</td>
<td>32.91</td>
<td>41.88</td>
<td>98.60</td>
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</table>

(a) Without Transaction Costs

<table>
<thead>
<tr>
<th></th>
<th><strong>CTC</strong></th>
<th><strong>CTO</strong></th>
<th><strong>OTC</strong></th>
<th><strong>OD</strong></th>
<th><strong>OD+</strong></th>
<th><strong>RSV_{close}_t-1 &lt; 0</strong></th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Mean</strong></td>
<td>8.95</td>
<td>0.38</td>
<td>−0.05</td>
<td>−0.59</td>
<td>1.91</td>
<td>4.04</td>
</tr>
<tr>
<td><strong>Sdev</strong></td>
<td>19.35</td>
<td>11.23</td>
<td>14.90</td>
<td>2.65</td>
<td>4.12</td>
<td>2.92</td>
</tr>
<tr>
<td><strong>Sharpe ratio</strong></td>
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<td>−0.04</td>
<td>−0.06</td>
<td>−0.54</td>
<td>0.26</td>
<td>1.10</td>
</tr>
<tr>
<td><strong>beta</strong></td>
<td>1.00</td>
<td>0.37</td>
<td>0.63</td>
<td>0.02</td>
<td>0.04</td>
<td>0.02</td>
</tr>
<tr>
<td><strong>Skew</strong></td>
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<td>−0.68</td>
<td>−0.35</td>
<td>1.09</td>
<td>2.10</td>
<td>4.77</td>
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<tr>
<td><strong>Kurt</strong></td>
<td>20.06</td>
<td>20.84</td>
<td>13.67</td>
<td>32.81</td>
<td>41.61</td>
<td>99.87</td>
</tr>
</tbody>
</table>

(b) With Transaction Costs
Figure 1. Overnight vs intraday e-mini volume split
Panel (a) plots average daily trading volumes in the SP and ES contracts with the ES split by overnight versus intraday trading sessions. Panel (b) plots year-by-year average percentages of overnight volume relative to total volume for the ES contract. Volumes are measured as the total number of contracts traded. The sample period for overnight trading is January 1998 - December 2020.
Figure 2. Intraday return averages
This figure plots the average hourly log returns (bars) and average cumulative 5-minute log returns (solid black line) holding the e-mini contract (first close-to-open and then open-to-close). Sample period is January 1998 - December 2020.
Figure 3. Intraday return averages

This figure plots average 5 minute returns holding the e-mini contract for the hours 1.00 – 4.00. Sample period is January 1998 - December 2020.
Figure 4. Bootstrapped estimates

The distribution of hourly log return mean estimates is calculated using a block bootstrap (BS) sampling 10,000 times where days are partitioned into 24 sub periods as in Table 1. The optimal block length is chosen following Patton, Politis, and White (2009). Panel (a) plots the distribution of all hourly returns pooled. Panel (b) plots the distribution of returns during 2:00 – 3:00. Panel (c) plots the distribution of all hourly t-statistics pooled. Panel (d) plots the distribution of t-statistics for 2:00 – 3:00. Panels (e) and (f) are equivalent to panels (a) and (c) after removing returns between 2:00 – 3:00 from the 24 sub periods. Dotted blue lines mark the 95% confidence interval. Black dotted lines represent median estimates for specific hours. Each histogram is normalised such that it represents a probability density function estimate, i.e., the sum of the bar areas is equal to 1. Sample period is January 1998 - December 2020.
Figure 5. Intraday return averages: subsamples
This figure plots the average hourly log returns (bars) and average cumulative 5-minute log returns (solid black line) holding the e-mini contract (first close-to-open and then open-to-close). Panel (a) plots the sample period is January 1998 - December 2010. Panel (b) plots the sample period is January 2011 - December 2020. Blue highlighted bars indicate Bonferroni corrected p-values which are significant at the 5% level or less which account for the multiple testing nature of our 24-hour dissection.
Figure 6. Return persistence

This figure displays the cumulative log returns to a $1 initial investment that trades various sub-periods of the day. Sample period is January 1998 – December 2020. Panel (a) considers long positions in the hours {24-01, 01-02, 02-03} in addition to an extended window spanning 24 - 03. Panel (b) considers the cumulative returns to a short position between 9-10 or 17-18. Sample period is January 1998 - December 2020.
Figure 7. Year-by-year

This figure plots yearly average log returns (top panels) and \((1 - p)\) the values from a t-test against the null hypothesis that these returns are zero (bottom panels). Sub captions indicate the hour of the night. Sample period is January 1998 – December 2020.
Figure 8. Intraday equity volumes

Panel (a) plots the average 5 minute trading volume of the e-mini for the entire trading day, showing the full intraday pattern of volume. Panel (b) focuses only on volume outside U.S. open hours. Volumes are normalised by dividing each 5-minute volume by its daily volume, and then averaging normalised 5-minute intervals over all days in the sample. Panel (c) plots average volumes for all hours of the day during 2020. Panel (d) zooms in on average overnight volumes during 2020.
Figure 9. Volume time

This figure displays the cumulative log returns and the cumulative signed volume in both clock time and volume time and sorted by closing signed volume ($SV_{close}$) from the previous trading day. Volume time is defined such that a one increment step on the x-axis advances each time a single contract is traded. The sample period is January 2007 – December 2020.
Figure 10. Average overnight returns sorted on closing imbalance

Panels (a) – (b) sort trading days based on ten sets of closing relative signed volume ($RSV_{close}$) of the preceding trading day and average annualized returns of each group are plotted subsequent Asian trading hours (18:00 – 2:00), for returns during European trading hours (1:00 – 4:00), for returns during the overnight drift hour (2:00 – 3:00). Panel (d) zooms in on the overnight drift hour for closing order flow sorts straddling zero imbalances. Sample period is January 1998 – December 2020.
Figure 11. E-mini trading volume: Asian hours

Figure displays average trading volume in the e-mini contract for the Asian trading hours. Volumes are normalised by dividing each 5-minute volume by its daily volume, and then averaging normalised 5-minute intervals over all days in the sample. Trading days are split into days where U.S. daylight savings time (DST) is active and where DST is not active, as the main Asian countries do not observe daylight savings time. Seen from a U.S. perspective, the Tokyo Stock Exchange (TSE) opens at 19:00 when U.S. DST is not active and at 20:00 when U.S. DST is active. TSE reopens at 22:30 (23:30) after its lunch break when U.S. DST is not active (active). All volumes are computed as averages of the 5 minute volume relative to the total daily volume. The sample period is January 2007 – December 2020.
Figure 12. Cumulative returns with and without transaction costs

Figure displays time series of cumulative returns for a one dollar investment in various intraday trading strategies for the e-mini contract. The investment starts in 2004 when the overnight spread reached its effective minimum of one tick (0.25 index points). Panel (a) is excluding (including) transaction costs. CTC is continuously holding the e-mini contract. OD is the strongest part of the overnight drift from 2:00 to 3:00, OD+ is from 1:30 to 3:30 and buy the dip goes long from 1:30 to 3:30 only on day following a negative closing order flow. The black line shows the cumulative risk-free return measured as the return of a 4 week U.S. Treasury bill. Returns excluding transaction cost are computed from the mid quotes and returns including transaction costs are computed from the best bid and best ask price.
sections A.1 reports supplementary results to our central empirical contribution which is the documentation of consistent positive returns for holding U.S. equity futures around the opening of European financial markets. section A.3 provides a survey of Grossman and Miller (1988) (GM) interpreting the results of that paper in the context of our setting. Section A.2 reports robustness tests related to our market making explanation. This section repeats our main inventory risk tests with an alternative measure of order imbalance. Section A.4 discusses a series of alternative explanations based on volatility risk, liquidity risk, the arrival of overnight news, and the resolution of uncertainty.

A.1. Supplementary Results: Overnight Drift

A. Relationship to existing overnight literature

Figure A.1 displays cumulative close-to-close ($CTC$) log returns on S&P 500 futures: $1 invested at the beginning of 1983 becomes $27 dollars by the end of 2020, translating into an annual log return of 8.65%. Decomposing into intraday versus overnight components open-to-close ($OTC$) log returns averaged 5.12% while close-to-open ($CTO$) log returns averaged 3.53% This figure updates the findings of Cliff, Cooper, and Gulen (2008) and Kelly and Clark (2011) who both document that equities earn a substantial proportion of their returns during the overnight period. Overnight return patterns are also well discussed in the financial press.38. We note here that earning a substantial overnight returns is not, in itself, that surprising. Given the length of the overnight period one would even expect the overnight period to earn the largest return if information flowed continuous as in a Black-Scholes economy. What is surprising, is that the overnight versus intraday return dissection only becomes noticeable after the advent of overnight electronic markets. Indeed, the red and blue lines track each other quite closely until after the introduction of GLOBEX and shortly before the introduction of the e-mini contract. These dates are marked by vertical dotted lines. Our discovery of an overnight drift in U.S. equities during the opening of European markets and our explanation based on demand for immediacy are closely related to this long standing puzzle.

[Insert figure A.1 here]

B. Supplementary Results: Section II

B.1. Day of the week

Panel (a) of figure A.3 plots cumulative 5-minute returns sampled for each trading day of the week. In terms of close-to-close returns, $r_{CTC}^{TUE} \sim r_{CTC}^{WED} \sim r_{CTC}^{THU}$ while returns on Mondays and Fridays are significantly lower. Considering the $OD$, it is clearly visible in each day of the week, and displays far less dispersion than close-to-close returns, suggesting that it is a systematic phenomenon. Panel (a) of Table A.5 tests this claim formally using a regression dummy framework as above. In all days

of the week, the 2:00 - 3:00 return is positive and significant at the 1% level and the magnitude of the returns is also quite similar.

Panel (b) of Table A.5, on the other hand, shows that the OP returns are always negative but only statistically significant on Thursdays and Fridays with mean returns equal to $-2.10$ and $-3.03$ basis points per hour per day, with $t$-statistics equal to $-2.02$ and $-2.76$, respectively. Figure A.10 reports three pieces of suggestive evidence as to why the OP occurs only on Thursdays and Fridays: Firstly, we observe more U.S. macro announcements released at 8:30 on Thursdays and Fridays. Generally, we experience large positive returns leading up to announcements, as has been documented in the literature (Savor and Wilson (2013)). We conjecture that (short-lived) price-reversals following the macro announcements partly explain the negative opening returns. Secondly, we do not observe many FOMC announcements on Thursdays and Fridays and we also know that returns typically are positive in the hours leading up to FOMC announcements which subsequently do not revert Lucca and Moench (2015). Thirdly, we observe most negative earnings announcements days are Thursdays and Fridays. In summary, while OP returns is concentrated in the final days of the week, OD returns are systematically positive and significant in each day of the week.

[ Insert figure A.3 and A.10 and table A.5 here ]

B.2. Month of the year

Panel (b) of figure A.4 plots average cumulative 5-minute returns across the trading day for the futures contract roll months March, June, September and December. While ID returns display significant variation, in particular OP are large and negative in September equal to $-3.45\%$, opening returns are either slightly positive or negative in other months. The OD, however, is clearly visible in all months. More formally, Table A.6 reports the statistical significance within each calendar month. Consistent with Figure A.4, the OD drift is positive in all months of the year and statistically significant at conventional levels in 9 out of 12 months.

[ Insert figure A.4 and table A.6 here ]

A.2. Supplementary Results: Section III & IV of paper

Sections III and IV conducted a number of tests of the relationship between the overnight drift and trading imbalances as predicted by by inventory risk models along the lines of Grossman and Miller. In these sections, we primarily measured end-of-day (EOD) order imbalances in terms of RSV and the sample period was 1998–2020. In this part of the OA we present counterparts to the results of the main body but using SV instead. We use the sample period 2007–2020 since total volumes were relatively stationary over this period, see figure A.6. Using the SV measure in the early sample period would be problematic since volumes has increased by more than a factor 1000 since the early 2000’s; thus, an order imbalance of 1000 contracts would be massive in 1998 when the e-mini had just started trading but it would be small in 2020.

Table A.7 reports summary statistics for hourly $SV_t$. On average, close-to-close $SV_t$ is equal to -2,217 contracts ($t$-stat = -3.27), is highly volatile, and negatively skewed. Indeed, the median $SV_t$ is actually positive. Negative $CTC$ $SV_t$’s are consistent with the idea that the futures market is

39Closing order imbalances can be very extreme as seen in 2006 where the was a net selloff of more than 250,000 contracts in the last hour of trading: A sense of calm that returned to the market Tuesday disappeared in the final minutes of trading as stocks gyrated and reversed earlier gains. see www.money.cnn.com/2006/05/23/markets/markets_newyork/index.htm.
traded as a hedging instrument for the underlying. However, while \( SV_t \)'s are negative during the day, they are largely positive overnight. During the \( OD \) hour, \( SV_t \) is equal to 124 contracts with a t-statistic of 4.23, mirroring the unconditional positive returns during this hour. Panel (c) zooms in on the signed volume during the closing hour of U.S. trading. In the following, we use the last hour preceding the maintenance to measure closing order imbalances. Thus, \( SV^\text{close}_t \) denotes the order imbalance based on all trades sampled during the hour 15:15 – 16:15.

[ Insert table A.7 here ]

Consistent with the findings for the sample period January 1998 – December 2020 using \( RSV^\text{close}_t \), figure A.7 shows that sorting days based on \( SV^\text{close}_t \), positive overnight returns occur only on nights following market sell-offs (negative end-of-day order imbalances). Price reversals following market rallies are much more modest thus we have uncovered a strong demand asymmetry between long and short inventory positions. Consistent with the prediction of GM that higher price uncertainty should command a higher liquidity premium, table A.8 reports double sorts on \( SV^\text{close}_t \) and EOD VIX and shows that the \( OD \) returns are amplified in states of higher ex-ante volatility but only following market sell-offs. Finally, table A.9 confirms high frequency return predictability arising at the opening of European financial markets via projections onto \( SV^\text{close}_t \).

[ Insert figure A.6, figure A.7, table A.8 and table A.9 here ]

From inventory models we know that order flow predicts returns. However, the more liquid a market is, the shorter the period of predictability should be because liquidity providers can quickly trade imbalances away. In illiquid markets, such as corporate bonds, you can observe predictability over days. For the e-mini, negatively autocorrelated return predictability usually only lasts a couple of minutes. For example, figure A.8 displays 5 minute predictability regressions of returns on lagged signed volume for lags out to one hour. Only the first 5-minute lag is significantly negative. The bottom panel shows this pattern shows up in returns at the same frequency. What makes predictability by the order imbalance at the closing of U.S. trading hours special, is that the volumes transacted are much larger than those traded in the subsequent hours. Therefore, a market maker providing immediacy in this market is faced with a (potentially) large order imbalance at the end of the day that will take a long(er) time to trade away overnight, creating a longer-horizon return predictability overnight. Indeed, this is precisely the fundamental assumption of Grossman-Miller style models: market makers have to absorb excess order flow in the near term in the hope of new traders arriving at some point in the future.

[ Insert figure A.8 here ]


There exists a risk free asset (cash), \( B \), with a zero rate of return, and a risky futures contract that pays \( S_3 \) at date \( t = 3 \) where \( S_3 \) is conditionally normally distributed. Public information about \( S_3 \) arrives before trading in period 1 and again before trading in period 2:

\[
S_3 = S_2 + \epsilon_3 = S_1 + \epsilon_2 + \epsilon_3 = \mu + \epsilon_2 + \epsilon_3, \tag{A.1}
\]

where news shocks \( \epsilon_2, \epsilon_3 \sim \mathcal{N}(0, \sigma_i^2) \).
Trading Periods

Assume there are \( N \) competitive market makers (MM) with a CARA utility function and identical risk aversions \( \alpha \). At \( t = 0 \) dealers hold a non-zero cash position but a zero position in the risky asset: \( q_0^{MM} = 0 \). In period \( t = 1 \), a representative intraday liquidity trader (ID), who holds an initial endowment of \( q_0^{ID} \) futures contracts, executes a transaction of \( q_1^{ID} \) contracts. Dealers provide immediacy at \( t = 1 \) by trading with the ID agent and next period \( t = 2 \) dealers meet a representative overnight liquidity trader (ON), who trades an offsetting amount. Denote the initial endowments of the ID and ON trader as \( q_0^D = I = -q_0^{ON} \). Demand for immediacy thus arises because the liquidity demand by non-market-maker traders in period 1 is asynchronous with the liquidity supplied by overnight liquidity traders that arrive in period 2. The ID liquidity trader thus faces the risk of delaying execution until one period later, or, offloading some of that trade now to the market markets who start with zero inventory but are willing to carry some inventory in exchange for a liquidity premium (expected transaction return).

The problem of determining equilibrium quantities and prices is solved backwards in time. At \( t = 2 \), agent \( i \in \{MM_1, \ldots, MM_n, ID, ON\} \) maximizes their expected utility subject to their budget constraints

\[
\max_{q_2^i} E_2[-\exp(-\alpha W_3^i)]
\]

\[
W_2^i = B_2^i + q_2^i S_2 = B_1^i + q_1^i S_2 \tag{A.3}
\]

\[
W_3^i = B_2^i + q_3^i S_3 \tag{A.4}
\]

\[
= W_2^i + q_2^i (S_3 - S_2), \tag{A.5}
\]

where the expectation is taken conditional on the information set realized at date \( t = 2 \). Eliminating the cash position from the problem is equivalent to

\[
\max_{q_2^i} \alpha(W_2^i + q_2^i(E_2[S_3] - S_2)) - \frac{1}{2}(\alpha q_2^i \sigma_t)^2. \tag{A.6}
\]

The first order condition is

\[
q_2^{*,i} = \frac{E_2[S_3] - S_2}{\alpha \sigma_t^2} \tag{A.7}
\]

\[
q_2^{*,i} = \frac{E_2[S_3] - S_2}{\alpha \sigma_t^2} - q_0^i, \tag{A.8}
\]

where in the second line we have written the first order condition in ‘excess demand’ terms

\[
\tilde{q}_t^i = q_t^i - q_0^i. \tag{A.9}
\]
Market clearing in period 2 gives us:

\[
0 = \sum_i q_i^2 = \left[ \frac{E_2[S_3] - S_2}{\alpha \sigma_t^2} - I \right] + N \cdot \left[ \frac{E_2[S_3] - S_2}{\alpha \sigma_t^2} \right] + \left[ \frac{E_2[S_3] - S_2}{\alpha \sigma_t^2} + I \right].
\]  

(A.10)

Moving backwards one period, at \( t = 1 \), the portfolio choice problem is now solved by the set of agents \( i \in \{ MM_1, \ldots, MM_n, ID \} \) and given by

\[
\max_{q_i^1} E_1 \left[ -\exp(-\alpha W_i^2) \right] \quad (A.11)
\]

\[
W_i^2 = B_i^1 + q_i^1 S_2 \quad (A.12)
\]

\[
W_i^1 = B_i^1 + q_i^1 S_1 = B_0^1 + q_0^1 S_1, \quad (A.13)
\]

which is equivalent to

\[
\max_{q_i^1} \alpha (W_i^1 + q_i^1 (E_1[S_2] - S_1)) - \frac{1}{2}(\alpha q_i^1 \sigma_t)^2. \quad (A.14)
\]

The first order condition in excess demand terms is given by

\[
q_i^{*,i} = \frac{E_1[S_2] - S_1}{\alpha \sigma_t^2} - q_0^1 = \frac{\mu - S_1}{\alpha \sigma_t^2} - q_0^1. \quad (A.15)
\]

Imposing market clearing in period \( t = 1 \) and remembering \( q_0^{MM} = 0 \) and \( q_0^{ID} = I \)

\[
q_i^{ID} + N q_i^{MM} = 0 \quad (A.16)
\]

\[
(N + 1) \frac{\mu - S_1}{\alpha \sigma_t^2} = I, \quad (A.17)
\]

and so the equilibrium clearing price is given by

\[
S_1 = \mu - I \sigma_t^2 \frac{\alpha}{N + 1}. \quad (A.18)
\]

At this point, it is worth making clear that the ID agent does not offload their entire initial position to the MM. Substituting the equilibrium price back into the optimal demands we see

\[
q_i^{*,MM} = \frac{I}{N + 1} \quad (A.19)
\]

\[
q_i^{*,ID} = -N q_i^{*,MM} = -\frac{N I}{N + 1} \quad (A.20)
\]

\[
q_i^{*,ID} = I - N \frac{I}{N + 1}. \quad (A.21)
\]

The larger the number of dealers present, the greater is the optimal initial position that is immediately traded. For example, with the introduction of a single EOD MM, 50% of the initial order imbalance will be carried overnight by the MM. In the CME e-mini market, on average since 2009, there are more than 30 dealers continually posting quotes at the best bid and ask, implying that 96% of imbalances, conditional on a liquidity event, will be absorbed end-of-day and carried
overnight.

Now, define the return $R_{\text{ON}} = (S_2 - S_1)/S_1$ which compensates the dealer for holding inventory between $t = 1 \to t = 2$. Then, from (A.17) and using $\sigma_t^2 = \text{Var}_1[S_2] = S_1^2 \text{Var}[S_2/S_1] = S_1^2 \text{Var}[R_{\text{ON}}] = S_1^2 \sigma_{R,t}^2$, we have

$$
(N + 1) \frac{E_1[S_2] - S_1}{\alpha S_1^2 \sigma_{R,t}^2} = \mathcal{I}
$$

(A.22)

$$\Leftrightarrow \quad \frac{E_1[S_2] - S_1}{S_1} = S_1 \mathcal{I} \times \sigma_{R,t}^2 \times \frac{\alpha}{N + 1},
$$

(A.23)

which shows that expected overnight return are comprised of

$$
E_1[R_{\text{ON}}] = \text{Dollar Order Imbalance} \times \frac{\text{Return Variance}}{\text{Risk Bearing Capacity}}^{-1}.
$$

(A.24)

From $R_{\text{ON}} = (S_2 - S_1)/S_1$, we can also consider the conditional covariance of the overnight return and the intraday order imbalance (from the perspective of period $t = 0$ such that $S_1 \mathcal{I}$ is random):

$$
\text{cov}_0[S_1 \mathcal{I}, R_{\text{ON}}] = -\text{var}_0(S_1 \mathcal{I}) \sigma_{R,t}^2 \times \frac{\alpha}{N + 1},
$$

(A.25)

which shows that the size of the reversal following the date $t = 1$ imbalance is larger when

- dollar order imbalance is larger (more variable)
- conditional variance is larger
- dealer risk bearing capacity is smaller

While the size of the price reversal above is variable, the speed of the reversal happens very fast and always within one period. This is because $q_0^{ID} = \mathcal{I} = -q_0^{ON}$. Relaxing this assumption one can solve for the case $q_0^{ID} = \mathcal{I} = -\Delta q_0^{ON}$. The case of $\Delta > 1$ implies a large overnight demand while the case $\Delta < 1$ implies a small overnight demand. It is straightforward to solve this model and we find that lower overnight demand will increase the magnitude of return reversals but the speed of mean reversion (between $t = 0$ and $t = 3$) is slower. Thus, lower overnight demand implies that overnight return reversals are not completed until later in the overnight session.

We now turn to the potential relationship between dealer risk bearing capacity and return variance. Keeping fixed the number of dealers, we can endogenize dealer risk aversion by incorporating a value-at-risk (VaR) constraint into the market maker’s problem, as is done, for example, in Danielsson, Shin, and Zigrand (2004); Adrian and Shin (2010, 2014a) and the subsequent literature. More specifically, we modify the optimization problem (A.14) to include a VaR constraint, so that the market makers solve

$$
\max_{q_i^{MM_i}} - \alpha (W_1^{MM_i} + q_i^{MM_i}(E_1[S_2] - S_1)) + \frac{1}{2} (\alpha q_i^{MM_i} \sigma_t)^2
$$

(A.26)

s.t.

$$
\bar{p} \geq \mathbb{P}_1 \left( W_1^{MM_i} + q_i^{MM_i}(E_1[S_2] - S_1) - W_2^{MM_i} \geq \text{VaR} \right).
$$

(A.27)
That is, the market maker maximizes expected utility of providing inter-period liquidity (as in A.14) but now subject to the probability of losses larger than the permitted value-at-risk (VaR) being lower than a pre-specified permitted probability $\bar{p}$. Denote by $\Phi (\cdot)$ the distribution function of the standard normal. Then we can rewrite (A.27) as

$$\Phi \left( \frac{-\text{VaR}}{\sigma_{W_{2,MMi}}} \right) \leq \bar{p},$$

or, equivalently,

$$\sigma_{W_{2,MMi}}^2 \leq \left( \frac{\text{VaR}}{\Phi^{-1}(1-\bar{p})} \right)^2 \equiv \bar{v}. \quad (A.28)$$

Here, $\sigma_{W_{2,MMi}}$ is the volatility of period 2 wealth, given period 1 information, which, for the market makers, is given by $\sigma_{W_{2,MMi}} = q_{1,MMi} \sigma_t$. Denoting by $\alpha \lambda_t / 2$ the Lagrange multiplier on the simplified VaR constraint (A.28), we can thus rewrite the market makers’ optimization problem as

$$\max_{q_{1,MMi}} \alpha (W_{1,MMi} + q_{1,MMi} (E_1[S_2] - S_1)) - \frac{1}{2} (\alpha q_{1,MMi} \sigma_t)^2 - \frac{\alpha \lambda_t}{2} \left( \bar{v} - (q_{1,MMi} \sigma_t)^2 \right) = 0 = \frac{\alpha \lambda_t}{2} \left( \bar{v} - (q_{1,MMi} \sigma_t)^2 \right). \quad (A.30)$$

Thus, in the presence of a VaR constraint, the optimal demand by a market maker is given by

$$q_{1,MMi}^* = \frac{\mu - S_1}{(\alpha + \lambda_t) \sigma_t^2}, \quad (A.31)$$

and the market maker’s effective risk aversion becomes $\alpha + \lambda_t$. For a given level of the permitted value-at-risk and permitted probability $\bar{p}$, increases in volatility tighten the value-at-risk constraint, raising the effective risk aversion of value-at-risk constrained market makers. Similarly, if the permitted value-at-risk is given as a fraction of equity – so that $\text{VaR} = \varphi W_{1,MMi}$ – rather than as a dollar amount, the value-at-risk constraint is tighter when market maker equity declines.

The framework above suggests that value-at-risk may serve as a reasonable proxy for market maker capital commitments to the trade. Value-at-risk is a measure of economic capital, that is, the capital required to absorb losses in excess of expected loss due to current risks. As noted in, for example, the BCBS white paper on “Range of practices and issues in economic capital frameworks”:

40 Economic capital was originally developed by banks as a tool for capital allocation and performance assessment.

In other words, banks use notions of economic capital to determine the composition of the asset side of their balance sheets, both from the perspective of the relative size of different lines of business as well as from the perspective of allocating to business units within each line of business. We thus view that using a measure of economic capital as being appropriate in the context of evaluating market maker risk bearing capacity. Although bank capital regulation has famously evolved over our sample period, the major regulatory changes have a limited impact on economic capital as it relates.

\[^{40}\text{https://www.bis.org/publ/bcbs152.pdf}\]
to equity futures since both the futures and the underlying basket of securities are exchange-traded throughout our sample period, and are on-balance-sheet items for supervised institutions. More specifically, we focus on the equity VaR as opposed to the total VaR of reporting institutions. Conversations that the Federal Reserve Bank of New York conducted with major market participants following the implementation of post-crisis banking regulation suggest that large financial institutions allow different business lines to make day-to-day allocation decisions independently, as long as the overall economic capital allocated to that business line (and, indeed, business unit) is not exhausted. Thus, for example, the equity futures “desk” makes day-to-day trading decisions independent of the Treasury desk. We thus view using equity VaR as balancing the desired definition of what constitutes a market maker in the market against the feasibility of granularity available in the data.

Acknowledging that our calculation is by its nature an approximation, we note that, even if the true economic capital allocated to the e-mini futures market is 10 times higher, our relative risk aversion estimate is comfortably within the range previously estimated in the literature.

Completing the derivation, the modified market clear condition in equation A.16 becomes

$$\left(\frac{\mu - S_1}{\alpha \sigma_t^2}\right) + N\left(\frac{\mu - S_1}{(\alpha + \lambda_t)\sigma_t^2}\right) = I$$

(A.32)

from which the equilibrium EOD price is now given by

$$S_1 = \mu - I\sigma_t^2 \left(\frac{\alpha^2 + \alpha \lambda_t}{N(\alpha + \lambda_t) + \alpha}\right)$$

(A.33)

from which we identify the modified risk bearing capacity as

$$RBC_t = \frac{N(\alpha + \lambda_t) + \alpha}{\alpha^2 + \alpha \lambda_t}$$

(A.34)

Then from

$$\frac{\partial RBC_t}{\partial \alpha} = -\frac{1}{(\alpha + \lambda)^2} - \frac{N}{\alpha^2}$$

(A.35)

$$\frac{\partial RBC_t}{\partial \lambda} = -\frac{1}{(\alpha + \lambda)^2}$$

(A.36)

we see the sensitivity of $RBC_t$ w.r.t risk aversion is strictly larger (in magnitude) compared to the non-constrained case, adjusted by a term that is the sensitivity of $RBC$ w.r.t the probability of the constraint binding. The expected overnight return becomes

$$E_t[R_{ON}] = \text{Dollar Order Imbalance} \times \text{Return Variance} \times RBC_t^{-1}$$

(A.37)

and from equations A.35 and A.36 it is straightforward to show that expected overnight returns are strictly increasing in both risk aversion and the tightness of the dealer constraint.

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41 Post-crisis changes to capital regulation had the biggest impact on over-the-counter, non-centrally cleared, off-balance-sheet securities.
A.4. Alternative Explanations

In this subsection we link CRSP, Computstat and IBES datasets for S&P 500 firms to build intraday and overnight earnings surprises, and consider international macro announcements from Bloomberg, and central bank announcements sourced from Bloomberg and central bank websites. We also exploit tick-by-tick trades and quotes on VIX futures (VX) sourced from Refinitiv and complemented with data from CBOE.

A. Volatility Risk

Figure A.11 (a) depicts average realized intraday volatility (squared log returns) from 1998.1–2020.12 sampled at a 1-minute frequency. The intraday volatility displays the well-known U-shaped pattern for Asian, European and US trading hours where volatility is high at the beginning and at the end of each trading period Andersen, Bondarenko, Kyle, and Obizhaeva (2018). Across trading periods, the level of volatility is lowest during Asian trading hours and highest during US trading hours, relative to the average trading volume across the 3 periods. Comparing average levels for each session, we find that US hours volatility is more than twice as large as Asian hours volatility and therefore considerably larger than estimates of return volatility using close-to-close prices. The large spike in volatility at 8:30 is caused by the spike in volume observed just after US macro announcements. Figure A.11(b) plots time series of the realized volatility for each of the three trading periods. The volatility is always lowest during Asian hours and highest during US hours but the difference has diminished over time as trading volume in the overnight session has picked up. The 3 time series are highly positively correlated, indicating that volatility increases on the same days for all three trading periods. More importantly, we do not observe an obvious link between realised quantities of risk and returns.

B. Overnight Liquidity

To measure liquidity risk we construct hourly estimates of 1) Kyle (1985) lambda (based on returns sampled at the 1-min frequency), 2) the Amihud price impact measure and 3) the bid-ask spread. Figure A.12 depicts the average intraday patterns of these measures as well as their time series for the Asian, European and U.S. trading hours. As expected, intraday illiquidity is lowest during U.S. trading hours where the trading activity is highest and illiquidity is highest during Asian hours when the trading activity is at its lowest. The bid-ask spread is very close to the minimum tick size (0.25 index points) at all times during the trading day. All liquidity measures experience large changes throughout the sample period. Most notably, the overnight illiquidity (Asian and European hours) has decreased strongly as overnight trading activity has picked up, and today is much closer to the illiquidity level in regular U.S. trading hours. Secondly, the illiquidity increases during times of crises, as one would expect.

Considering all three measures, we do not observe intraday patterns which could rationalize the OD returns with theories of liquidity risk. We see average intraday bid-ask spreads are almost always trading at the minimum tick size, equal to 0.25 index points. The spread is only significantly higher after 16.30 when trading resumes after the maintenance break and volumes are close to zero (see figure 8). The jumps in the bid-ask spread at 8:30 and 10:00 corresponds to the U.S. macro announcements which are released at these times.
In addition, since we observe the aggregate limit order book for the market, we can also measure intraday illiquidity by computing the depth of the market. Market depth is computed as the number of contracts available in each 5 minute interval, and is reported for the first five levels on each side of the order book. Figure A.14 shows the intraday depth averaged across all days in the 2009.1-2020.12 sample. Here we observe that, at each level, the depth of the bid is equal to the depth of the ask. We also note there are three depth regimes differentiated by Asia, European and U.S. trading hours. Depth is flat in Asian hours and rises throughout European hours.

At U.S. open, depth increases steeply, remains relatively flat during the regular U.S. hours and then spikes at U.S. close before dropping in the overnight market. However, we also see that the overnight market remains highly liquid. For example, until 2.00 at the top level (L1) there are, on average, 100 contracts available, which in dollar terms with the S&P level at 2000 is equal to $10 million at the bid or ask. Considering all levels, L1 - L5 depth rises to $80 million. Indeed, a highly liquid overnight market is consistent with the large overnight volumes traded in this market, which as noted in the introduction, have averaged in excess of $15 billion daily.

[C. Overnight News]

We now consider if overnight news released after the U.S. cash market close are not immediately incorporated into prices during Asian hours but instead accumulate and are resolved at European open when trading volumes increase. Indeed, a large fraction of U.S. corporate earnings announcements are released after U.S. market close. Furthermore, Asian and European macro or central bank information released during the U.S. overnight session may signal news about U.S. growth prospects. Explanations for the overnight drift along these lines are related to a literature that shows conditional risk premia are higher on days prior to and on days of macroeconomic announcements.\footnote{In the context of stock returns, Savor and Wilson (2014) show that equity risk premia are consistently larger on U.S. inflation, GDP and non-farm announcements days. Lucca and Moench (2015), on the other hand, document a drift in the U.S. stock market which precedes FOMC announcements.}

We study this conjecture by examining hour-by-hour returns conditional on U.S. earnings announcements., and U.S., Japanese or European macro- and central bank announcements.

C.1. Earnings Announcements

We test if firm-specific announcements predict intraday returns. Previous literature (see e.g. Bernard and Thomas, 1989; Sadka, 2006, and the subsequent literature) has documented a positive (negative) drift in stock prices of individual firms following a positive (negative) earnings announcement surprise. The earnings data is obtained from I/B/E/S and Compustat. Following Hirshleifer, Lim, and Teoh (2009), for each firm $i$ and on day $t$ we define the earnings surprise as

$$ES_{i,t} = \frac{A_{i,t} - F_{i,t-1}}{P_{i,t-1}},$$

where $A$ is the actual earnings per share (EPS) as reported by the firm, $F$ is the most recent median forecast of the EPS and $P$ is the stock price of the firm at the end of the quarter. As I/B/E/S updates the professional forecasters’ expectations on a monthly basis, the shock is the difference between the actual earnings and forecasters expected earnings approximately 1 month prior to the announcement date. Scaling the shock $A - F$ by the stock price implies that firm shocks are equally

[Insert figures A.12 and A.14 here]
weighted.\textsuperscript{43} We define the daily earnings surprise of the S&P 500 index, \( ES_t \), as the daily sum of all \( ES_i \).

Figure A.15 plots the time series of \( ES_t \). The shocks are periodic on a quarterly basis and generally positive (\( \sim 75\% \) of all shocks are positive). Notably, we see large negative shocks during the financial crisis and almost exclusively positive shocks following the crisis.

To test this conjecture formally, we sort all trading days based on \( ES_t \). We choose only announcements that are published after U.S. close (16:00 ET). This is because the effect of announcements published early in the day should be incorporated into the price on that day, while announcements that occur after CTO hours could affect returns in these hours. Table A.13 reports the average returns for day \( t + 1 \) after sorting on \( ES_t \). We sort all trading days into 5 groups based on \( ES_t \). In group 1, \( ES_t < 0 \). For group 2-4, \( ES_t \) is positive and increasing by group. Group 5 is for days where \( ES_t \) is zero, i.e. not a single firm announced their earnings prior to these days (this was \( \sim 46\% \) of all trading days. The table contains a number of interesting findings. First, we see a strong monotonic positive relation between earnings shocks and CTC returns across groups. Second, no news days have the highest CTC return, equal to 4.57 \% p.a, with a t-statistic of 1.86, and in this sense “no news is good news”. Third, negative shocks are not incorporated into the price until the U.S. market opens, while positive shocks are incorporated immediately during the CTO period. However, most importantly for the focus of this paper, we do not detect a post close information effect: the OD is not driven by earnings announcements as it is positive and significantly different from zero for all 5 set of days.

\[\text{[Insert figure A.15 and table A.13 here]}\]

\textbf{C.2. Macro and Central Banks}

From Bloomberg’s Economic Calendar we collect dates and times for

- U.S.: Non-farm Payrolls; CPI Ex Food and Energy; GDP QoQ.
- EU: Unemployment Rate; PPI MoM; Industrial Production SA MoM.
- U.K.: Jobless Claims Change; CPI Ex Food and Energy; QoQ.
- Japan: Jobless Rate; PPI MoM; Industrial Production MoM.

Announcement times are generally close to 8:30 ET in the U.S., 2:00 ET in the Eurozone, 4:30 ET in the U.K, and 19:50 ET in Japan.

For central banks, we collect announcement dates and times from the websites of the following central banks: \( (i) \) FOMC; \( (ii) \) the ECB; \( (iii) \) the BoE; \( (iv) \) the BoJ. FOMC target rate announcements are released at or very close to 14:15 ET. ECB target announcements are at 6:45 ET, followed by a press conference at 7:30 ET. BoE announcement days often coincide with ECB days and the announcements are at 7:00 ET. Finally, BoJ announcements do not occur at a regular time but target rate decisions are generally announced between 22.00 and 1.00 ET. Our sample period is January 1998 to December 2020.

We test the effect of announcements on hourly subinterval returns in a regression framework with dummy variables which take a ‘1’ on days with an announcement and ‘0’ otherwise. More specifically, the dummy takes a value of 1 if the announcement occurs within the current \textit{calendar

\begin{footnotesize}
\textsuperscript{43}EPS is earnings per share outstanding, implying that EPS/P is earnings per market cap.
\textsuperscript{44}We also test specifications of \( ES_t^{500} \) where firms are value weighted and result are similar.
\end{footnotesize}
day. Thus, Japanese and European macro announcements are contemporaneous with the overnight return, while U.S. announcements occur subsequent to the overnight returns. The regression we estimate is

$$r_{t,n}^H = a_n + b_{1}^n 1_{U.K.} + b_{2}^n 1_{EU} + b_{3}^n 1_{JP} + b_{4}^n 1_{U.S.} + \varepsilon_n,$$

(A.38)

where $1_i$ is a macro or central bank announcement dummy for country $i$.

Panel (a) of table A.14 reports estimates for macro announcements. The intercept during the OD hour (2:00–3:00) is estimated to be 1.52 bps with a t-statistic of 5.98, i.e. the drift is present on non-announcement days and thus not driven by macro announcements. Furthermore, none of the announcement dummies are statistically different from the non-announcement days in this hour. The U.K. macro dummy is economically large and significant negative at the 10% level at 3:00 (which is 8:00 in London). More generally, we fail to detect an announcement effect in any of the overnight hours. U.S. announcements occur at 8:30 and indeed we see a large positive return of 3.22 bps with a t-statistics of 2.29. Panel (b) of table A.14 reports estimates for central bank announcements. Again, the intercept is unaffected at 2:00-3:00 and we obtain an estimate of 1.40 bps with a t-statistic of 6.52. The BoE dummy is economically large and marginally significantly positive between 4:00 - 5:00 consistent with central bank announcement premium. The FOMC dummy is large but insignificant.

Summarizing, we fail to detect a relationship between the overnight drift and (i) earnings announcements that are released after the close of the cash market, during Asian hours, or (ii) overnight news from Asian or European central bank or macro announcements; thus, it is unlikely that the overnight drift is driven by risk compensation related to announcement premia.

C.3. Resolution of Uncertainty

The results directly above suggest that the overnight drift is unlikely to be related to an information effect. Recent literature (see e.g. Ai and Bansal (2018) for the theoretical argument and Hu, Pan, Wang, and Zhu (2019) for suggestive empirical evidence), however, has argued that resolution uncertainty, as measured by changes in the VIX, ahead of macroeconomic announcements could explain the pre-announcement drift of Lucca and Moench (2015). More recently, in work subsequent to ours, Bondarenko and Muravyev (2020) postulate uncertainty resolution at the open of European markets as a possible explanation for the central empirical result of our paper (figure 2).

To investigate this hypothesis, we consider changes in volatility by computing intraday and overnight VIX futures ($VX$) returns. Indeed, investors wanting to manage volatility risks around the clock can now trade VIX futures ($VX$) contracts in all time zones. $VX$ futures are open nearly 23 hours a day, 5 days a week, trading electronically on the CBOE futures exchange. $VX$ is closed daily from 16:15 to 16:30 and from 17:00 to 18:00 ET. On Sundays, they start at 6:00 ET. $VX$ futures trade with a dollar value of $1000 \times$ the level of the VIX Index. Regular expirations are on the Wednesday 30 days before the corresponding S&P 500 option expiration. Due to holidays the option expiration date may be irregular and settle on the preceding Tuesday. $VX$ futures contracts trade with monthly expirations and we consider a position that trades the front month contract and rolls into the next-to-delivery contract on the Monday preceding expiration Wednesdays and thus avoiding settlement returns.

Panel (a) of figure A.16 displays the average cumulative 5-minute log returns for the front month $VX$ contract. The intraday $VX$ returns are relatively flat during the U.S. hours. At the
close of regular U.S. trading hours, in the run up to the maintenance break, \( VX \) returns are strongly negative, exceeding -80% p.a.\(^{45}\) During regular Asian trading hours \( VX \) returns rebound, generating annualized returns of 50% between 18:00 and 1:00. At the opening of European markets \( VX \) returns are negative, equal to 50% p.a between 2:00 and 4:00. Panel (a) of table A.15 reports average overnight hourly \( VX \) returns, measured in basis points, which are highly statistically significant around European open.

Focusing on \( VX \) returns at European open, one can easily rationalize a contemporaneous negative co-movement with \( ES \) returns (absent a resolution of uncertainty conjecture) in terms of the ‘leverage effect’, which is the well known empirical fact that equity volatility tends to fall (rise) when equity returns are positive (negative). A common explanation for this phenomenon is due to Black (1976) and Christie (1982) who argue that companies become mechanically more leveraged as equity prices decline relative value of their debt and, as a result, their equity values become more volatile as in Merton (1974). Panel (b) of figure A.16 demonstrates the leverage effect in intraday data by computing the intraday 1-minute correlations between \( ES \) and \( VX \) futures returns \((r_{i}^{ES} \times r_{i}^{VX})\) for intervals where we observe quote updates and averaging these over all days in our sample. During both overnight and intraday periods the correlation is close to -80% which demonstrates that economic interpretations of resolution of uncertainty based on a contemporaneous \( VIX \) relationship is limited: “correlation does not imply causation”.

More interesting, is the question of whether end-of-day order imbalances in one futures contract predict overnight returns in the other contract. Table A.15 answers this question by estimating two sets of high frequency predictability regressions. Panel (a) reports multivariate regressions with e-mini returns on the left and EOD \( ES \) and \( VX \) order imbalances on the right hand side

\[
ES r_{t,n}^{H} = \mu_{n} + \beta_{n}^{ESP} ES SV_{t-1}^{close} + \beta_{n}^{VXSP} VX SV_{t-1}^{close} + \epsilon_{t,n}, \quad \text{for } n = 1, \ldots, 12,
\]

while panel (b) replaces the left hand sides with \( VX \) returns

\[
VX r_{t,n}^{H} = \mu_{n} + \beta_{n}^{VXSP} VX SV_{t-1}^{close} + \beta_{n}^{ESP} ES SV_{t-1}^{close} + \epsilon_{t,n}, \quad \text{for } n = 1, \ldots, 12.
\]

Summarizing the table, while \( ES \) imbalances at U.S. close predict subsequent overnight returns in both the \( ES \) and the \( VX \) contracts, \( VX \) imbalances only predict overnight \( VX \) returns. Overnight \( ES \) returns between 2:00 and 3:00 are forecastable by closing \( ES \) order imbalance after controlling for \( VX \) order imbalances. \( VX \) returns, on the other hand, are predicted by \( ES \) order imbalances between 2:00 and 3:00 and then subsequently we observe some marginally significant predictability by \( VX \) order imbalances between 4:00 and 6:00, albeit with positive and negative signs.

Thus, while \( ES \) and \( VX \) returns are contemporaneously mechanically linked through the leverage effect, overnight returns in both markets are predicted by end-of-day imbalances in the \( ES \), making the resolution of uncertainty hypothesis an unlikely explanation for the overnight drift.

\[\text{[Insert figure A.16 here]}\]

\[\text{[Insert tables A.15 here]}\]

---

\(^{45}\)Volumes between 16:15 and 18:00 are very low and we do not report returns or correlations for this period of the day.
### A.5. Tables

<table>
<thead>
<tr>
<th>Hour</th>
<th>18-19</th>
<th>19-20</th>
<th>20-21</th>
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<th>02-03</th>
<th>03-04</th>
<th>04-05</th>
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<th>07-08</th>
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<td>−0.04</td>
<td>−0.06</td>
<td>−0.20</td>
<td>−0.06</td>
<td>0.54</td>
<td>0.50</td>
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<td>0.14</td>
<td>0.39</td>
<td>−0.01</td>
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</tr>
<tr>
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<td>0.73</td>
<td>−0.14</td>
<td>−0.22</td>
<td>−0.85</td>
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<td>2.41</td>
<td>2.29</td>
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<td>1.32</td>
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<td>1.47</td>
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</tr>
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<td>0.89</td>
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<td>0.022</td>
<td>9.8 \cdot 10^{-9}</td>
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<td>0.59</td>
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<td>0.96</td>
<td>0.45</td>
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<td>0.14</td>
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<td>0.77</td>
<td>0.05</td>
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<td>0.35</td>
<td>0.58</td>
<td>−0.22</td>
</tr>
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<td>−1.39</td>
<td>−3.46</td>
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<td>−0.83</td>
<td>5.96</td>
<td>−0.54</td>
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<td>1.23</td>
<td>0.49</td>
<td>1.44</td>
</tr>
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<td>85.42</td>
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<td>28.07</td>
<td>152.23</td>
<td>28.61</td>
<td>31.58</td>
<td>15.26</td>
<td>20.24</td>
<td>17.54</td>
<td>38.40</td>
<td>47.81</td>
<td>47.59</td>
</tr>
</tbody>
</table>

(a) Summary statistics for S&P 500 e-mini futures hourly returns occurring overnight. Returns are computed from volume-weighted average prices. Panel (a) displays overnight hours and panel (b) displays intraday hours. Mean, medians and standard deviations are displayed in basis point terms. Sample period is January 1998 — December 2020.
Table A.2. Summary statistics: January 1998 — December 2010
Summary statistics for S&P 500 e-mini futures hourly returns. Returns are computed from mid quotes at the top of the order book. Panel (a) displays overnight hours and panel (b) displays intraday hours. Mean, medians and standard deviations are displayed in basis point terms. t-statistics testing again the null of zero returns are computed from HAC robust standard errors. Sample period is January 1998 — December 2010.
Table A.3. Summary statistics: January 2011 — December 2020

Summary statistics for S&P 500 e-mini futures hourly returns. Returns are computed from mid quotes at the top of the order book. Panel (a) displays overnight hours and panel (b) displays intraday hours. Mean, medians and standard deviations are displayed in basis point terms. t-statistics testing again the null of zero returns are computed from HAC robust standard errors. Sample period is January 2011 — December 2020.
### Table A.4. Benjamini–Yekutieli Thresholds

The table provides Benjamini–Yekutieli (BY) corrected significance levels (thresholds) for the null hypotheses of the S&P 500 e-mini futures average hourly log returns being zero. The BY procedure is a method to handle multiple testing problems. Specifically, it aims to control the false discovery rate which is the expected ratio of the number of type I errors to the total number of rejections of the null. The BY method is a ‘step up’ procedure that computes null specific thresholds starting from the least significant hypothesis and working up until significant alternative hypotheses are detected. This implies that ever test has a unique threshold (see Harvey, Liu, and Saretto (2020) for a recent survey of multiple testing procedures in the context of financial economic applications). In the table, returns are computed from mid quotes at the top of the order book and reported in basis points. Means are displayed in basis point terms. t-statistics testing again the null of zero returns are computed from HAC robust standard errors. p-values indicate significance levels under a student-t distribution. BY thresholds are shown at the 10%, 5% and 1% level. A threshold is denoted with a ⋆ if the corresponding p-value of a test is below the given threshold. Panel (a) displays overnight hours and panel (b) displays intraday hours. Sample period is January 1998 — December 2020.

#### Panel (a) Overnight

<table>
<thead>
<tr>
<th>Hour</th>
<th>18-19</th>
<th>19-20</th>
<th>20-21</th>
<th>21-22</th>
<th>22-23</th>
<th>23-24</th>
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<th>01-02</th>
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<th>07-08</th>
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</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
<td>−0.46</td>
<td>0.35</td>
<td>0.15</td>
<td>0.05</td>
<td>−0.03</td>
<td>0.04</td>
<td>0.46</td>
<td>0.43</td>
<td>1.48</td>
<td>0.35</td>
<td>−0.08</td>
<td>0.15</td>
<td>0.61</td>
<td>−0.08</td>
<td>0.26</td>
</tr>
<tr>
<td>t-stat</td>
<td>−1.43</td>
<td>1.80</td>
<td>0.68</td>
<td>0.25</td>
<td>−0.19</td>
<td>0.29</td>
<td>2.77</td>
<td>2.75</td>
<td>7.13</td>
<td>1.33</td>
<td>−0.32</td>
<td>0.63</td>
<td>2.46</td>
<td>−0.31</td>
<td>0.71</td>
</tr>
<tr>
<td>p-value</td>
<td>0.15</td>
<td>0.072</td>
<td>0.50</td>
<td>0.80</td>
<td>0.85</td>
<td>0.77</td>
<td>0.0056</td>
<td>0.0060</td>
<td>1.1 · 10⁻¹²</td>
<td>0.18</td>
<td>0.75</td>
<td>0.53</td>
<td>0.014</td>
<td>0.75</td>
<td>0.48</td>
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<tr>
<td>BY 10% threshold</td>
<td>0.0088</td>
<td>0.0077</td>
<td>0.014</td>
<td>0.023</td>
<td>0.022</td>
<td>0.0033</td>
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<td>0.00011*</td>
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<td>BY 5% threshold</td>
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<td>0.012</td>
<td>0.011</td>
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<td>0.00055*</td>
<td>0.0050</td>
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<td>0.0077</td>
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<tr>
<td>BY 1% threshold</td>
<td>0.00088</td>
<td>0.00077</td>
<td>0.0014</td>
<td>0.0023</td>
<td>0.0024</td>
<td>0.0022</td>
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<td>0.00099</td>
<td>0.0020</td>
<td>0.0015</td>
<td>0.00066</td>
<td>0.0021</td>
<td>0.0013</td>
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</tbody>
</table>

#### Panel (b) Intraday

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<th>Hour</th>
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<th>10-11</th>
<th>11-12</th>
<th>12-13</th>
<th>13-14</th>
<th>14-15</th>
<th>15-16</th>
<th>16-17</th>
<th>17-18</th>
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</thead>
<tbody>
<tr>
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<td>−1.24</td>
<td>−0.25</td>
<td>−0.23</td>
<td>0.41</td>
<td>−0.15</td>
<td>−0.06</td>
<td>0.61</td>
<td>0.00</td>
<td>−0.43</td>
</tr>
<tr>
<td>t-stat</td>
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<td>−0.45</td>
<td>−0.52</td>
<td>1.07</td>
<td>−0.37</td>
<td>−0.12</td>
<td>0.99</td>
<td>0.01</td>
<td>−3.62</td>
</tr>
<tr>
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<td>0.28</td>
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<td>0.91</td>
<td>0.32</td>
<td>1.00</td>
<td>0.00030</td>
</tr>
<tr>
<td>BY 10% threshold</td>
<td>0.0055</td>
<td>0.018</td>
<td>0.017</td>
<td>0.011</td>
<td>0.019</td>
<td>0.025</td>
<td>0.012</td>
<td>0.027</td>
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</tr>
<tr>
<td>BY 5% threshold</td>
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<td>0.0055</td>
<td>0.0094</td>
<td>0.013</td>
<td>0.0061</td>
<td>0.013</td>
<td>0.0011*</td>
</tr>
<tr>
<td>BY 1% threshold</td>
<td>0.00055</td>
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<td>0.0017</td>
<td>0.0011</td>
<td>0.0019</td>
<td>0.0025</td>
<td>0.0012</td>
<td>0.0026</td>
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</table>
### Table A.5. Day of week mean returns

Mean returns are estimated for each day of the week by projecting hourly return series on a set of dummy variables, one for each hour of the day, for all days in the sample. Estimates are in basis points. *t*-statistics reported in parenthesis are computed from HAC robust standard errors. Sample period is January 1998 — December 2020.

#### (a) Overnight hourly returns

<table>
<thead>
<tr>
<th>Hour</th>
<th>18-19</th>
<th>19-20</th>
<th>20-21</th>
<th>21-22</th>
<th>22-23</th>
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<th>01-02</th>
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<th>04-05</th>
<th>05-06</th>
<th>06-07</th>
<th>07-08</th>
<th>08-09</th>
</tr>
</thead>
<tbody>
<tr>
<td>Monday</td>
<td>-3.65</td>
<td>0.67</td>
<td>0.71</td>
<td>0.00</td>
<td>0.15</td>
<td>0.32</td>
<td>-0.30</td>
<td>-1.10</td>
<td>1.54</td>
<td>1.22</td>
<td>0.06</td>
<td>-0.20</td>
<td>0.81</td>
<td>1.29</td>
<td>0.17</td>
</tr>
<tr>
<td>t-stat</td>
<td>(-2.39)</td>
<td>(1.51)</td>
<td>(1.50)</td>
<td>(0.00)</td>
<td>(0.43)</td>
<td>(0.99)</td>
<td>(-0.93)</td>
<td>(-0.27)</td>
<td>(3.23)</td>
<td>(1.89)</td>
<td>(0.11)</td>
<td>(-0.40)</td>
<td>(1.54)</td>
<td>(2.49)</td>
<td>(0.21)</td>
</tr>
<tr>
<td>Tuesday</td>
<td>0.89</td>
<td>0.75</td>
<td>0.26</td>
<td>0.93</td>
<td>-0.07</td>
<td>0.07</td>
<td>0.51</td>
<td>1.03</td>
<td>1.55</td>
<td>-0.29</td>
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<td>1.32</td>
<td>1.03</td>
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<td>(0.23)</td>
<td>(1.61)</td>
<td>(2.93)</td>
<td>(3.26)</td>
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<td>(2.59)</td>
<td>(1.70)</td>
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<td>(0.36)</td>
<td>(0.48)</td>
<td>(2.17)</td>
<td>(0.03)</td>
<td>(3.94)</td>
<td>(0.04)</td>
<td>(0.61)</td>
<td>(0.72)</td>
<td>(0.42)</td>
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<td>(-1.24)</td>
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<td>Thursday</td>
<td>-0.22</td>
<td>1.38</td>
<td>1.41</td>
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<td>0.10</td>
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<td>-0.90</td>
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<td>-1.00</td>
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<tr>
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<td>(-0.79)</td>
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<td>(1.36)</td>
<td>(2.83)</td>
<td>(0.17)</td>
<td>(0.72)</td>
<td>(-1.58)</td>
<td>(1.01)</td>
<td>(-2.14)</td>
<td>(1.06)</td>
</tr>
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<td>0.01</td>
<td>-0.19</td>
<td>-0.10</td>
<td>0.79</td>
<td>0.74</td>
<td>1.28</td>
<td>0.79</td>
<td>-0.36</td>
<td>0.09</td>
<td>0.47</td>
<td>-0.31</td>
<td>1.48</td>
</tr>
<tr>
<td>t-stat</td>
<td>(1.39)</td>
<td>(-2.63)</td>
<td>(-2.90)</td>
<td>(0.02)</td>
<td>(-0.44)</td>
<td>(-0.32)</td>
<td>(1.43)</td>
<td>(1.92)</td>
<td>(2.60)</td>
<td>(1.28)</td>
<td>(-0.63)</td>
<td>(0.17)</td>
<td>(0.84)</td>
<td>(-0.58)</td>
<td>(1.39)</td>
</tr>
</tbody>
</table>

#### (b) Intraday hourly returns

<table>
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Table A.6. Month of year mean returns

Mean returns are estimated for each month of the year by projecting hourly return series on a set of dummy variables, one for each hour of the day, for all days in the sample. Estimates are in basis points. \(t\)-statistics are computed from HAC robust standard errors. Sample period is January 1998 — December 2020.

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(a) Overnight hourly returns

(b) Intraday hourly returns
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(a) Overnight

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(b) Intraday

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(c) EOD

Table A.7. Summary statistics: signed volume around the clock

Summary statistics for S&P 500 e-mini futures hourly signed volume defined as

$$SV_t = \# buy\ orders - \# sell\ orders,$$

which states order imbalance measured in terms of number of contracts. Panel (a) displays overnight hours and panel (b) displays intraday hours. Panel (c) displays $SV_t$ in quarterly intervals between 15:00 – 16:15 (ET) and in the final column reports summary statistics for $SV_t^{close}$ which is signed volume measured between 15:15 – 16:15 (ET). Mean, medians and standard deviations are displayed in millions of contracts. Sample period is January 2007 — December 2020.
### Table A.8. Double sorts on signed volume and closing VIX

We split the sample into positive (panel a) and negative (panel b) closing signed volume. Within each set we double-sort trading days into terciles of relative signed volume RSV and the closing level of the VIX. Within each set we report average RSVs and VIX levels (A1, A2, B1, B2). Double sorted overnight drift OD return averages are reported (A3, B3) along with high minus low differences and p-values testing the difference against zero. Sample period is January 2007 – December 2020.

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<th>Panel A2: Average VIX</th>
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<table>
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<td>SV Med</td>
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<td>-0.68</td>
</tr>
<tr>
<td>SV High</td>
<td>0.33</td>
<td>-1.29</td>
</tr>
<tr>
<td>High-Low</td>
<td>1.19</td>
<td>0.41</td>
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<table>
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<tr>
<th></th>
<th>Panel B1: Negative SV</th>
<th>Panel B2: Average VIX</th>
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<tr>
<td>SV Low</td>
<td>-2,747.50</td>
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<td>SV High</td>
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<table>
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<th>Panel B3: OD Average Returns</th>
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<td>SV Med</td>
<td>4.14</td>
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<td>SV High</td>
<td>4.98</td>
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<tr>
<td>High-Low</td>
<td>4.99</td>
<td>10.95</td>
</tr>
<tr>
<td>p-value</td>
<td>0.03</td>
<td>0.00</td>
</tr>
</tbody>
</table>

**Notes:**
- **RSV** refers to relative signed volume.
- **VIX** refers to the CBOE Volatility Index.
- **OD** refers to overnight drift.
Table A.9. Regression: overnight returns on closing signed volume

Panel (a) displays regression estimates of hourly overnight returns regressed on closing signed volume:

$$r_{t,n}^H = \mu_n + \beta_n SV_{t-1}^{close} + \varepsilon_{t,n} \quad n = 1, \ldots, 12.$$  

Panel (b) estimates a multivariate extension to this regression that includes relative signed volume recorded in the final three hours of the trading day before the maintenance break. Days where the time difference between London and New York is different from 5 hours are excluded. Estimates are in basis points. $t$-statistics reported in parenthesis are computed from robust standard errors clustered within each month. Sample period is January 1998 – December 2020.
### Table A.10. Falsification test

Panel (a) displays regression estimates of hourly overnight returns regressed on a one hour lag of signed volume. Panel (b) displays regression estimates of hourly overnight returns regressed on twelve lags of hourly relative signed volume. Days where the time difference between London and New York is different from 5 hours are excluded. Estimates are in basis points. *t*-statistics reported in parenthesis are computed from robust standard errors clustered within each month. Sample period is January 1998 – December 2020.
Table A.11. Regression: overnight returns on closing signed volume and interactions

Panel (a) displays regression estimates of hourly overnight returns regressed on closing signed volume and an interaction term that takes on a value of ‘1’ if $SV_{t-1}^{\text{close}} < 0$ and ‘0’ otherwise

$$r_{t,n}^{H} = \mu_{n} + \beta_{n}^{SV} SV_{t-1}^{\text{close}} + \beta_{n}^{NEG} 1_{NEG,t} + \beta_{n}^{SV \times NEG} SV_{t-1}^{\text{close} \times 1_{NEG,t}} + \epsilon_{t,n} \quad n = 1, \ldots, 12.$$  

Panel (b) displays regression estimates of hourly overnight returns regressed on closing signed volume and an closing signed volume interacted with the level of the VIX from the close of the preceding day

$$r_{t,n}^{H} = \mu_{n} + \beta_{n}^{SV} SV_{t-1}^{\text{close}} + \beta_{n}^{VIX} VIX_{t-1}^{\text{close}} + \beta_{n}^{SV \times VIX} SV_{t-1}^{\text{close}} \times VIX_{t-1}^{\text{close}} + \epsilon_{t,n} \quad \text{for } n = 1, \ldots, 12.$$  

Days where the time difference between London and New York is different from 5 hours are excluded. Estimates are in basis points. $t$-statistics reported in parenthesis are computed from robust standard errors clustered within each month. Sample period is January 2007 – December 2020.
Table A.12. Daylight saving tests

In panel (a) hourly overnight returns are regressed on closing relative signed volume and a dummy variable for daylight savings time:

\[ r_{t,n}^H = \mu_n + \beta_n^{SV} SV_{t-1}^\text{close} + \beta_n^{DST} 1_{DST,t} + \beta_n^{SV \times DST} SV_{t-1,close} \times 1_{DST,t} + \epsilon_{t,n} \quad n = 1, \ldots, 12, \]

where the dummy variable takes on a value of ‘0’ in winter time (DST not active) and ‘1’ in summer time (DST active) and daylight savings is seen from a U.S. perspective. The Tokyo Stock Exchange (TSE) opens at 19:00 when DST is not active and at 20:00 when DST is active. Estimates are in basis points. In panel (b) hourly overnight returns are regressed on closing signed volume and time-zone difference dummy:

\[ r_{t,n}^H = \mu_n + \beta_n^{SV} SV_{t-1}^\text{close} + \beta_n^{DIFF} 1_{DIFF,t} + \beta_n^{RSV \times DIFF} SV_{t-1,close} \times 1_{DIFF,t} + \epsilon_{t,n} \quad n = 1, \ldots, 12, \]

where the dummy variable takes on a value of ‘0’ when the time-zone difference between London and New York is 5 hours and a value of ‘1’ when the time-zone difference is 4 hours. \( t \)-statistics reported in parenthesis are computed from robust standard errors clustered within months. Sample period is January 2007 – December 2020.
Table A.13. Earnings announcements

We sort evening earnings announcements into negative, positive low/medium/high days, and non-announcement days. Within each sort we compute average returns for the close-to-close (CTC), close-to-open (CTO), open-to-close (OTC), overnight drift (OD) and opening return (OR) periods. We report t-tests of the difference against the null of zero in parenthesis. Sample period is 1998.1 – 2020.12.

<table>
<thead>
<tr>
<th></th>
<th>CTC</th>
<th>CTO</th>
<th>OTC</th>
<th>OD</th>
<th>OR</th>
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<tr>
<td>NEG</td>
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<td>-6.40</td>
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<td>(1.79)</td>
<td>(-1.34)</td>
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<tr>
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<tr>
<td>t-stat</td>
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<td>(-0.04)</td>
<td>(-0.07)</td>
<td>(3.45)</td>
<td>(-2.60)</td>
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<tr>
<td>POS-MEDIUM</td>
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<td>1.96</td>
<td>-0.64</td>
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<tr>
<td>t-stat</td>
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<td>(-0.18)</td>
<td>(0.50)</td>
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<td>(-0.43)</td>
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<td>POS-HIGH</td>
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<td>1.17</td>
<td>-0.12</td>
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<tr>
<td>t-stat</td>
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<td>(0.09)</td>
<td>(2.50)</td>
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<tr>
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<td>(1.60)</td>
<td>(1.17)</td>
<td>(4.91)</td>
<td>(-1.64)</td>
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Table A.14. Announcements

We test the effect of announcements on the fixing return pattern in a bilateral regression framework with dummy variables which take a ‘1’ on days with an announcement and ‘0’ otherwise. Specifically, for each subinterval return we estimate the following regression

\[ r_{H,t,n} = \mu_n + b_{1,n} 1_{\text{U.K.}} + b_{2,n} 1_{\text{EU}} + b_{3,n} 1_{\text{JP}} + b_{4,n} 1_{\text{U.S.}} + \varepsilon_{n,t}, \quad n = 1, \ldots, 15, \]

where for panel (a) \( 1_i \) is an employment, GDP or inflation announcement dummy for country \( i \). For panel (b) \( 1_i \) is a central bank announcement dummy for country \( i \). \( t \)-statistics are computed from HAC robust standard errors. Sample period is 1998.1 – 2020.12.

(a) Macro

<table>
<thead>
<tr>
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<th>18</th>
<th>19</th>
<th>20</th>
<th>21</th>
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<th>24</th>
<th>01</th>
<th>02</th>
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<td>0.80</td>
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<tr>
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<td>(0.06)</td>
<td>(0.85)</td>
<td>(2.16)</td>
<td>(-0.18)</td>
<td>(1.13)</td>
<td>(0.57)</td>
<td>(-0.07)</td>
<td>(0.15)</td>
<td>(0.39)</td>
<td>(0.40)</td>
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<td>1.39</td>
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<td>0.30</td>
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<td>(-0.18)</td>
<td>(-0.36)</td>
<td>(0.99)</td>
<td>(1.04)</td>
<td>(-0.84)</td>
<td>(2.13)</td>
<td>(0.23)</td>
<td>(1.50)</td>
<td>(1.07)</td>
<td>(-1.43)</td>
</tr>
</tbody>
</table>

(b) Central Banks
### Table A.15. Regression: overnight returns on closing signed volume: VX

Panel (a) displays regression estimates of hourly overnight VX returns regressed on a constant which measured the unconditional mean during this hour. Panel (b) displays regression estimates of hourly overnight ES returns regressed on ES and VX closing signed volume leading up to the U.S. close period of the previous trading day:

$$ES_{t,n}^H = \mu_n + \beta_n^{ESSV} ES_{SV_{t-1}}^{close} + \beta_n^{VXSV} VX_{SV_{t-1}}^{close} + \epsilon_{t,n}, \quad \text{for } n = 1, \ldots, 12,$$

Panel (c) displays regression estimates of hourly overnight VX returns regressed on ES and VX closing signed volume leading up to the U.S. close period of the previous trading day:

$$VX_{t,n}^H = \mu_n + \beta_n^{VXSV} VX_{SV_{t-1}}^{close} + \beta_n^{ESSV} ES_{SV_{t-1}}^{close} + \epsilon_{t,n}, \quad \text{for } n = 1, \ldots, 12,$$

Days where the time difference between London and New York is different from 5 hours are excluded. Estimates are in basis points. \(t\)-statistics reported in parenthesis are computed from robust standard errors clustered within each month. Sample period is 2015.1 – 2020.12
Figure A.1. Time series of returns for the S&P 500 futures contract

Figure plots the time series of close-to-close, open-to-close and close-to-open log returns to the S&P 500 BIG futures contract. Opening prices are sampled at 9:30 EST and closing prices are sampled at 16:15 EST. Between 1983.1 – 1998.1 returns are computed from VWAPs sourced from the CME. Between 1998.1 – 2004.4 returns are computed from the VWAPs sourced from the Refinitiv. Beyond 2004.1 until the end of the sample in 2020.12 we computed returns from the VWAPs on the e-mini contracts since this became the most liquidity futures contract traded on the SPX index.
Figure A.2. Global equity market trading hours

Figure displays opening and closing times for 14 global equity markets in June 2019. Green bars indicate opening times and red bars indicate closing times. The abbreviations are NYSE=New York Stock Exchange, TSE=Tokyo Stock Exchange, LSE=London Stock Exchange, HKE=Hong Kong Stock Exchange, NSE=National Stock Exchange of India, BMF=Bovespa Bolsa de Valores Mercadorias & Futuros de Sao Paulo, ASX=Australian Securities Exchange, FWB=Frankfurt Stock Exchange Deutsche Borse, RTS=Russian Trading System, JSE= Johannesburg Stock Exchange, DIFX=NASDAQ Dubai, SSE=Shanghai Stock Exchange, NZSX=New Zealand Stock Exchange, TSX=Toronto Stock Exchange. Opening and closing times are collected from the public websites of the exchanges and reported in Eastern Standard Time (ES). Several of the opening times shift by one or two hours when U.S. DST is not active (see table II for details).
Figure A.3. Day-of-week effects
This figure displays the cumulative 5-minute log returns of the e-mini across the trading day, for each day of the week, averaged across all trading days in our sample. Estimates are annualized and displayed in percentage points. Sample period is 1998.1 – 2020.12.

Figure A.4. Month-of-the-year effects
This figure displays the cumulative 5-minute log returns of the e-mini across the trading day, for each month in the March quarterly cycle, averaged across all trading days in our sample. Estimates are annualized and displayed in percentage points. Sample period is 1998.1 – 2020.12.
Figure A.5. Year-by-year returns: 9:00 - 10:00 & 17:00 – 18:00
This figure plots yearly average log returns (top panels) and $(1 - p)$ the values from a $t$-test against the null hypothesis that these returns are zero (bottom panels). Sub captions indicate the hour of the night. Sample period is January 1998 – December 2020.
Figure A.6. Distribution and time series of closing order imbalances

Distribution and time series of closing order imbalances. Order imbalances are measured both as the absolute order imbalance in number of contracts, $SV$ and the order imbalance relative to total trading volume, $RSV$. The closing period is defined as 15:15–16:15 ET. The sample period is January 1998 – December 2020.
Figure A.7. Average overnight returns sorted on closing imbalance

Panels (a) - (b) sort trading days based on ten sets of absolute closing order flow of the preceding trading day, $S_{t}^{close}$, and average annualized returns of each group are plotted. Subsequent Asian trading hours (18:00 – 02:00), for returns during European trading hours (01:00-04:00), for returns during the overnight drift hour (02:00 – 03:00). Panel (d) zooms in on the overnight drift hour for closing order flow sorts straddling zero imbalances. Sample period is January 2007 – December 2020.
Figure A.8. Autocorrelations

The top panel reports correlation coefficients between 5-minute log returns and lagged 5-minute relative signed volume. The bottom panel plots correlation coefficients between 5-minute log returns and lagged 5-minute log returns. Black bars indicate 95% upper and lower confidence intervals. Correlations are computed using all hours of the trading day for the sample period January 1998 - December 2020.
As in Adrian and Shin (2014a), for firms which report VaRs at the 95% confidence level, we scale the VaR to the 99% using the Gaussian assumption. This figure displays the time-series of the resulting equity VaR. Source: Bloomberg. Sample period is 1999 Q1 – 2020 Q4.
Figure A.10. Announcements per weekday

Figure displays the number of trading days, for each day of the week, where U.S. macro, bank or earnings announcements are released. Sample period is 1998.1 – 2020.12.
Figure A.11. Realized volatility
Panel (a) displays the average intraday realized volatility of the E-mini computed from 1-minute data. Volatility is annualized and displayed in percentage points. Panel (b) displays a time-series of annualised realised volatility sampled within Asian, European, and U.S. trading hours. Sample period is 1998.1 – 2020.12
Figure A.12. Liquidity measures
Figure displays the intraday Amihud measure, Bid–Ask spread and Kyle’s lambda of the E-mini and time series of the 3 measures for the Asian, European and U.S. trading hours. The sample period is 2004.1 – 2020.12.
Figure A.13. Times Series of the Bid–Ask Spread during the *OD* hour
Figure displays the times series of the average bid–ask spread for the E-mini S&P 500 Futures contract between 02:00–03:00. The sample period is January 1998 – December 2020.

Figure A.14. Market depth
Figure displays the average market depth measured at a 5 minute frequency throughout the trading day. Market depth is measured as the number of contracts available and is reported for the first five levels on each side of the order book. The sample period is 2009.1 – 2020.12.
Figure A.15. SUE score

Figure displays the time series of the SUE score for the S&P 500 index. The daily earnings surprise of the S&P 500 index is defined as the daily sum of all individual firm surprises, $ES_{i,t}$. For each firm $i$ and on day $t$ we define the earnings surprise as $ES_{i,t} = \frac{A_{i,t} - F_{i,t} - P_{i,t}}{P_{i,t}}$, where $A$ is the actual earnings per share (EPS) as reported by the firm, $F$ is the most recent median forecast of the EPS and $P$ is the stock price of the firm at the end of the quarter. The earnings data is obtained from I/B/E/S and Compustat. The sample period is 1998.1 – 2020.12.
Figure A.16. VIX Futures

Panel (a) displays the average hourly log returns (bars) and average cumulative 5-minute log returns (solid black line) of the VIX Futures contract (first close-to-open and then open-to-close). Panel (b) plots intraday 1-minute correlations between $ES$ and VX futures returns $(r_{t}^{ES} \times r_{t}^{VX})$ for intervals where we observe quote updates and averaging these over all days in our sample. The sample period is 2015.1 – 2020.12 but excludes VX expiration days and the day preceding VX expiration days.